# Real-Time Three-Dimensional Acoustic Imaging System with A Reflector and Its Applications

by Hirofumi Taki

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### **Preface**

Presentation of detailed environmental information allows a visually impaired person to live a life independently. To realize a robust vision substitute system with high time and spatial resolution we propose a through-air acoustic imaging system with a reflector mirror and a 2-D element array. In the proposed system, a transmitter radiates a wide beam to the entire measurement field. The echo from a target is gathered by a concave mirror. The distance between the reflector mirror and the element array is fixed, and thus the defocused image is distributed on the array. The image of the target is reconstructed from the received signal on the array by numerical back projection. Since the proposed imager measures the entire target field in a transmit and receive event, the imager has significantly high time resolution. Furthermore in this system most of the echo arrived at the mirror is gathered and received on the array. Thus the proposed imager has higher spatial resolution than that of a conventional imager with the same size element array. In this paper we evaluate the spatial resolution of the proposed imager using numerical calculation based on physical optics.

In order to transfer detailed environmental information to the visually impaired, we propose two stimulation methods to enhance transfer information using a 2-D tactile array. First, stimulators are divided into several groups. Since each stimulator group is activated alternately, the interval of stimulations can be shortened to less than the two-point discrimination threshold. In the case that stimulators are divided into two and four groups the number of stimulators increases to twice and four times, respectively, that in the case of the two-point discrimination threshold. Second, a user selects the measurement range and then the system presents targets within the range. The user acquires spatial information of the entire measurement area by changing the measurement range. This method can accurately present a range of targets. We examine and confirm these methods experimentally.

For the improvement of medical diagnoses a real-time 3-D medical acoustic imager is strongly desired. We propose a 3-D acoustic imager with a reflector and a 2-D dense element array for high time and spatial resolution. All elements on a small dense array are excited with proper time delays to transmit a broad beam similar to that of a single element transmitter. In this method a wide beam with high power is radiated, and thus the proposed imager has high signal-to-noise ratio. The echo is gathered by a concave reflector, and received by the dense array. The image of the target is reconstructed by

numerical back projection from the de-focused image distributed on the array. With this scheme, images of the entire measurement field can be reconstructed from a single transmit and receive event. For sidelobe suppression the reflection ratio of the reflector mirror is tapered off in the image reconstruction from the received signal. The synthesized transmit point can be changed in this system and thus the coherent integration of multiple receive signals of different transmit points improves the spatial resolution by using synthetic aperture technique. We also evaluate the spatial resolution of the proposed imager using numerical calculation based on physical optics.

## Contents

1	Ger	General introduction			
	1.1	.1 Instruction			
	1.2	Obsta	cle detection devices	2	
		1.2.1	White cane	2	
		1.2.2	Acoustic mobility aid devices	2	
		1.2.3	Laser sensing devices	6	
	1.3	Vision	substitute systems for environmental information	7	
	1.4		nation transfer method for sensory substitute system	9	
	1.5	Filtere	ed back projection	10	
	1.6	Medic	al acoustic 2-D imaging system	11	
		1.6.1	Mechanical scanning	11	
		1.6.2	Electronic scanning	13	
		1.6.3	Dynamic beam focusing	15	
	1.7	Medic	al acoustic 3-D imaging system	16	
		1.7.1	Mechanical scan of a single element probe	17	
		1.7.2	Manual or auto scan of a 1-D array with position tracking	17	
		1.7.3	Mechanical scan of a 1-D array	17	
		1.7.4	Electronic scan of a 2-D array	21	
2	A E	Iybrid	Method and Sensor for a High-resolution Ultrasound Vision		
	$\mathbf{Sub}$	$\dot{ m stitute}$	System for the Visually Impaired	<b>2</b> 3	
	2.1	Introd	uction	23	
	2.2	Princi	ple of the hybrid 3-D imaging system with a 2-D array and a reflector	24	
	2.3	Acous	tic propagation calculations	25	
	2.4	Off-foo	cus method for image reconstruction	27	
			nization of the mirror shape	29	
		2.5.1	Coordinate system used in the optimization of the mirror shape	31	
		2.5.2	Optimization of the mirror shape in the vertical section	32	
		2.5.3	Optimization of the mirror shape in a horizontal section	33	
		2.5.4	Optimization of the 3-D reflector mirror	34	
	2.6	Evalua	ation of the spatial resolution of the proposed imager in physical optics	36	

	2.7	Real-time signal processing
	2.8	Conclusion
2	тт	To the Control of the
3		man Interface and Transmit Frequency Control for The Through-Air oustic Real-Time High Resolution Vision Substitute System
	3.1	introduction
	3.2	Summary of High Resolution Vision Substitute System
	3.3	Transmit Frequency Control
	3.4	Spatial Information Transfer by Tactile Display
	0.1	3.4.1 Setting of stimulation points and measuring direction
		3.4.2 Spatial Information Transfer
	3.5	Conclusion
	0.0	Conclusion
4	_	h-Resolution Real-Time 3-D Acoustic Imaging System with a Re-
	flec	
	4.1	Introduction
	4.2	Materials and methods
		4.2.1 Principle of the hybrid 3-D imaging system with a small dense array
		and a reflector
		4.2.2 Calculation of acoustic propagation
		4.2.3 Optimization of the reflector shape and the array configuration
		4.2.4 Sidelobe suppression in image reconstruction
	4.3	Results
	4.4	Discussion
		4.4.1 Evaluation of the radiation pattern
		4.4.2 Considerations on signal-to-noise ratio
	4.5	Conclusion
5	Т	
<sub>0</sub>		nsfer Information Enhancement with a 2-D Tactile Stimulator Array an Acoustic Vision Substitute System
	5.1	Introduction
		Methods
	0.2	5.2.1 Alternating stimulation method
		5.2.2 Voluntary range selection
		$\sqrt{}$
		1
		5.2.4 Vibrotactile stimuli
		5.2.5 Participants
	۲.0	5.2.6 Main experiment
	5.3	Results
	5 4	Conclusion

6	Improvement of the Spatial Resolution of a 3-D Acoustic Medical Imag-				
	ing	System Based on Hybrid Method Using Synthetic Aperture Tech-			
	niqı	ue	96		
	6.1	Introduction	96		
	6.2	Formation of the transmit beam using a focusing method	98		
	6.3	Calculation parameters	99		
	6.4	Transmit time delays for focusing the transmit beam	99		
	6.5	The Region with a guaranteed focus	99		
	6.6	Improvement of the spatial resolution by multiple transmit and receive events	101		
	6.7	Results and Discussion	105		
	6.8	Conclusion	106		
$\mathbf{A}$	Pro	duction of the coefficient used in Eq. 2.1.	108		

## List of Tables

5.1	Variety of responses in the alternating stimulation method experiment. If	
	a participant perceives a 1-point pattern, he responds with one of the 8	
	numbers; 1-8. If he perceives a 4-point pattern, he selects one of the three	
	choices; left, middle, or right.	90
5.2	The average and the standard deviation of the possibility that the distance	
	between the position of the stimulation and that of the response is each	
	value when a 1-point stimulation is presented and the pattern of the re-	
	sponse is correct. The average is written in the upper line of each cell, and	
	the standard deviation with vinculum in the lower line	91
5.3	Definition of the variables used in the evaluation of the alternating stim-	
	ulation method. Their values are the numbers of the sensation responded	
	to in the experiment	92
5.4	The average and the standard deviation of the possibilities that the re-	
	sponse is correct or not correct when the response is a 4-point pattern,	
	The possibilities for 4-point and 1-point stimulations are defined simply as	
	$a_{22}/(a_{21}+a_{22}+a_{23})$ and $a_{12}/(a_{11}+a_{12}+a_{13})$ , respectively	92
5.5	The average and the standard deviation of the possibility that the response	
	is correct when a tactile pattern is a 4-point square stimulation	94

# List of Figures

1.1	Schematic view of a white cane	3
1.2	Schematic view of the wave propagation	4
1.3	Transmit and receive time when pulse waves are radiated	4
1.4	Frequency modulation of transmit and receive waves for target range de-	
	tection	5
1.5	Schematic view of the detection of target direction with two receive elements.	5
1.6	Schematic view of a laser triangulation system	7
1.7	Schematic view of the scan types of B-mode imagers	12
1.8	Schematic view of an annular array probe	12
1.9	Schematic view of an endoscope with a radial scan imager. The left and	
	right figure is the longitudinal and cross section of the endoscope	13
1.10	Beam scanning from the change of actibated elements. The change of	
		14
1.11	Schematic view of the beam formation employed by a sector scan probe	14
1.12	0 11	
	in a certain condition about element interval	15
1.13	Schematic view of the dynamic beam focusing. (1) Single transmit beam is	
	radiated for one measurement direction. (2) In the receive phase, the ele-	
	ment array employs various sets of time delays to acquire a narrow receive	
	beam at each measurement range. The recieve beams (a), (b), and (c) are	
	formed for short, middle, and long range measurement, respectively	16
	Schematic view of the mechanical scan of a 1-D array	18
	Schematic view of multi-line imaging	19
1.16	Transmit and receive schemes of a synthetic aperture imager. A wide trans-	
	mits beam is radiated to the entire measurement plane. Then all the image	
	lines in the measurement plane is formed in parallel. In the next transmit	
1 1 -	event, a transmit beam is radiated from the next transmit point	19
1.17		
	receive event. The coherent integration utilizing the synthetic aperture	
	technique realizes a spatial resolution equivalent to that of an aperture	0.0
	given by the convolution of the transmit points and the receive aperture	20

<ul><li>1.18</li><li>1.19</li></ul>	Since a transmit beam and a receive beam have different radiation patterns, the directions of grating lobes are different by each other. Therefore grating	20
	lobes are suppressed	22
2.1	Schematic view of the proposed vision substitute system	25
2.2	Arrangement of the sensor array and mirror	26
2.3	Schematic view of the auto-focus method.	28
2.4 2.5	Schematic view of the off-focus method	28
	exists at the center for a 100 cm depth	30
2.6	Received power distribution map on an element array. The distance between the array and the bottom of the mirror is 2.5 cm. A point target exists at the center for a 100 cm depth	30
2.7	Estimated power of an imager based on the off-focus method. A point target exists at the center for a 100 cm depth	31
2.8	Coordinate system used for optimization of the mirror shape	32
2.9	Angular characteristics of the efficiency of the proposed imager in a vertical section.	33
2.10		34
2.11	Schematic view of the constructed 3-D mirror using interpolation	35
	Angular characteristics of the efficiency of the proposed imager	36
	Lateral resolution of the proposed imager in a vertical plane	37
2.14	Lateral resolution of the proposed imager in a horizontal plane	38
2.15	Used area on the mirror when a target exists at the center	38
2.16	Receive power efficiency of the proposed imager in a horizontal plane	39
2.17	Used area on the mirror when a point target exists in a direction 30 degrees away from the center	40
3.1	Schematic view of the system	43
3.2	Angular characteristics of imaging calculated by physical optics in the vertical section	44
3.3	Frequency characteristics of the received signal power at various range	45
3.4	Signal to noise ratio versus range	46
3.5	Stimulating points on the forehead	47
3.6	Measuring directions in the target area. Intervals follow quadratic function.	47

3.7	Schematic view of targets in the measuring area. Color depth is related to echo power.	48
3.8	echo power	40
<b>0.</b> 0	power	49
3.9	Stimulating points matched with targets in the case of measuring distance	
3.10	is $d_1$ . Size indicates stimulating pressure related to echo power Stimulating points matched with targets in the case of measuring distance	49
	is $d_2$ . Size indicates stimulating pressure related to echo power	50
4.1	Schematic view of the system in the transmit phase	53
4.2	Schematic view of the system in the receive phase	54
4.3 4.4	Arrangement of a 2-D element array and a mirror in the transmit phase Schematic view of the mirror and array configuration for calculating in the	55
	time domain.	57
4.5	Arrangement of a 2-D element array and a mirror in the receive phase	58
4.6	Element pattern for a 797-element array	60
4.7	Waveform of the pulse used in this paper	61
4.8	The area used on the mirror in the x-z section. The value of used area is 1 and that of non-used area is 0. The x, y and z coordinates of a target are	
	0.005, 0 and 0.07 m respectively	62
4.9	Lateral resolution where the used area consists of plural groups. The main	
	lobe divides, and thus the sidelobe level becomes high	63
4.10	The used area on the optimized mirror in the x-z section. The value of the used area is 1 and that of the non-used area is 0. The x coordinates of targets are $-0.015$ , 0 and 0.015 m. The target range is 0.07 m in the x-z	
	section	64
4.11	The used area on a mirror projected onto the x-y plane where a target exists at the center for a 0.07 m depth	65
4 19	The used area on a mirror projected onto the x-y plane where the x coor-	0.0
7.12	dinate of a target is 0.015 m in the x-z section for a 0.07 m depth	67
4.13	The taper function for the reflection ratio on the mirror in numerical back	01
1.10	projection	68
4.14	Lateral resolution of a tapered and non-tapered proposed imager with a	00
	0.016 m width array in a 3-D problem. The x coordinate of a target is	
	0.015 m, and those of the measuring points are -0.04 to 0.04 m	69
4.15	Spatial resolution of a phased array imager with a 1-D array. The focal	
	length of the acoustic lenses is 0.07 m, and the targets exist at the center	
	for depths of (a) 0.02 m and (b) 0.07 m. This section is perpendicular to	
	the longitudinal axis of the linear array	72
4.16	Spatial resolution of the proposed imager in the x-z section. Targets exist	
	at the center for depths of (a) 0.02 m and (b) 0.07 m	73

	the (a) x-z and (b) y-z sections for a 0.07 m depth. (a) X coordinates of targets are $-0.03$ , $-0.015$ , $0$ , $0.015$ and $0.03$ m. (b) Y coordinates of targets are 0, 0.015 and 0.03 m	74 75 76
5.1 5.2	Schematic view of the acoustic vision substitute system	79
5.3	and stimulator groups are activated alternately	81 82
5.4	Schematic view of targets in the measurement area	82
5.5	Stimulating points matched with targets when the measuring range is $d_1$ .	83
5.6	Stimulating points matched with targets when the measurement range is $d_2$ .	83
5.7	Solenoid array placed on participants 'foreheads. The 2 × 4 solenoids placed at the center of the array are the stimulators. The two solenoids placed at the sides always generate sound and vibration to prevent participants from distinguishing tactile patterns by sound	84
5.8	An arrangement of stimulators divided into two groups when employing the alternating stimulation method	85
5.9	Schema of a solenoid component in the 2-D stimulator array placed on the forehead	86
5.10	Stimulus waveform in the simultaneous stimulation trials. Pulse repetition rate is 30 Hz and pulse width is half of the pulse onset interval. Each burst has 6 pulses and burst onset interval is 800 ms	87
5.11	Tactile patterns in the simultaneous stimulation trials. The 1-point stimulations are presented at one of the 8 positions. The 4-point stimulations are presented simultaneously at one of the three positions; left, middle, and	97
5.12	right Stimulus waveform in the alternating stimulation trials. Waveforms (1) and (2) are delivered to the active solenoids of groups 1 and 2, respectively.	87
5.13	Stimulus onset asynchrony between the two groups is 400ms	88
5.14	tions consist of two stimulation groups	88 89
	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	_

<ul><li>5.15</li><li>5.16</li></ul>	Solenoid numbers and activated solenoid groups of the 4-point stimulation. A 1-point stimulation is presented by activating one of the eight solenoids. A 4-point stimulation is presented at left, middle, or right position by four activated solenoids. Thus these stimulations are named 1-8, left, middle, and right.  The average of the possibilities that (1) the response is correct or (2) not correct when the response is a 4-point pattern for the interpretation of the perception of no signal, including the 2 standard deviation error bar. Colored bars are those of the simultaneous stimulation; white bars are of the proposed alternating stimulation.	90
6.1 6.2 6.3	Schematic view of the system in the receive phase	97 98
	from an element is reflected by the mirror, and then radiated to the measurement point $T_a$ after passing through the focus $T_r$	100
6.4	The Region with a guaranteed focus. When the focus is contained within the region, the transmit wave is radiated to the measurement point $T_a$	101
6.5	Radiation pattern of the proposed imager in the $x$ - $z$ section for (a) 0 m	101
6.6	and (b) 0.07 m depths	102
6.7	This corresponds to the radiation pattern shown in Fig. 6.5(b) Arrangement of the focuses and the regions with a guaranteed focus for a	103
0.7	-0.01 m depth	104
6.8	The synthesized aperture from 14 transmit and receive events when measuring the center for a 0.07 m depth	104
6.9	Lateral resolution of the proposed imager acquired from single and 16 transmit and receive events in the $x$ - $z$ section for a 0.07 m depth. The $x$ coor-	
6.10	dinates of point targets are $-0.015$ , 0 and 0.015 m	
	r	

## Chapter 1

### General introduction

### 1.1 Instruction

The number of visually handicapped is more than 300 thousands in Japan 2001, and the heavily visually impaired accounts for 17 %. The blindness is caused mainly by diabetes, glaucoma, cataract, retinitis pigmentosa, pathologic myopia. The changes of the cultural and social environments increase the occurrence of diabetes. Since cataract and retinitis pigmentosa are occurred by the aging, the occurrence of these diseases will increase in Japan, an aging society. Therefore in future the number of totally blind will increase, to improve the quality of life of the blind will become more important problem. Many researchers have investigated mobility aid systems for blind. In order to go a destination for a blind, it is necessary to detect and avoid obstacles. Particularly in the case of visiting a new place, for instance a travel, real-time detection and distinction of many obstacles is needed to decide next action; avoidance, wait, or search a bypass. Mobility aid means are classified in two groups. One is to depend on an attendance or a guide dog, that is, an aid of a human being or an animal with vision. The other is to use a mobility aid instrument. The travel with an attendance is the safest mean; however, it prevents the blind to live their own lives. The travel with a guide dog has many problems for training and keeping a dog. The mobility aid instruments are thus important for the blind. Mobility aid instruments are divided roughly into three types. The first is used for obstacle detection. The second is to transfer the environmental information. The last is a guidance system to guide the blind to the destination. We propose an acoustic vision substitute system to transfer the environmental information with high spatial resolution.

In advanced countries, the heart disease is one of the main cause of death. For example, it is the second cause in Japan. To improve a medical diagnosis of heart disease, 3-D volumetric high-resolution acoustic images are in high demand. We study volumetric 3-D acoustic imaging systems as promising candidates for the purpose. We propose a novel acoustic 3-D imaging system to realize real-time high-resolution imaging.

### 1.2 Obstacle detection devices

Obstacle detection devices need to detect an obstacle by a certain mean. Main means to detect an obstacle are as follows.

- 1) White cane.
- 2) Acoustic mobility aid devices.
- 3) Laser sensing devices.

#### 1.2.1 White cane

A white cane is the most famous instrument to detect obstacles. A white cane is consists of a grip, a shaft, and a tip, as shown in Fig. 1.1. The usage, contrived by R. Hoover, is spread in many countries [1]. The user grips a white cane at the center forward the body, and shake it right and left. The tip of the cane detects an obstacle at the location two paces forward. It is important that the step and the touch of the tip on the ground occur at once.

The usage of a white cane for a mobility aid device is called as touch technique [2]. In touch technique, it is necessary to note the following points. First, a white cane needs enough length to detect an obstacle at the location two step forward. Therefore the cane length is adjusted by considering the body size, the arm length, the pace, the walking speed, and the reaction time. Second, the user shakes a cane right and left to scan an arc by the tip of the cane. The arc width is a little wider than shoulders. Next, the user swings the cane rhythmically to occur the step and the touch of the tip on the ground at once. Light touch of the tip is desirable. Furthermore, the user interprets the tactile and auditory senses, caused by the swing of the cane, for the recognition of the environment.

The problems of the white cane as follows. First, a white cane passes a plane in a scan, and thus a swell in the plane is detected. However, the tip of a cane passes through an arc, and therefore a user detects a hollow only in the arc. Second, it scans the area lower than the chest, and thus it can not detect obstacles that exist higher than the chest. Next, it can detect only in the range of two steps. Longer obstacle detection is needed for the safe and comfortable walking. Besides, in the crowd it can not be used. Utilizing a white cane needs movement of a arm, and then a user becomes tired in the case of a long use. Lastly, long training time is needed to walk alone with it.

### 1.2.2 Acoustic mobility aid devices

High frequeicy sound above the audible range is generally called as ultrasound. Ultrasound wave is defined as a sound wave or elastic vibration with the frequency of more than

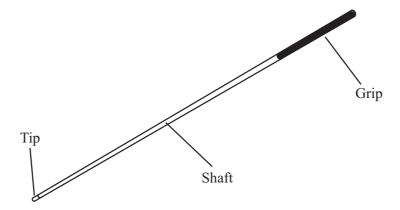


Figure 1.1: Schematic view of a white cane.

20 kHz. An ultrasound wave has directivity, and thus we can radiate an ultrasound wave to a measurement field. The echo from an obstacle in the measurement field is received, and then the obstacle is detected.

For the determination of target range two methods are practicable. One employs pulse waves, and the other swept-frequency ultrasound. Fig. 1.2 shows the schematic view of the propagation route of a transmit wave. A pulse wave radiated from a transmit element is scattered by a target, and then received on a receive element. This causes a time delay  $\Delta t$  between a transmit time and a receive time, as shown in Fig. 1.3. The target range is given by

$$r = c\Delta t/2,\tag{1.1}$$

where c is the sound velocity in the air.

Fig. 1.4 shows the frequencies of transmit and receive waves when a device radiates swept-frequency ultrasound, where the center frequency is  $f_0$ . In this method there is a certain frequency difference  $f_d$  between transmit wave and receive one during most of measurement time, as shown in Fig. Figint-uswept. The target range is obtained by

$$r = cf_{\rm d}T/(2\Delta f),\tag{1.2}$$

where T is the modulation repetition time,  $\Delta f$  is the maximum modulation frequency.

A simple method to determine the target direction is to measure one direction in a transmit and receive event. A user directs a device of this type to a measurement direction, and then checks the existence of an obstacle at the direction. The user scans the device in the entire measurement field.

Another strategy to determine the target direction utilizes plural receive elements. Fig. 1.5 shows the schematic view when a device has one transmitter and two receivers. In this case the target direction is given by

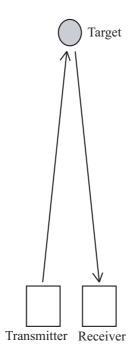


Figure 1.2: Schematic view of the wave propagation.

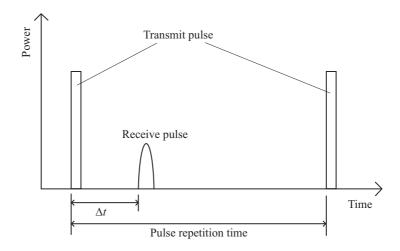


Figure 1.3: Transmit and receive time when pulse waves are radiated.

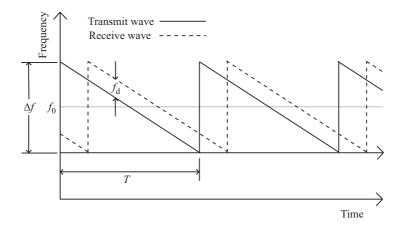


Figure 1.4: Frequency modulation of transmit and receive waves for target range detection.

$$\phi = \sin\left(\frac{r_{\rm R}^2 - r_{\rm L}^2}{2d\sqrt{r_{\rm R}^2 + r_{\rm L}^2 - 4d^2}}\right),\tag{1.3}$$

where  $r_{\rm R}$  and  $r_{\rm L}$  are the distances of the right and left receivers from the target, and d is the baseline interval of the transmitter and the receiver. When  $(r_{\rm R}-r_{\rm L})^2-4d^2\ll (r_{\rm R}+r_{\rm L})^2$ , the target direction is obtained by

$$\phi \simeq \operatorname{asin}\left(\frac{r_{\mathrm{R}} - r_{\mathrm{L}}}{2d}\right).$$
 (1.4)

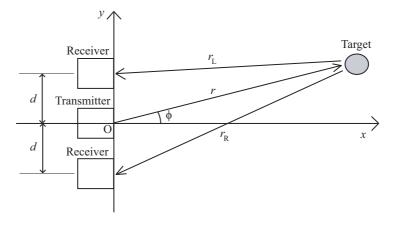


Figure 1.5: Schematic view of the detection of target direction with two receive elements.

A mobility aid device measuring one direction in a transmit and receive event is called a clear path indicator. Devices of this type are proposed to indicate the path without an

obstacle. N. Pressey [4] proposed the Mowat sensor, a hand-held device radiating acoustic pulses whose width is 15 degrees long and 30 degrees wide. It can detect within the range of 4 m. In the case of an obstacle exists in the beam radiation field, the Mowat sensor alarms a user and informs the obstacle range. L.Russel proposed the Pathsounder [5], a device to wear on the chest. It radiates an acoustic beam of 15 degrees width, and can detect within the range of 1.8 m. These devices requires manual scanning or chest movement to measure all the target field. This causes low time resolution.

L. Kay proposed another ultrasonic obstacle detector called Sonicguide [6]. The measurement field is 3 m width within the range of 5 m. A transmitter radiates frequency modulation ultrasound continuously to entire the measurement field. Since the range of an obstacle corresponds to the difference between the transmit and receive frequencies, it informs the frequency difference. Two receivers are put respectively at the right and left sides of the transmitter, and they present separetely to the right and left ears. There is a difference between two power of the signals presented at both ears, where it corresponds to the target direction. Therefore a user can suppose the target direction from the difference between the presented power at the both ears. For example the presented power at the right ear is larger than that at the left ear, the target direction is the right side. The problem of the Sonicguide is as follows; 1) Since it presents complex sound continuously, it is influenced seriously from the environmental noise. 2) In spite of a long training time being needed, a part of the users can be accustomed to using it.

S. Shoval *et al.* presented the Navbelt, a instrument for a travel aid [9]. It consists of a portable computer, ultrasonic sensors, and stereophonic headphones. The acoustic signals are transmitted as discrete beeps or continuous sound. These devices can detect the existence of an obstacle, however, the spatial resolution is insufficient to distinguish plural obstacles.

#### 1.2.3 Laser sensing devices

Laser sensing devices has been available commercially from more than thirty years ago. J. M. Benjuamine et al. [3] proposed the Laser Cane, using GaAs laser pulses. From the top of the cane three pulses are radiated to upward, forward, and downward. The measurement fields are respectively at the head-hight, forward within the range of 3.5 m, and at the foot of a user. This is a clear path indicator, that is, it informs only the existence of an obstacle in the path. The problem of the Laser Cane is as follows; 1) Since the weight is heavier than a white cane, the latest version of the Laser Cane, C-5, is 453 g, the user is fatigued to shake it. 2) The manipulation of the Laser Cane is complex. 3) It has low range resolution. 4) Scattered light, especially that of the solar light, causes the error detection of the device.

For high range resolution laser triangulation systems have been proposed. The schematic view of the system is shown in Fig. 1.6. The target range r is given by

$$r = \frac{B(f\sin\alpha - d\cos\alpha)}{f\cos\alpha + d\sin\alpha},\tag{1.5}$$

where B is the baseline between the laser and the center of the lens, f is the focal distance of the lens, d is the location of the laser spot,  $\alpha$  is the slope of the element array to the laser line.

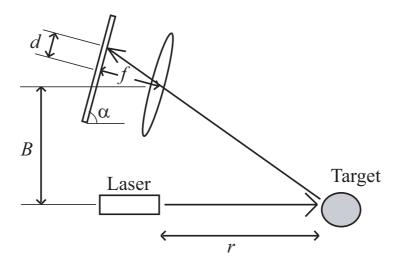


Figure 1.6: Schematic view of a laser triangulation system.

R. Farcy et al. proposed a device obstacles [7]. It consists of a triangulating laser telemeter, electric parts, and auditory feedback devices close to the ear. D. Yuan et al. investigated another hand-held mobility aid device using active triangulation [8]. The range information is presented to a user through haptic interface. Since a device of this type needs hand movement scnanning for measuring all the target field, the time resolution is low.

# 1.3 Vision substitute systems for environmental information

A study about a vision substitute system are directed to one of the two purposes; to inform visual information and to read a book. As a reading aid for blind, J. G. Linvil and J. C. Bliss are proposed the Optacon [10]. This instrument has a 6 times 24 stimulator matrix, and each stimulator 's intensity is controlled by the received power at each phototransistor of a camera. A user holds the camera at the right hand and scan it on a page of a book. The stimulator matrix is 2 cm wide and 5 cm long, and each stimulator presents 230 Hz vibrotactile stimulations. The user touches the matrix by a fingertip and recognizes

letters. In the case that 2.4 seconds is used to read a Japanese Katakana character, the possibility of correct response is 83 %. S. Saida et al. investigated a function of 3 display modes using a vibrotactile display against the abdomen [11]. Y. Yanagida proposed anoter reading aid instrument with 3 times 3 vibrating moters on the back of a chair [12]. In some cases, 87 % succession for letter reading.

To detect and distinguish obstacles, a vision substitute system to inform visual information is needed. G. Brindley and W. Lewin [13] produced a sensation of vision by electrical stimulation of the visual cortex. They implanted each of two 90 electrod matrixs at the right and left visual cortexs. They confirmed that the electrical stimulations at the visual cortex makes the perception of phosphenes to a subject. M. S. Humayan [14] implanted electrodes at the retinal layers and sitimulated electrically under local aneshesia. In a resolution test, a subject could resolube phosphenes at 1.75 degrees center-to-center distance. M. Mahadevappa et al. [15] investigated the percetptual thresholds and electrode impedance in the electrial stimulation at the retinal layers. These methods have the following problems; 1) Since these methods need to implant electrods to a user, they are invasive strongly. 2) The advance in these method is slow because the study needs an implantion to a human subject. L. Hesse et al. [16] evaluated the effectiveness of implantation of retinastimulation electrodes using cats. They investigated the responses in the visual cortex of a cat. Since the purpose of the vision substitute system is not to make some responses in visual cortex but to inform the vusual information, the study using aminals is easy to progress but is difficult to be put to practical use.

C. C. Collins [17], P. Bach-y-Rita [18], C. C. Collins and P. Bach-y-Rita [19] proposed a tactile vision substitute system, called TVSS. An image taken by a television-type camera is transformed to the vibrotactile or electrotactile stimulations at the skin of a user. Each stimulation intensity is correspond to the intensity at each pixel of the image. They confirmed that a user can distinguish vertical, horizontal, and diagonal lines. In addition a TVSS can inform the broad form and size of a object [20]. In spite of these capabilities a TVSS is not useful to inform the spatial information with plural objects. The problems of a TVSS is as follows; 1) The purpose of this system is to inform the enormous visual information totally. 2) Since the spatial resolution of a TVSS is much poorer than that of the eye, a user can not identify each object in the case of plurel objects exsisting in the sight. 3) A user cannot recognize the range of a object without the identification of the object.

Another strategy for the presentation of the visual information to a blind is employing auditory senseare. J. Coffey [21] and G. Smith et al. [22] made letter reading assistance systems for using auditory sensation. In these systems each letter is correspond to a soud of particular frequency, and the systems output multiple sounds. R. Fish [?] presented a vision substitute system using sound localization. Since auditory sense is important for a blind to know the environment, these systems employing auditory sense prevent from grasping the situation of the environment.

# 1.4 Information transfer method for sensory substitute system

A 2-D tactile stimulator array can present spatial information to the skin in the way similar to the visual information presented to the retina. However, it has insufficient spatial resolution and dynamic range compaired with the visual information. Because of the lack of transfer information presented with a tactile stimulator array, it is not useful when plural targets exist in the measurement field, that is, in the daily life. Therefore many resercheres have investigated the limitation of spatial information presented through tactile stimulation.

Sensory substitution systems employ vibrotactile or electrotactile displays, and then K. A. Kaczmarek et al. [24] and C. A. Perez et al. [25] compared between electrotactile and vibrotactile stimulations. The characteristics of the electrotactile stimulation are as follows; 1) Since the stimulator is an electrod, the structure of a stimulator array is simple. 2) While the constant current stimulation gives stable sensation to a user, regardless of the connection condition of an electrod to the skin, the user burns himself/herself at the stimulation point of bad connection to a electrod. 3) In the constant voltage stimulation a user is not injured even if the connection to an electrod is bad, however, the current is not constant and then the sensation is not stable. The characteristics of the vibrotactile stimulation are as follows; 1) Piezo-electric tarnsducers are miniature, consume low power, have low stimulation power and can set high stimulation frequency. Therefore they are mainly used for the fingertip stimulation. 2) While solenoids can not select high stimulation frequency, they can stimulate high power.

Vision substitution methods using tactile sensasion are reported from the early 1970's. A TVSS employed tactile stimulations, and the lack of the presented visual information and the power consumption became the problems of the TVSS. Therefore many researchers have investigated to improve the stimulus quality and reduce the power consumption. K. A. Kaczmarek et al. investigated the optimum pulse repetition rate, number of pulses per burst, burst frequency for maximizing the dynamic range of electrotactile stimulation [26][27]. C. J. Poletto et al. designed a high-voltage constant current stimulator for exact electrotactile stimulation at the fingertip [28]. Since constant current stimulation is often painful, they examined a method for elevating the pain threshold to electrotactile stimulation [29]. C. A. Perez et al. investigated the optimum vibrotactile waveform for maximizing tactile sensisivity and decreasing power consumption [25][30]. Futhermore they investigated the stimulation power required to reach tactile thretholds in electromechanical and piezo-electric tranceducers. Althoug several stimulation waveforms have been reported, the information presented by a tactile stimulator array is not sufficient for a vision substitute system to detect and distinguish obstacles.

### 1.5 Filtered back projection

To analize an object by x-ray scanning, the line integral data should be inverted to retreive the absorption coefficient distribution of the target field. J. Radon [31] solved this problem, and A. M. Cormack [32] gave a solution for x-ray scanning. The numerical reconstruction methods can be classified into two groups; Fourier reconstruction and the filtered back-projection methods. It was shown that the two methods are theoretically equivalent [33].

The Fourier reconstruction method is based on the projection-slice theorem [refnum1990]. The projection function onto the x axis is

$$p(x) = \int_{-\infty}^{\infty} f(x, y) dy, \tag{1.6}$$

where f(x,y) is the absorption coefficient. The set of projection functions for all directions is equivalent to the Radon transform. The Fourier transform of f(x,y) is

$$F(X,Y) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(x,y)e^{2\pi i(xX+yY)}dxdy.$$
 (1.7)

The slice in the X axis is the Fourier transform of p(x) as follows.

$$\int_{-\infty}^{\infty} p(x)e^{2\pi ixX}dx = \int_{-\infty}^{\infty} \left\{ \int_{-\infty}^{\infty} f(x,y)dy \right\} e^{2\pi ixX}dx$$
$$= \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(x,y)e^{2\pi ixX}dxdy = F(X,0). \tag{1.8}$$

Therefore f(x,y) is solved from S(X) using an inverse 2-D Fourier transform.

The Fourier reconstruction is sensitive to errors of the calculation in Fourier space. They influence the whole image, and the phase errors are the most serious effect. R. N. Bracewell et al. [ref???1961] found a way to avoid numerical Fourier transforms. After an equivarent correction is applied to all the projection functions, the absorption coefficient distribution is reconstructed from the modified functions using back-projection.

$$R^*[g](X) = \int_0^{2\pi} g(\theta, x \cos \theta + y \cos \theta) d\theta, \tag{1.9}$$

where  $R^*$  is called as back-projection. This is not an inverse to the Radon transform, and therefore star-like artifacts occure. In the noiseless case, a ramp filter is optimum to eliminate the artifacts.

$$f = \frac{1}{4\pi} R_* H[g]. \tag{1.10}$$

Check the reason why a ramp filter is optimum and a filtered back-projection is equivarent to the 2-D inverse Fourier transform.

### 1.6 Medical acoustic 2-D imaging system

Medical acoustic imagers, having high value for medical diagnoses, are low cost and non-hazardous to human body. They are thus widely used for medical diagnoses. Most of them radiate ultrasound pulses to human body. The pulses are scattered at the inhomogeneity of the medium, and then the echo is received at the transducers of the imagers. Therefore they measure one direction in a transmit and receive event.

There are two types of images constructed from measurement of one direction in the body. One is A mode image and the other is M mode one. An acoustic probe of an A-mode imager is fixed and measures one direction in the body. Longitudinal and lateral axes of the A-mode image show the amplitude of the echo and the range of the reflection point, respectively. An acoustic probe of a M-mode imager also measure one direction in the body. Longitudinal and lateral axes of the image show the range of the reflection point and the measurement time, respectively. The echo power is converted to the brightness in the M-mode image. A M-mode imager is used for the measurement of the fast moving organ, such as a heart.

B-mode imaging is proposed to measure one section of the body. An acoustic probe of a B-mode imager scans transmit and receive beams electronically or mechanically in a measurement plane in the body. The echo power is converted to the brightness, and a 2-D image is constructed from the data of all measurement directions. Several scan types of B-mode imagers are used for medical diagnoses. Fig. 1.7 shows the schematic view of the types. These imagers are useful, however, for the improvement of medical diagnoses a high-resolution acoustic 3-D imager is in high demand.

### 1.6.1 Mechanical scanning

A probe of this type measures one direction in a transmit and receive event, and the measurement direction is changed mechanically. Probes of two types are employed for mechanical scan imagers. One is a single element probe, and the other is annular array one. The structure of a single element probe is simple, and thus the probe is low cost. However, the focal distance is fixed because of employing an acoustic lens or the element shape. This causes a limitation of the measurement range.

An annular array probe is employed to measure wide range. The probe consists of plural elements, as shown in Fig. 1.8. An annular array probe can change focal distance using electronic focusing, and thus the measurement range becomes wider than that of a single element probe.

Three types of mechanical scanning are utilized for 2-D imaging. In linear scan a probe moves along a line, and measures in a rectangular field. In sector scan a plobe is swinged and a sector measurement field is acquired. A radial scan imager is used for an endoscope. Fig. 1.9 shows an endoscope with a radial scan imager. Ultrasound pulses radiated from a transducer are reflected at C on a mirror, and then transmitted to the

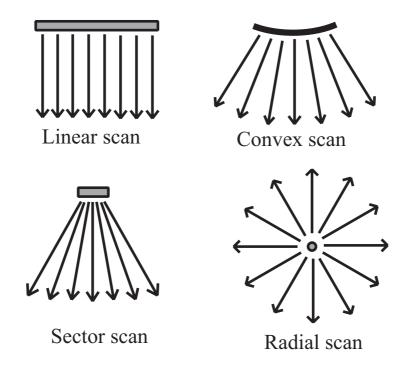


Figure 1.7: Schematic view of the scan types of B-mode imagers.

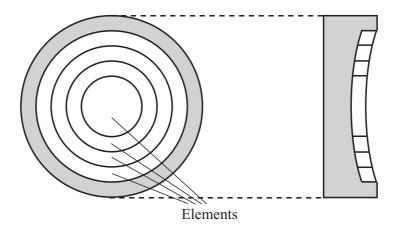


Figure 1.8: Schematic view of an annular array probe.

measurement field. Rotation of the mirror causes the beam scan of this imager.

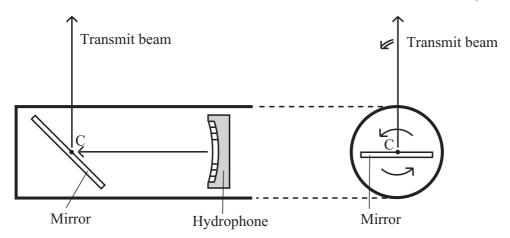


Figure 1.9: Schematic view of an endoscope with a radial scan imager. The left and right figure is the longitudinal and cross section of the endoscope.

### 1.6.2 Electronic scanning

Linear and sector electronic scans are the main scanning method in this category. A linear scan probe has dozens of elements placed in a row. The change of activated elements causes beam scan, as shown in Fig. 1.10.

The soperation basis of a convex scan imager is similarly equal to that of a linear scan imager. The difference of a convex from a linear one is that the elements are placed along a curved surface. A convex probe scans radially, and thus the measurement field is wider than that of a linear probe in the long range.

A sector electronic scan probe has narrow elements placed in a row. Beam formation is caused by radiation of ultrasound pulses from the elements with proper time delays, as shown in Fig. 1.11. The time delay  $T_{\rm D}$  employed by an element is given by

$$T_{\rm D} = \left\{ -\sqrt{(F \tan\theta + d_{\rm E})^2 + F^2} + F/\cos\theta \right\} / c,$$
 (1.11)

where F is the range of the focus,  $\theta$  is the angle of the focus from the center, c is the sound velocity, and  $d_{\rm E}$  is the distance between the element employing the time delay  $T_{\rm D}$  and that at the center of the array. When  $F \tan \theta \gg d$  the time delay  $T_{\rm D}$  is obtained from Eq. 1.11 by

$$T_{\rm D} \simeq d {\rm sin} \theta / c.$$
 (1.12)

In a certain condition about element interval a lobe appears except a main lobe in the measurement field. This lobe is called as a grating lobe, as shown in Fig. 1.12. When

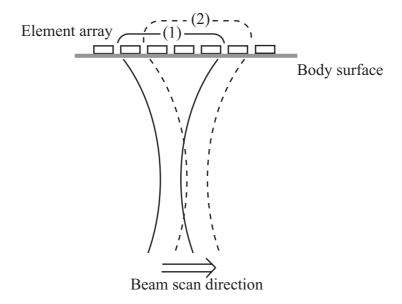


Figure 1.10: Beam scanning from the change of actibated elements. The change of activated elements from (1) to (2) causes the beam scan to the right direction.

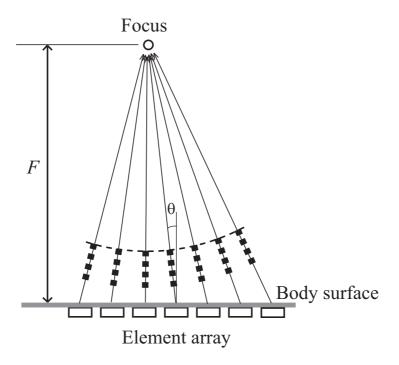


Figure 1.11: Schematic view of the beam formation employed by a sector scan probe.

grating lobes appear the received signal is influenced by the echo from the directions of the grating lobes, and thus a correct image is not acquired. Since it is necessary to prevent unwanted grating lobes, the element interval of a electronic sector scan probe  $I_{\rm E}$  satisfies the following equation.

$$I_{\rm E} < \frac{\lambda}{1 + \sin\theta_{\rm M}},\tag{1.13}$$

where  $\theta_{\rm M}$  is the maximum scan angle, and  $\lambda$  is the wavelength employed by the probe.

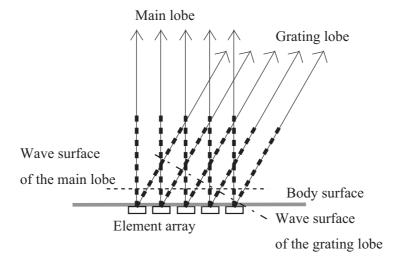


Figure 1.12: Grating lobe appeared in the measurement field. An unwanted lobe appears in a certain condition about element interval.

### 1.6.3 Dynamic beam focusing

The spatial resolution of an imager utilizing beam focus deteriorates in front and behind the focus. To improve the spatial resolution an imager with an element array probe utilizes the following methods. In the multi-stage electronic focusing method, transmit beams with various focal length are radiated for each measurement direction. Only the information around the focus is employed, and then an image in one measurement direction is constructed from multiple transmit and receive events. The problem of this method is low time resolution.

In the dynamic focusing method, single transmit beam is radiated for one measurement direction. In the receive phase, the element array employs various sets of time delays to acquire a narrow receive beam at each measurement range. Dynamic focusing is a kind of signal processing to the receive signal, and thus an image in one measurement direction is constructed in a transmit and receive event. Therefore the time resolution of an imager with dynamic focusing does not deteriorate.

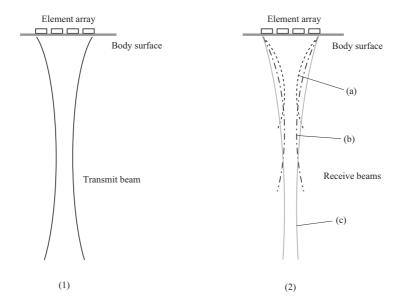


Figure 1.13: Schematic view of the dynamic beam focusing. (1) Single transmit beam is radiated for one measurement direction. (2) In the receive phase, the element array employs various sets of time delays to acquire a narrow receive beam at each measurement range. The recieve beams (a), (b), and (c) are formed for short, middle, and long range measurement, respectively.

### 1.7 Medical acoustic 3-D imaging system

For the improvement of medical diagnoses volumetric 3-D high-resolution acoustic images are in high demand. A 3-D acoustic imager employs one of the following methods accordingly to the purpose.

- 1) Mechanical scan of a single element probe
- 2) Manual or auto scan of a 1-D array
- 3) Mechanical scan of a 1-D array
- 4) Electronic scan of a 2-D array

Mechanical scan of a single element probe can utilize high transmit frequency, and thus there is the possibility to be useful for short range measurement. Manual or auto scan of a 1-D array is employed to acquire large measurement field in a static organ, such as the breast of a woman. An acoustic imager with mechanical scan of a 1-D array has

large measurement field and high spatial resolution with adequate time resolution. The electronic scan technique with a 2-D array is improved rapidly. This method is directed to high time and spatial resolution.

### 1.7.1 Mechanical scan of a single element probe

A single element probe with a fixed focus, caused by an acoustic lens or the element shape, measures one direction in a transmit and receive event. Thus a 3-D image is acquired from a 2-D scan of a single element probe. The problem of this method is the low lateral resolution in front and behind the focus.

Since 1960's numerical image reconstruction using synthetic aperture technique has been proposed [35][36]. Numerical image reconstruction utilizing mechanical scan of a single element is the simplest one [37][38]. A monostatic data acquisition scheme can reconstruct images with adequate spatial resolution; however, an imager using this method has insufficient time resolution for practical clinical applications.

### 1.7.2 Manual or auto scan of a 1-D array with position tracking

Since a 1-D element array measures in the plane parallel to the longitudinal axis of the array, a 3-D image is acquired from a 1-D scan perpendicular to the longitudinal axis of the array. A 3-D imager of this type utilizes freehand or mechanical scan. A position sensor is attached to the acoustic probe to track the position of the probe, and thus the position of the measurement plane in the body is located. A 1-D scan of this type causes low time resolution of a 3-D imager. Therefore this scan type is employed for the measurement of a static organ.

### 1.7.3 Mechanical scan of a 1-D array

Similaly to the auto scan, swing or rotation of a 1-D element array probe can acquires a 3-D image, as shown in Fig 1.14. A conventional 1-D element array probe measures one direction in a transmit and receive event. It is necessary for a 3-D imager to measure much more directions than that for a 2-D imager. Thus a 3-D imager with an 1-D array probe has much lower time resolution than that of a 2-D imager. When a 3-D imager measures in the field of  $60^{\circ} \times 60^{\circ} \times 10^{\circ}$  cm the time resolution of the imager becomes 2.2 volumes/s, where we assume the beam spacing is 1 degree and the sound velocity is 1550 m/s. For improvement of time resolution of a 3-D imager multi-line imaging ?? and digital beamforming methods have been studied. Synthetic aperture technique has been introduced for higher spatial resolution. To improve signal-to-noise ratio defocusing method was proposed.

Fig. 1.15 shows the schematic view of the multi-line imaging [39]-[41]. In this method transmit beam is sufficiently wide to include multiple narrow receive beams. Multiple

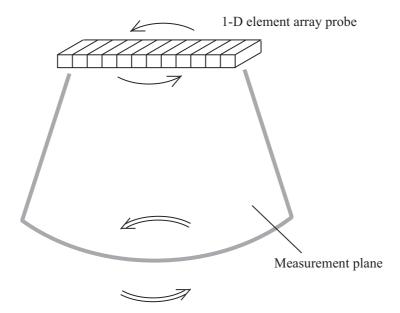


Figure 1.14: Schematic view of the mechanical scan of a 1-D array.

receive beams are formed in paralell using multiple sets of receiver delay lines. Therefore in this method multiple image scan lines are acquired in a transmit and receive event.

A synthetic aperture imager with a 1-D element array [42][43] transmits a wide beam of single element response to the entire measurement plane, as shown in Fig. 1.16. All elements on the array receive the echo, and then all the image lines in the measurement plane is formed in parallel. In the next transmit event, a transmit beam is radiated from the next transmit point. After all the transmit points radiate once, the final image is constructed from the sum of all the received signal beamformed at the measurement point. In this method the effective aperture of the imager is synthesized from multiple transmit and receive event, as shown in Fig. 1.17. The coherent integration utilizing the synthetic aperture technique realizes a spatial resolution equivalent to that of an aperture given by the convolution of the transmit points and the receive aperture, and thus a synthetic aperture imager with multiple transmit and receive event has high spatial resolution. The time resolution of a synthetic aperture imager is not determined by the number of image lines, but by that of transmit points. Therefore an imager of this type trades off spatial resolution with time resolution.

The acoustic power radiated from a single element limits the signal-to-noise ration (SNR) of a synthetic aperture imager. To improve SNR of an imager multiple elements radiate ultrasound pulses with apodization or a set of time delays, as shown in Fig. 1.18 [42]. When multiple elements radiate ultrasound pulses simultaneously with apodization, a wide transmit beam is formed; however, the acoustic power capacity of each element is not fully used. When multiple elements radiate defocused ultrasound pulses with a set of

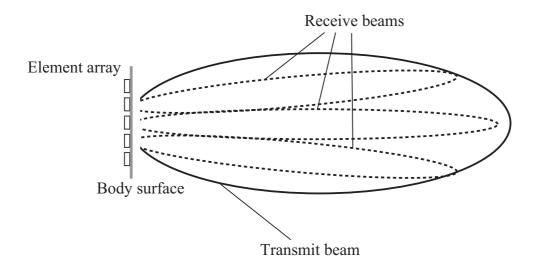


Figure 1.15: Schematic view of multi-line imaging.

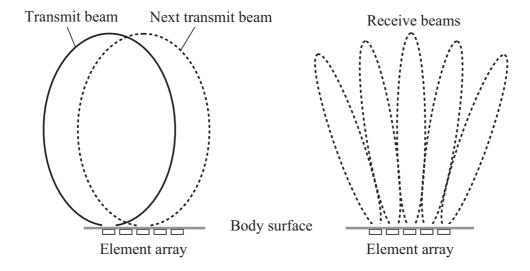


Figure 1.16: Transmit and receive schemes of a synthetic aperture imager. A wide transmits beam is radiated to the entire measurement plane. Then all the image lines in the measurement plane is formed in parallel. In the next transmit event, a transmit beam is radiated from the next transmit point.

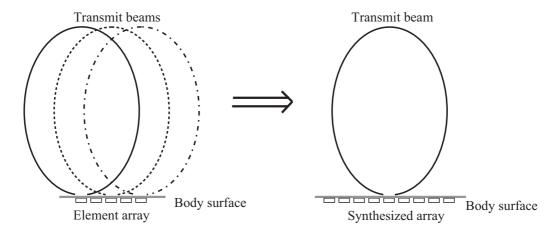


Figure 1.17: The effective aperture of the imager synthesized from multiple transmit and receive event. The coherent integration utilizing the synthetic aperture technique realizes a spatial resolution equivalent to that of an aperture given by the convolution of the transmit points and the receive aperture.

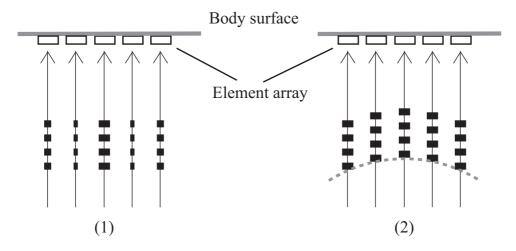


Figure 1.18: Transmit schemes using multiple elements to synthesize a single element response. Multiple elements are excited (1) simultaneously with apodization, and (2) with a set of time delays to form defocused ultrsound pulses.

time delays, the acoustic power capacity of each element is fully utilized in addition to synthesize a single element response.

### 1.7.4 Electronic scan of a 2-D array

Volumetric 3-D high-resolution acoustic images are in high demand for medical diagnoses. A conventional phased array imager excites all array elements to form a transmit beam, and uses all of them for receive beamforming [44]. Although only the receive beam is dynamically focused, imaging under this condition results in a high electronic signal-to-noise ratio (SNR) as well as good spatial and contrast resolution. This configuration has two main problems; one is that the number of elements becomes enormous for a 2-D array of a 3-D phased array imager, and the other is low time resolution caused by the enormous number of image lines in the 3-D measurement field.

A strategy to decrease the number of elements, at the cost of the loss of some lateral resolution and SNR, is to utilize a 2-D sparse array, with an element spacing of more than one-half of a wavelength. D. H. Turnbull *et al*. [45] investigated the arrangement of the sparse randam 2-D array. Since the 2-D randam array has no periodicity, grating lobe is avoided. T. S. Sumanaweera *et al*. investigated 2-D spiral arrays [46].

S. W. Smith *et al.* [47] proposed an idea of using different transmit and receive geometries, as shown in Fig. 1.19. Since a transmit beam and a receive beam have different radiation patterns, the directions of grating lobes are different by each other. Therefore grating lobes are suppressed. This idea was developed by Lockwood *et al.* [48][49].A. Austeng et al. [50] investigated and made a comparative study about the sparse arrays. Although several designs of sparse array have been reported, it is difficult to reduce the number of elements to less than half of the dense array. Furthermore, a 3-D imager of this type has low time resolution.

A strategy to improve time resolution is multi-line imaging technique applied for a acoustic imager with 2-D array [51]. In this method multiple image lines are acquired in a single transmit and receive event at the cost of some loss of lateral resolution, similar to a multi-line imager with a 1-D array.

Digital beamforming technique [52] is mainly used for radar systems. Since the echo received on an element array is digitized, an imager utilizing this technique has high flexibility as follows; formation of multiple beams in parallel to improve time resolution significantly, and employment of proper aperture apodization to suppress sidelobe level. However, enormous number of elements are needed to acquire a 3-D image with sufficient spatial resolution.

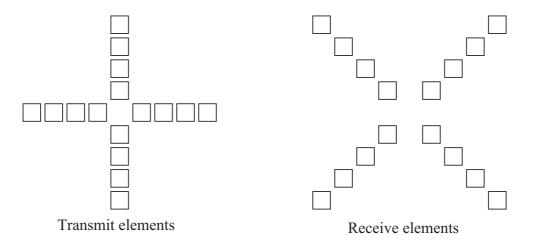


Figure 1.19: A 2-D element array design using different transmit and receive goemetries. Since a transmit beam and a receive beam have different radiation patterns, the directions of grating lobes are different by each other. Therefore grating lobes are suppressed.

## Chapter 2

# A Hybrid Method and Sensor for a High-resolution Ultrasound Vision Substitute System for the Visually Impaired

### 2.1 Introduction

A white cane is widely used as a vision assistance device for the blind; however, such a device has difficulty detecting an obstacle at chest height. Other instruments, such as a hand held laser telemeter and an eyeglass configured sonar-type device, only inform of the existence of an obstacle. Since they have insufficient spatial resolution, they are not useful as navigation systems under conditions with plural targets such as are encountered in daily life.

A vision substitute system for blind needs two capabilities. One is high time resolution for real-time operation. The other is high spatial resolution to individually recognize and to identify plural target positions. This study is directed to propose a vision substitute system for use in daily life. Thus the system needs to recognize objects on a table and to find the direction where a wall breaks off, that is, where an exit is. Acoustic sonar systems are useful for this purpose; indeed, many studies have focused on acoustic through-air sensors [53]-[55]. However, so far there has been insufficient spatial and time resolutions for a proposed vision substitute system to be of practical use.

In the field of the electromagnetic waves, phased array and digital beamforming methods are often used to acquire high spatial resolution images. A phased array imager measures one direction in a transmit and receive event and so it is difficult to scan a 3-D target field in a short time. Utilizing parallel scanning with plural sensors improves time resolution of a phased array imager [56][57]; however, it has still insufficient time resolution because of the velocity of sound in air.

A digital beamforming imager measures the entire target field in a transmit and receive event and therefore has high time resolution. However, the number of elements on the array becomes enormous to achieve sufficient spatial resolution. Another strategy to improve time resolution and decrease the number of elements, at the cost of the loss of some lateral resolution and signal-to-noise ratio, is a digital beam forming imager with a 2-D sparse array with element spacing of more than one-half of a wavelength [58]-[61]. This method uses a wide transmit beam and multiple receive beams formed simultaneously. Although several designs for arrays have been reported, it is difficult to reduce the number of elements to less than half of a dense array.

In this paper we propose a system based on a hybrid array-reflector configuration. In this system a wide transmit beam is radiated to the entire measurement field. The echo from a target is gathered by a reflector and received on a 2-D element array. Since the proposed imager measures the entire target field in a single transmit and receive event, it is suitable for real-time operation. In addition, most of the echo arrived at the reflector mirror is received on the array and thus the spatial resolution and signal-to-noise ratio is improved from a digital beamforming imager with a same size 2-D array.

In section 2, we outline the framework on the proposed hybrid imager. Section 3 provides some necessary wave equations and parameters to evaluate the spatial resolution of the proposed imager. In section 4, we propose the off-focus method. In this method, a reflector and a 2-D array are fixed. Images are reconstructed from the received signal on the array by numerical back projection. Section 4 optimizes the reflector shape. Section 6 evaluates the spatial resolution of the proposed imager using physical optics. We propose a method for real-time signal processing in section 7. Finally, we draw conclusions in section 8.

# 2.2 Principle of the hybrid 3-D imaging system with a 2-D array and a reflector

Fig. 2.1 shows a schematic view of the proposed vision substitute system. It consists of a transmitter, a concave reflector, a 2-D element array, and a stimulating device. The transmitter radiates ultrasound pulses to the entire measurement field. Elements on the array are spaced at intervals of one-half of the wavelength. Images are reconstructed from the received signal on the array. Since the human forehead has a low two-point discrimination threshold and a wide stimulating area, we propose that the stimulating device is placed on the forehead. The proposed vision substitute system stimulates this location on the forehead. The target direction corresponds to the location of the stimulating point on the forehead. In this way a user can recognize the target direction.

The proposed imager measures the entire measurement field in a transmit and receive event. Thus the time resolution of the proposed imager is improved significantly from that of a phased array imager. Since most of the echo reflected by the mirror is gathered

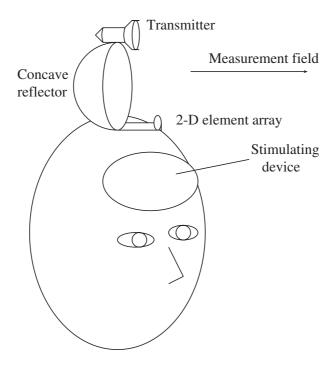


Figure 2.1: Schematic view of the proposed vision substitute system.

and received on the array, the proposed imager has higher spatial resolution than a digital beamforming imager with a same size array. Therefore, the number of elements can be reduced to about 1/8 of a dense 2-D array having the same spatial and time resolution but using a digital beamforming method, as is shown later.

## 2.3 Acoustic propagation calculations

In this section we explain the wave equations to evaluate the angular resolution of the proposed imager. Fig. 2.2 is the coordinates system used in this calculation. The z axis is directed to the measurement field. Generality is not lost when the proposed imager is symmetrical in the x-z plane. We set the center and a normal vector of a 2-D array as  $(x_s, 0, z_s)$  and  $(-\sin\theta_s, 0, \cos\theta_s)$ , respectively. Where  $\theta_s$  is the angle between the normal vector of the array and the z axis, as shown in Fig. 2.2. We assume the reflection ratio of the mirror as 1.

When a target exists at  $T_1(x, y)$ , the particle velocity of the transmit wave at  $T_1$  is given by

$$v_{\mathrm{T}_{1}0} = \sqrt{\frac{W}{2\pi k\rho\omega}}G_{\mathrm{r}}R_{\mathrm{r}}(x,y,z)\frac{1+jkr}{r^{2}}$$

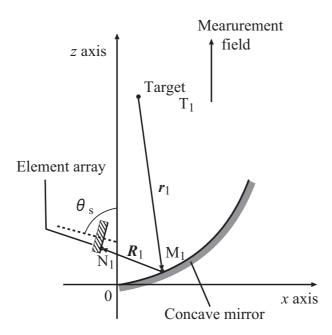


Figure 2.2: Arrangement of the sensor array and mirror.

$$\cdot e^{-(\alpha+jk)r},\tag{2.1}$$

where  $\alpha$  is the attenuation coefficient of the air, W is the radiation power from a transmitter,  $G_{\rm r}$  is the gain of the transmitter, r is the vector from the transmitter to  $T_1$ , r = |r|, k is the wave number,  $\omega$  is the angular frequency,  $\rho$  is the density of the medium,  $R_{\rm r}(x,y,z)$  is the directivity function of the transmit element satisfying the condition  $0 \le R_{\rm r}(x,y,z) \le 1$ . We assume the transmitter as a point source. Eq. 2.1 is correct under the condition that  $l_t^2 \ll r^2$  when an imager employs a circular transmit element of  $2l_t$  in diameter.

The echo scattered at  $T_1$  is reflected on the mirror at  $M_1$ , and received by an element at  $N_1$ . The volume velocity of a small area around  $T_1$  is given by  $v_{T_10}\Delta S'\frac{\boldsymbol{n}_0\cdot\boldsymbol{r}}{n_0r}$ , where  $\Delta S'$  is the square measure of the small area around  $T_1$ ,  $\boldsymbol{n}_0$  is the normal vector of the target surface at  $T_1$ ,  $n_0 = |\boldsymbol{n}_0|$ . Then the velocity potential and pressure variation at  $M_1$  are given, respectively, by

$$\phi_{M_1} = A(x,y) \frac{v_{T_{10}}}{2\pi r_1} \frac{\mathbf{n}_0 \cdot \mathbf{r}}{n_0 r} e^{-\alpha r_1 - jkr_1} \Delta S', \qquad (2.2)$$

$$v_{\rm M_1} = \frac{1 + jkr_1}{r_1} \phi_{\rm M_1}, \tag{2.3}$$

where the reflection ratio of the amplitude at the target surface is A(x, y),  $\mathbf{r}_1 = \overrightarrow{\mathbf{T}_1 \mathbf{M}_1}$ ,  $r_1 = |\mathbf{r}_1|$ . The volume velocity of the small area around  $\mathbf{M}_1$  is given by  $v_{\mathbf{M}_1} \Delta S(\frac{\mathbf{n}_1 \cdot \mathbf{r}_1}{n_1 r_1})$ , where

 $\Delta S$  is the square measure of the small area around  $M_1$ ,  $\mathbf{n}_1$  is the normal vector of the mirror at  $M_1$ ,  $n_1 = \mathbf{n}_1$ . We assume a spherical wave is radiated from  $M_1$  and thus the velocity potential at  $N_1$  is given by

$$\phi_{1} = \int_{S'} \int_{S} \frac{v_{M_{1}}}{2\pi R_{1}} (\frac{\mathbf{n}_{1} \cdot \mathbf{r}_{1}}{n_{1} r_{1}}) e^{-\alpha R_{1} - jkR_{1}} dS dS'$$

$$= \int_{S'} \int_{S} \frac{jkA(x, y) v_{T_{1}0} (1 + jkr_{1})}{4\pi^{2} r_{1}^{2} R_{1}} (\frac{\mathbf{n}_{0} \cdot \mathbf{r}}{n_{0} r})$$

$$\cdot (\frac{\mathbf{n}_{1} \cdot \mathbf{r}_{1}}{n_{1} r_{1}}) e^{-(jk+\alpha)(r_{1}+R_{1})} dS dS', \qquad (2.4)$$

where  $\mathbf{R}_1 = \overrightarrow{\mathbf{M}_1 \mathbf{N}_1}, R_1 = |\mathbf{R}_1|.$ 

The particle velocity along the x and y axes are obtained by  $v_{1x} = -\frac{\partial \phi_1}{\partial x}$  and  $v_{1z} = -\frac{\partial \phi_1}{\partial z}$ , respectively, and thus the particle velocity perpendicular to the element array is given by

$$v_1 = -v_{1x}\sin\theta_s + v_{1z}\cos\theta_s. \tag{2.5}$$

Since the pressure variety is given by  $p_1 = \rho \frac{\partial \phi_1}{\partial t} = j\rho \omega \phi_1$ , the echo power at N<sub>1</sub> is given by  $I_1 \simeq I_{1m} = \frac{1}{2}p_1v_1^*$ , when the phase of  $p_1$  is the same as that of  $v_1$ .

 $p_1$  and  $v_1$  have almost the same phase under the condition that  $kR_1 \gg 1$ . When  $R_1 > 3$  cm and the sound velocity c = 340 m/s, the condition is satisfied when the transmit frequency  $f \gg 1.8$  kHz. Therefore, the condition is satisfied when ultrasound is transmitted. In this study f = 170 kHz, and so  $I_1 = 0.99994$   $I_{1m}$ . We thus assume  $I_1 = I_{1m}$ . Since the receive power is given by

$$W_{\rm R} = I_1 D, \tag{2.6}$$

where D is the square measure of the effective aperture of a receive element. The ratio of the receive power to the transmit one is then given by

$$W_{\rm R}/W = I_1 D/W. \tag{2.7}$$

In this paper we introduce the assumption that the transmit and receive elements have no directivity.

## 2.4 Off-focus method for image reconstruction

To detect target locations from the images received on the array it is necessary to adjust the distance between an element array and the reflector mirror for the purpose to focus on the array, as shown in Fig. 2.3. We call this the auto-focus method. This method needs a device to mechanically adjust the distance, and thus an imaging system based on an auto-focus method becomes complex.

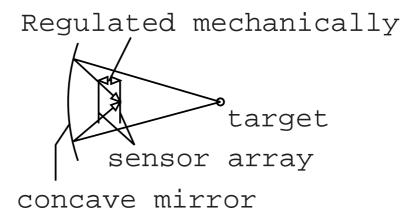


Figure 2.3: Schematic view of the auto-focus method.

We propose a method in which images are reconstructed from the distributed images received on the element array by numerical back projection. We call this the off-focus method, as shown in Fig. 2.4. For image reconstruction by numerical back projection, it is necessary to draw the estimated power in the measurement field. Image reconstruction based on numerical back projection is processed as follows. The phase of the received signal is reversed before being projected backward from the receive element U at  $N_2$ . The waves projected backward are reflected by the mirror at  $M_2$  and then focused at the target locations.

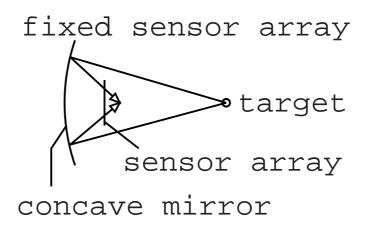


Figure 2.4: Schematic view of the off-focus method.

The estimated velocity potential at  $T_2$ , caused by the element U, is obtained by

$$\phi_{2U} = \frac{A_U^*}{2\pi} \int_S \frac{1 + jkR_2}{R_2^2 r_2} \frac{\mathbf{n_2} \cdot \mathbf{R_2}}{n_2 R_2} \frac{\mathbf{n_2} \cdot \mathbf{R_2}}{n_2 R_2} \cdot e^{-(jk+\alpha)(r_2+R_2)} dS, \qquad (2.8)$$

where the amplitude received by the element U is  $A_U$ ,  $\mathbf{R}_2 = \overrightarrow{\mathrm{N}_2\mathrm{M}_2}$ ,  $\mathbf{r}_2 = \overrightarrow{\mathrm{M}_2\mathrm{T}_2}$ ,  $\mathbf{n}_2$  is the normal vector of the mirror at  $\mathrm{M}_2$ ,  $R_2 = |\mathbf{R}_2|$ ,  $r_2 = |\mathbf{r}_2|$ ,  $n_2 = |\mathbf{r}_2|$ . The estimated velocity potential at  $T_2$  is given by

$$\phi_2 = \sum_U \phi_{2U}.\tag{2.9}$$

In the off-focus method images are reconstructed from the signal received on the array by numerical back projection; therefore, it is not necessary to focus on the array. To evaluate the correctness of the off-focus method we compare the spatial resolution of different array positions. In this section, for the simplicity of calculation, we employ a rotationally symmetric parabolic mirror and assume that the blocking due to the array over the mirror can be neglected.

The parameters used in this evaluation are; a square array 4 cm in width is set on a plane parallel to the x-y plane for a depth of  $z = z_s$ , the center of the array is on the z axis, the shape function of the mirror, 10 cm in width, is  $z = (x^2 + y^2)/12$ . The square measure of the effective aperture of an element is 0.01 cm<sup>2</sup>, the transmit frequency f = 170 kHz, attenuation coefficient  $\alpha = 3 \times 10^{-8} f$  neper/cm. In this paper we assume that the echo scattered backward from a target is a spherical wave. We investigate the image of a point target to evaluate the spatial resolution of a proposed imager.

The received power on the array when  $z_{\rm s}=3.1$  and 2.5 cm are shown in Fig. 2.5 and 2.6, respectively, where the focal length of the reflector mirror is 3.1 cm. A point target is located at the center for a 100 cm depth.

The spatial resolution of the proposed imager is shown in Fig. 2.7. The responses in the two cases correspond with each other in the field of high estimated power; that is, the shapes of the main lobe, and the first and second sidelobes are the same in the both cases. This indicates that the distance between the element array and the mirror has just a trifling effect on the spatial resolution. Since adjustment of the element array is not necessary with the off-focus method, we employ the proposed off-focus method for both its simplicity of the structure for the imaging system and the decrease in weight it brings.

## 2.5 Optimization of the mirror shape

In section 4, we employ a rotationally symmetric parabolic mirror. It is not necessary for an imager based on the off-focus method to focus on the array and thus there is a probability that a reflector mirror with no focus is optimal for the off-focus imager. For a wide measurement field it is desired that the imager has high spatial resolution

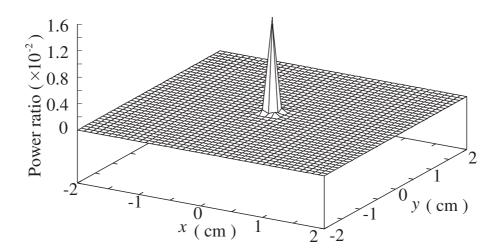


Figure 2.5: Received power distribution map on an element array. The distance between the array and the bottom of the mirror is 3.1 cm. A point target exists at the center for a 100 cm depth.

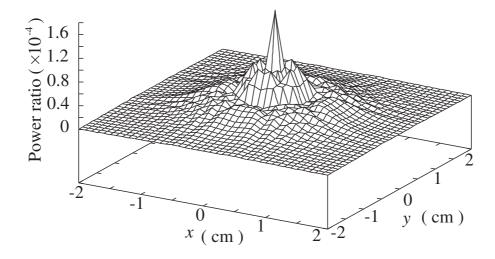


Figure 2.6: Received power distribution map on an element array. The distance between the array and the bottom of the mirror is 2.5 cm. A point target exists at the center for a 100 cm depth.

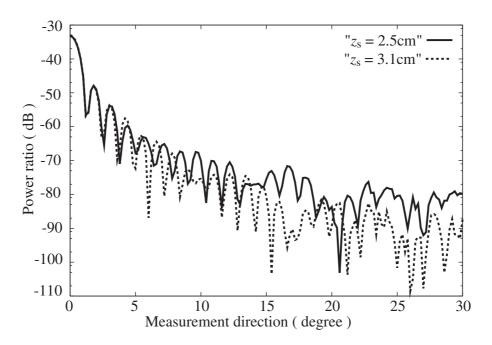


Figure 2.7: Estimated power of an imager based on the off-focus method. A point target exists at the center for a 100 cm depth.

and sensitivity in the peripheral direction, as well as in the center. In this section we investigate the optimum shape of the reflector mirror for an imager based on the off-focus method.

# 2.5.1 Coordinate system used in the optimization of the mirror shape

We arrange a 2-D element array and a reflector mirror offset to prevent the array from blocking the echoes arriving at the mirror, as shown in Fig 2.8. The center of the measurement field is in the x-z plane and the angle between the center and the z axis is 15 degrees, where the center is in the field of x > 0. We determine the parameters for the optimization of the mirror shape as follows; the visual angle of the measurement field is 30 degrees vertically and 60 degrees horizontally, the imager employs an elliptical array 3 cm long and 4 cm wide, and the reflector mirror is 20 cm in width for both x and y axis directions. The imager is symmetrical in the x-z plane, and the center of the array exists at  $S_c$ . The section of the mirror in the x-z plane is OQ. P is on the curved line OQ, where  $\angle OS_cP = \angle PS_cQ$ . The x' axis is the tangent of the curved line OQ at P in the x-z plane. The y' axis is parallel to the y axis, and P is on the y' axis.  $\overrightarrow{O'P}$  is the normal vector of the mirror at P, and  $\overrightarrow{PC}$  corresponds to the center of the measurement field. The z' axis

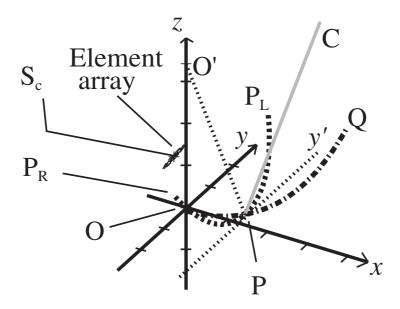


Figure 2.8: Coordinate system used for optimization of the mirror shape.

corresponds to the line PO'.

We optimize the mirror shape using geometric optics [64] for effectively gathering the echo to the array. First, we optimize the curvature of the curved line OQ, and then optimize that of  $P_LP_R$ , where the curved line  $P_LP_R$  is the section of the mirror in the O'P-y' plane. Finally we determine the shape of the reflector mirror by interpolating between the two curved lines.

## 2.5.2 Optimization of the mirror shape in the vertical section

In this study we assume that the reflector mirror is symmetrical in the x-z plane, and we set the center of the element array  $S_c$  at  $(-1.5 \text{ cm}, 0, z_s)$ . We then determine the mirror shape and the slope of the array as follows. We define  $I_{1\nu}$  and  $I_{DBF1\nu}$  as the summation received on the array with and without, respectively, a reflector for gathering the echo on the array, where  $\nu$  is the angle between the line PC and the target direction in the x-z plane. The ratio of  $I_{1\nu}$  to  $I_{DBF1\nu}$  shows the efficiency of the proposed method in a target direction in a vertical plane. We then maximize the evaluation function

$$V_{\text{ver}} = \prod_{\nu=-15}^{15} E_{1\nu}^{1+2*(15-|\nu|)/15},$$
 (2.10)

$$E_{1\nu} = I_{1\nu}/I_{\text{DBF}1\nu}.$$
 (2.11)

We employ a geometric exponential function for the evaluation for two reasons. First, the function gives a low evaluation value when the proposed imager has one and more directions of low efficiency. Second, the center of the measurement field requires high efficiency for high spatial resolution, as with the visual information. The optimized shapes of the mirror are the same when the values of the weight over the efficiency at the center are in the range of the square and the fifth power. Thus we set the weight as the cube.

We assume the shape function of the mirror in the x-z section as a quartic function in the xyz coordinate system. We optimize the shape function of the mirror,  $\theta_s$  and  $z_s$ , where  $\theta_s$  is the angle between the x axis and the array, and  $z_s$  is the height of the array center at at  $S_c$  from the bottom of the mirror at O. Fig. 2.9 shows the efficiency of the proposed imager with the optimized mirror in each measurement direction in the x-z plane when  $4 \le z_s \le 9$ .

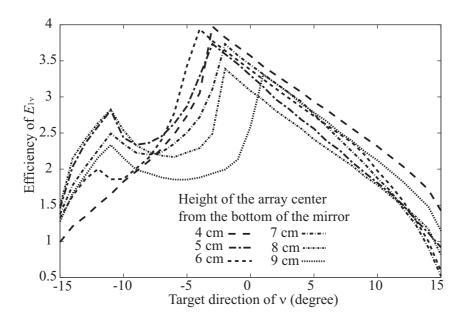


Figure 2.9: Angular characteristics of the efficiency of the proposed imager in a vertical section.

## 2.5.3 Optimization of the mirror shape in a horizontal section

In this study we assumed that the imager was symmetric in the x-z plane and thus the horizontal section of the array would be parallel to the y axis. Since the horizontal section of the mirror is also symmetrical in the x-z plane, we set the shape function of the section of the mirror as a polynominal function of degree 8 in the x'y'z' coordinate system. We also define  $I_{2\nu}$  and  $I_{\text{DBF}2\nu}$  as the summation received on the array with and without,

respectively, a reflector for gathering the echo on the array, where  $\nu$  is the angle between the line PC and the target direction in the CP-y' plane. The ratio of  $I_{2\nu}$  to  $I_{\text{DBF}2\nu}$  shows the efficiency of the proposed method in a target direction in a horizontal plane. We then maximize an evaluation function

$$V_{\text{hor}} = \prod_{\nu=0}^{30} E_{2\nu}^{1+2*(30-\nu)/30}, \qquad (2.12)$$

$$E_{2\nu} = I_{2\nu}/I_{\text{DBF}2\nu}. \qquad (2.13)$$

$$E_{2\nu} = I_{2\nu}/I_{\text{DBF}2\nu}.$$
 (2.13)

Fig. 2.10 shows the efficiency of the proposed imager with the optimized mirror in each measurement direction in the CP-y' plane when  $4 \le z_s \le 9$ .

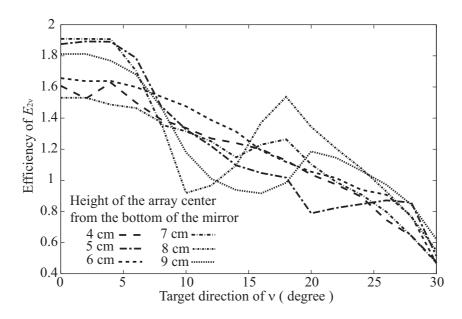


Figure 2.10: Angular characteristics of the efficiency of the proposed imager in a horizontal section.

#### 2.5.4Optimization of the 3-D reflector mirror

We determine the optimum of  $\theta_s$  and the shape functions in the vertical and horizontal plane from the product of two evaluation functions,  $V_{\text{ver}}$  and  $V_{\text{hor}}$ . We then interpolate to construct a 3-D reflector mirror from the shape functions, as shown in Fig. 2.11. Fig. 2.12 shows the angular characteristics of the efficiency of the proposed imager with the interpolated mirror.

For the optimization of a 3-D mirror shape it is necessary to ascertain the optimization of  $z_{\rm s},~\theta_{\rm s}$  and the shape functions of the mirror with a 3-D problem. Therefore, we set

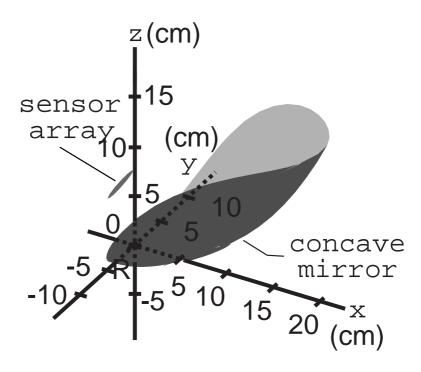


Figure 2.11: Schematic view of the constructed 3-D mirror using interpolation.

the interpolated mirror as the initial value, and then we optimize a 3-D mirror using geometric optics as follows.

In the proposed imager, most of the echoes are reflected by the mirror and received on the array. We call the region of the mirror as the used area. When the used area consists of plural parts, a division of the main lobe is caused from interference of the parts. Therefore, it is necessary to set an evaluation function to prevent the used area from being divided into several parts. Minimizing the second moment of the used area about its center of gravity ensures that the used area consists of just one part; however, the used area also becomes small. Then we set functions

$$V_{\nu} = \sum_{\mathbf{w}} W_{\nu}(x'_{m}, y'_{m}) I_{m\nu}(x'_{m}, y'_{m}), \qquad (2.14)$$

$$d_{\nu}(x'_{m}, y'_{m})^{2} = (x'_{m} - x'_{G\nu})^{2} + (y'_{m} - y'_{G\nu})^{2} + (z'_{m} - z'_{G\nu})^{2}, \qquad (2.15)$$

$$W_{\nu}(x'_{m}, y'_{m}) = S_{\nu} - d_{\nu}(x'_{m}, y'_{m})^{2}, \qquad (2.16)$$

$$d_{\nu}(x'_{\rm m}, y'_{\rm m})^2 = (x'_{\rm m} - x'_{\rm G\nu})^2 + (y'_{\rm m} - y'_{\rm G\nu})^2$$

$$+(z'_{\rm m}-z'_{\rm G\nu})^2,$$
 (2.15)

$$W_{\nu}(x'_{\rm m}, y'_{\rm m}) = S_{\nu} - d_{\nu}(x'_{\rm m}, y'_{\rm m})^2,$$
 (2.16)

where  $\nu$  is the angle between the target direction and the line PC,  $I_{\rm m\nu}(x_{\rm m}',y_{\rm m}')$  is the echo power received on the array and reflected at the small area of the square measure as  $\Delta S(x_{\rm m}', y_{\rm m}')$  around  $M'(x_{\rm m}', y_{\rm m}', z_{\rm m}')$  on the mirror,  $G_{\nu}(x_{\rm G_{\nu}}', y_{\rm G_{\nu}}', z_{\rm G_{\nu}}')$  is the center

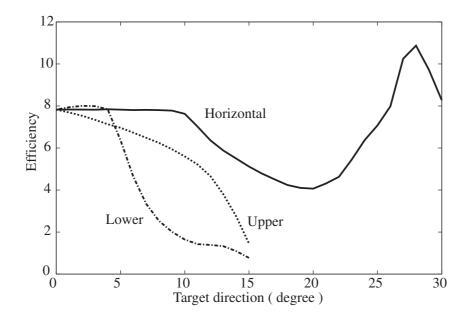


Figure 2.12: Angular characteristics of the efficiency of the proposed imager.

of gravity of the used area, and  $S_{\nu}$  is the square measure of the used area. Since the measurement field is 30 degrees vertically and 60 degrees horizontally, we set the evaluation function  $V_{3D}$  as the geometric function of  $V_{\nu}$  when the target exists in the x-z and CP-y' planes.

$$V_{3D} = \prod_{\nu_1 = -15}^{15} V_{\nu_1}^{1+2*(15-|\nu_1|)/15} \cdot \prod_{\nu_2 = 0}^{30} V_{\nu_2}^{1+2*(30-\nu_2)/30}, \qquad (2.17)$$

where  $\nu_1$  and  $\nu_2$  are the angles between the target direction and the line PC in the x-z and CP-y' planes, respectively.

In the next section we evaluate the spatial resolution of the optimized mirror.

# 2.6 Evaluation of the spatial resolution of the proposed imager in physical optics

In the optimization of the mirror shape we utilize geometric optics to simplify the optimization and so decrease the calculation time. We can use geometric optics when the mirror size is sufficiently larger than the wave length  $\lambda$ , because it neglects the effect of

interference at the edge of the mirror. In this section we more exactly evaluate the spatial resolution of the proposed imager utilizing physical optics [65], where the sound pressure variation on the reflector mirror is integrated numerically to consider the effect of the interference at the rim of the mirror.

Fig. 2.13 and 2.14 shows the angular resolution of the proposed imager from physical optics. The -3 dB lateral resolution of the proposed imager is; 2.52, 1.16 and 1.88 degrees in the target directions of -10, 0 and 10 degrees from the center in the vertical plane, and 1.20, 0.98 and 1.78 degrees in the target directions of 0, 10 and 20 degrees in the horizontal plane, where the transmit frequency f is 170 kHz. Fig. 2.15 shows the used area on the mirror from geometric optics, where a point target exists at the center for a 100 cm depth. The lateral resolution calculated using physical optics is consistent with that estimated from the used area on the mirror from geometric optics.

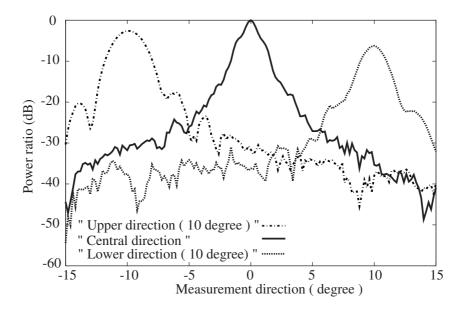


Figure 2.13: Lateral resolution of the proposed imager in a vertical plane.

In Fig. 2.16 we compare the efficiency of the proposed imager with an optimized 3-D imager using physical optics from a geometric one when a point target exists in the horizontal plane for a 100 cm depth. The angle between the target direction and the center is less than 30 degrees. We define the efficiency as the power ratio received on the array with or without a reflector mirror. The two efficiencies correspond with each other when a target exists in a field that is less than 15 degrees away from the center. There is some distance when a target exists in the direction that is more than 15 degrees away from the center; however, the fluctuation tendency of the efficiencies is the same. Fig. 2.17 shows the used area on the mirror when a point target exists in a direction of 30 degrees away from the center. This indicates that the echo from a peripheral direction is reflected

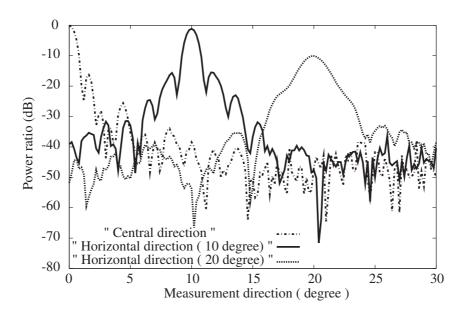


Figure 2.14: Lateral resolution of the proposed imager in a horizontal plane.

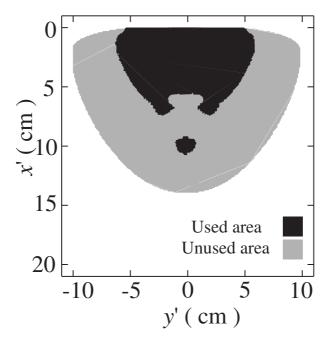


Figure 2.15: Used area on the mirror when a target exists at the center.

at the peripheral region of the mirror and then received on the array. Since the calculation using geometric optics assumes that a mirror exists with the width of the Fresnel zone around a reflection point, the receive power on the array is estimated as larger than the true value. We assume that this causes the difference between the efficiencies estimated using the two methods. The difference is a simple function of the target direction; thus, it can be easily corrected using Fig. 2.16. In this way the validity of the optimization of the mirror shape using geometric optics is demonstrated.

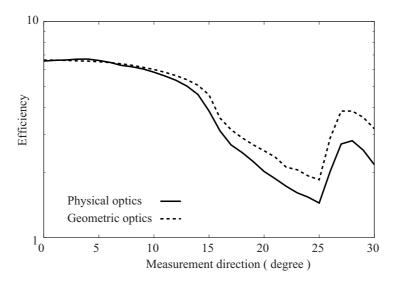


Figure 2.16: Receive power efficiency of the proposed imager in a horizontal plane.

The efficiency at the center is 6.62 and 6.56 in geometric and physical optics, respectively. The -3 dB lateral resolution at the center is 1.16 and 1.20 degrees in the vertical and horizontal planes, respectively. A digital beamforming imager with a circular 2-D element array has -3 dB lateral resolution

$$\theta_{1/2} = 58.4\lambda/D_1,\tag{2.18}$$

where  $D_1$  is the diameter of the array. Therefore, the spatial resolution of the proposed imager is the same as that of a digital beamforming imager with an elliptical array 10.07 cm long and 9.73 cm wide. The proposed imager has a elliptical array 3 cm long and 4 cm wide and thus the square measure of the array is 1/8.17 of that used in a digital beamforming imager having the same lateral resolution. This indicates the number of elements on the array can be reduced to about 1/8 of a dense 2-D array of a digital beamforming imager. The proposed imager has -3 dB lateral resolution that is better than 2 degrees in a measurement field of 15 degrees long and 30 degrees wide. This demonstrates that the proposed imager can satisfactorily be used as a vision substitute system.

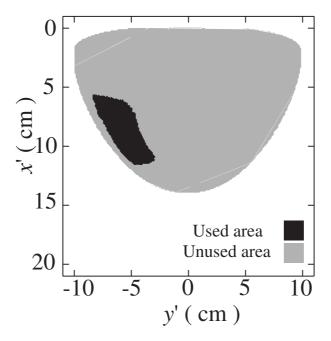


Figure 2.17: Used area on the mirror when a point target exists in a direction 30 degrees away from the center.

## 2.7 Real-time signal processing

For real-time signal processing, we calculate in advance the part of Eq. 2.8

$$L_{UT_2} = \frac{1}{2\pi} \int_{S} \frac{1 + jkR_2}{R_2^2 r_2} \frac{\boldsymbol{n_2} \cdot \boldsymbol{R_2}}{n_2 R_2} \cdot e^{-(jk+\alpha)(r_2+R_2)} dS.$$
 (2.19)

The estimated velocity vector is given by

$$\phi_{2U} = \sum_{U} A_{U}^{*} L_{UT_{2}}, \tag{2.20}$$

where we prepare a set of the values  $L_{UT_2}$  in a dictionary and calculate the vector from received signals with the aid of a dictionary look-up algorithm.

The data quantity used for a dictionary is estimated as follows. A dictionary has a set of the values  $L_{UT_2}$  at all the measurement points. The number of elements used on the array is 942 when the elements are placed on an elliptical array 3 cm long and 4 cm wide at intervals of 0.1 cm. The number of measurement directions is about 430 where the measurement direction intervals are 1 and 3 degrees at the center and a direction 30 degrees away from the center in a measurement field 30 degrees vertically and 60 degrees

horizontally, respectively. The number of sampled in the range from 15 cm and 4.5 m is 29 when the intervals of those sampled range between 1 cm and 30 cm for 1.5 cm and 4.5 m depths, respectively. Therefore the data number in a dictionary is 12 million.

A dictionary needs a memory device of about 90 MB when each datum is a single precision complex floating point number. All the data in the dictionary can be read to a memory device at one time; thus this system needs a suitably short data access time but without using a hard disc drive.

The calculation time of the estimated power of all the measurement points is about 0.07 seconds when we use an Xeon Pentium4 of 2.8 GHz. Since the sampling rate is  $14\mu$ s when the imager transmits a acoustic pulse wave of 2 cm in pulse length and samples 4 times for each range, the sampling process is realized using an analog-digital converter with a 64 MHz sampling rate when the number of elements is 942. The sample and hold time is  $14\mu$ s, which can be neglected compared to the propagation time. Hence the proposed imager can sample and receive signals at one time. The signal processing time containing the propagation time is about 0.1 second, and thus the proposed system can realize real-time imaging of 3-D environmental information.

### 2.8 Conclusion

We propose a hybrid imager with a concave mirror and a 2-D element array that uses an off-focus method, where images are reconstructed numerically from the received signals, as a low cost vision substitute system with high time and spatial resolution. Using a hybrid method a wide transmit beam is radiated to the entire measurement field. Since most of the echo from a target is reflected on the mirror and gathered on the array, the spatial resolution of the proposed imager is improved from that of a digital beamforming imager with a same size array. Using an off-focus method the distance between the reflector mirror and the array is fixed, and images of targets are reconstructed from the received signals by numerical back-projection. We optimize the mirror shape by utilizing geometric optics, and then evaluate the spatial resolution of the proposed imager using physical optics. The measurement field of the proposed imager is 30 degrees vertically and 60 degrees horizontally. The -3 dB lateral resolution is about 1 degree at the center, where the transmit frequency is 170 kHz, the concave mirror is 20 cm in width, and the elliptical array is 3 cm long and 4 cm wide. This means that the number of elements can be reduced to about 1/8 of that for a dense 2-D array of a digital beamforming imager. We also investigated a real-time signal processing system for the proposed imager.

## Chapter 3

# Human Interface and Transmit Frequency Control for The Through-Air Acoustic Real-Time High Resolution Vision Substitute System

### 3.1 introduction

Intensive studies have been made on human-machine information transfer through tactile excitation for vision substitution. A two-dimensional matrix of stimulators can display spatial information to the skin, and previous works have been directed to change visual image to vibrotactile or electrotactile stimulation [66][67]. In this method intensity of each stimulator corresponds to the light intensity of visual image and does not indicate the range of the target. Vision substitute system needs high time resolution to present dynamic change of spatial resolution and high spatial resolution to recognize many targets individually. Although various tactile vision substitution systems have been proposed, they are not useful as navigation systems for visually handicapped due to limited spatial and time resolution [68][69][70]. We proposed a high resolution real-time vision substitute system [71]. In this method we transmit ultrasonic pulse wave and receive the echoes by an element array with a reflector mirror. In this study we further propose a spatial information transfer method to present the range, direction and surface topography of the target through tactile excitation on the forehead, and a technique to control transmit frequency.

## 3.2 Summary of High Resolution Vision Substitute System

Phased array imagers and digital beam forming imagers have been proposed for high-resolution 3-D imaging system. Phased array imagers measure one direction by a transmit and receive event, and do not have sufficient time resolution. Digital beam forming imagers with 2-D dense array measure entire the target area by a transmit and receive event, but need enormous elements on the array. Though digital beam forming imagers with sparse array have been reported, it is difficult to reduce the number of elements to less than half of the dense array [72][73].

We proposed an acoustic 3-D imaging system based on a hybrid array-reflector configuration which realizes high time and spatial resolutions with modest computional load. Fig. 3.1 shows the schematic view of the proposed vision substitute system. In this system a broad transmit beam is radiated over the entire measuring area. The reflected echo is first focused by a concave reflector, and then received by the array. Reconstruction of widely distributed images on the array is based on numerical back projection. We call this hybrid method.

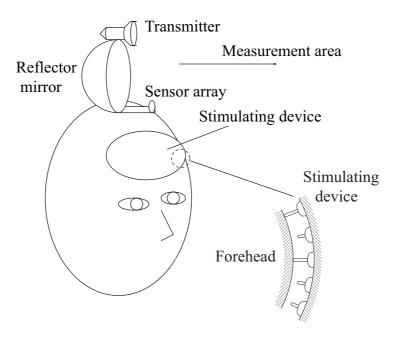


Figure 3.1: Schematic view of the system.

Fig. 3.2 shows the spatial resolution of the hybrid method in the case of the reflection mirror width of 20 cm, the elliptic dense 2-D array with 4cm major axis and 3cm minor axis, and the transmit frequency of 170 kHz. Its angle of view is  $\pm 15$  degrees and  $\pm 30$ 

degrees in the vertical and horizontal section, respectively. As evaluated by physical optics, the angular resolution at the center direction is 1.16 degree in the vertical section, and 1.20 degree in the horizontal section. Only 1/8 times as many elements are needed compared to the digital beam forming method. With the aid of dictionary look-up algorithm, the image reconstruction based on numerical back projection takes less than 0.1 second, which is sufficiently short for a real-time operation.

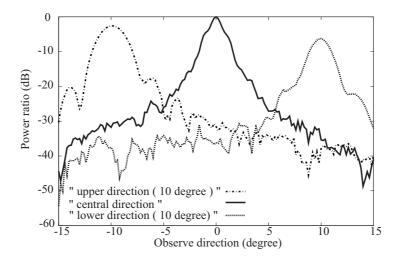


Figure 3.2: Angular characteristics of imaging calculated by physical optics in the vertical section.

## 3.3 Transmit Frequency Control

In the previous section, spatial resolution is investigated for the case that transmit frequency is 170 kHz and measuring range is 1 m. The signal to noise ratio of the echo from long distance deteriorates when we radiate pulses of high transmit frequency like 170 kHz due to strong attenuation. In this section we propose a scheme to select the optimum transmit frequency versus range.

Absorption attenuation of the echo power is proportional to  $e^{-4\alpha l}$ , where l is the target range and  $\alpha$  is the absorption coefficient. Fig. 3.3 shows frequency characteristics of the received echo power versus range. We set the absorption coefficient  $\alpha = 1.0 \times 10^{-8} f$  neper/cm, where f is the transmit pulse frequency. Received power is normalized by that of measuring range 1 m and transmit pulse frequency 20 kHz. Echo power attenuation of a high frequency pulse is limited at a short range, but significant at a long range. This means that a low frequency pulse should be radiated for a long range detection. The angular resolution of digital beam forming imager with 2-D circular array

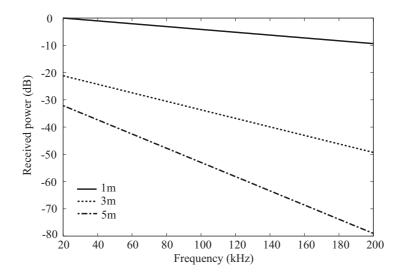


Figure 3.3: Frequency characteristics of the received signal power at various range.

is c/fD rad, where c is the propagation velocity of sound and D is the array size. We transmit low frequency pulses for long range detection to increase the echo power and high frequency pulses for short range detection to improve angular resolution. Repetition of transmit and receive events causes range aliasing. Echo power from another range over that from measuring range is given by

$$P_n = e^{-4\alpha(n-1)l}/n^4, (3.1)$$

where nl is the range which causes range aliasing. We set constant lf to make  $P_n$  and l independent of each other by controlling the transmitting frequency. In the case of  $lf = 170 \text{ m} \cdot \text{kHz}$ ,  $P_2 = -20.9 \text{ dB}$  and  $P_3 = -36.8 \text{ dB}$ . This means the influence of range aliasing is negligible. Fig. 3.4 shows signal to noise ratio of received echo versus range. Solid line is signal to noise ratio of proposed method, and broken line is that of constant transmit frequency of 170 kHz. Improvement of SNR becomes larger at longer range detection, which increases to 40 dB at the measuring range of 5 m.

## 3.4 Spatial Information Transfer by Tactile Display

### 3.4.1 Setting of stimulation points and measuring direction

We assume to stimulate vibrotactile excitation at the location corresponding to the target direction. As the forehead has wide area for stimulation and keen sense of touch, it is suitable for stimulation region. Since the spatial resolution against stimulation at the forehead is about 5 mm, we set stimulator pitch 5mm. Fig. 3.5 shows the alignment of

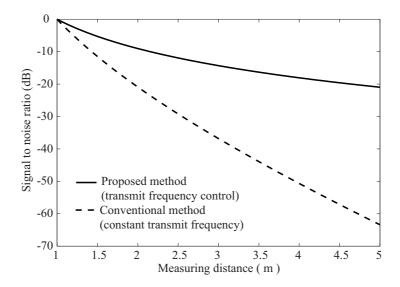


Figure 3.4: Signal to noise ratio versus range.

the stimulating points on the forehead in the case of the stimulating area of 6 cm long and 10 cm wide. The stimulator array consists of  $13 \times 21$  elements.

Vision has wide angle of view and high angular resolution at the center. We set the angle of view of the vision substitute system  $\pm 15$  degrees in the vertical section,  $\pm 30$  degrees in the horizontal section, and the sampling interval of measuring direction 1 degree at the center. We set measuring directions as follows.

First, we arrange measuring directions on the horizontal and vertical lines at irregular spacing. We set hyperbolas which go through the measuring points on the lines, and we define their intersections as the measuring directions. Fig. 3.6 shows measuring directions in the target area. The sampling interval of measuring directions on the lines follow quadratic function. Stimulating points on the forehead of Fig. 3.5 and measuring directions of Fig. 3.6 correspond one to one.

In the case of arranging 21 measuring directions on the horizontal line of  $\pm 30$  degrees at a regular spacing, the sampling interval is 3 degree. In the proposed layout, the interval is 1 degree at the center and 4 degree at the peripheral directions.

## 3.4.2 Spatial Information Transfer

To distinguish multiple targets, we need to present targets' direction, range and echo power related to their surface topography. The proposed system presents the direction of a target by stimulating location, and their echo power by vibrotactile excitation intensity. The subject can recognize target range as follows.

Fig. 3.7 shows schematic view of targets in the measuring area. Color depth of targets

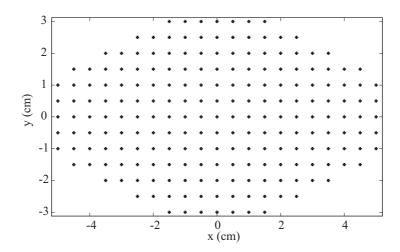


Figure 3.5: Stimulating points on the forehead.

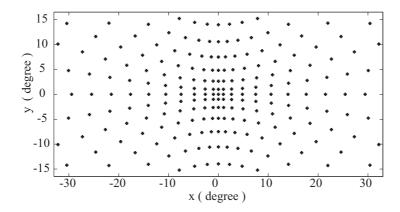


Figure 3.6: Measuring directions in the target area. Intervals follow quadratic function.

is related to their echo power. Fig. 3.8 is the projection image of targets to the measuring area. Neighboring target is displayed in the case of plural targets existing in the same direction. The range of target A, B, C is less than d1, and that of D, E, F is between  $d_1$  and  $d_2$ .

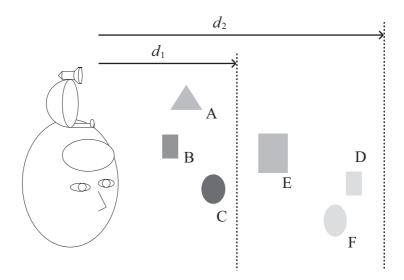


Figure 3.7: Schematic view of targets in the measuring area. Color depth is related to echo power.

First, the subject determines measuring range of  $d_1$  and instruct it to the vision substitute system. We suppose the instruction is given by biting force of a switch. The pulse frequency and interval are made suitable to the range  $d_1$  and the system present direction and echo power of target A, B, C by vibrotactile excitation on the forehead. Fig. 3.9 shows stimulating points matched with targets in the case of measuring range of  $d_1$ . Size of each symbol indicates the stimulation pressure related to the echo power. The system presents the echo power by stimulating pressure and the subject can recognize not only the size and direction of targets but also its surface topography. Second, he/she instructs the system the measuring range of  $d_2$ , and the system presents the directions and the echo power of target A, B, C, D, E, F. Fig. 3.10 shows stimulating points matched with targets in the case of measuring range  $d_2$ .

From the change of displayed information the subject recognizes the range of target D, E, F is between  $d_1$  and  $d_2$ . He/she can also find the boundary of target B and E (also C and F) from stimulating pressure difference. Targets at shorter range is more important and vision detects only the nearest target in each direction. For safety of subjects and similarity with vision we propose to present the nearest target in the case of plural targets existing in the same direction. By measuring from short range to long range, we get spatial information of the whole target area. The time resolution of the

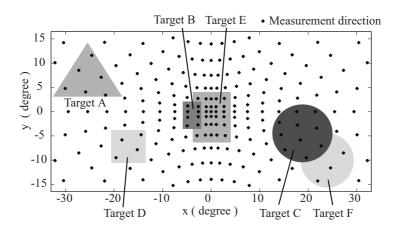


Figure 3.8: Targets' directions in the measuring area. Color depth is related to echo power.

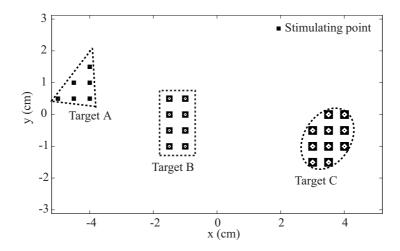


Figure 3.9: Stimulating points matched with targets in the case of measuring distance is  $d_1$ . Size indicates stimulating pressure related to echo power.

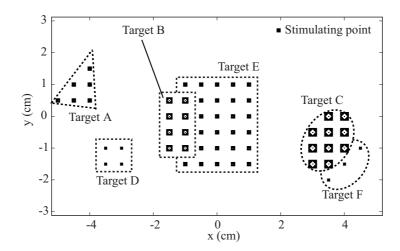


Figure 3.10: Stimulating points matched with targets in the case of measuring distance is  $d_2$ . Size indicates stimulating pressure related to echo power.

system is about 0.1 second, which can deal with movement of pedestrians.

### 3.5 Conclusion

For the wide range detection of the acoustic vision substitute system, we proposed a transmit frequency control method. In this method, we transmit low frequency pulses for long range detection to receive sufficient echo power and high frequency pulses for short range detection to improve angular resolution. In the case of product of transmit frequency and measuring range is  $lf = 170 \text{ m} \cdot \text{kHz}$ , the effect of range aliasing is reduced to less than -20 dB. We also proposed a human-machine information transfer method to present the target area of  $\pm 15$  degrees long and  $\pm 30$  degrees wide by the sampling interval of 1 degree at the center. The vibrotactile stimulator array consists of  $13 \times 21$  arrangement on the forehead of 6 cm  $\times$  10 cm size. The subject instructs measuring range to the vision substitute system, and it presents direction and echo power of targets existing within the instructed range. The direction and echo power of the target is presented by stimulating location on the forehead and excitation intensity, respectively. In this method, he/she can distinguish multiple targets of the same range. The time resolution of 0.1 sec per 1 image is sufficiently high for the use of pedestrians.

## Chapter 4

## High-Resolution Real-Time 3-D Acoustic Imaging System with a Reflector

#### 4.1 Introduction

Volumetric 3-D high-resolution acoustic images are in high demand for medical diagnoses. A conventional phased array imager excites all array elements to form a transmit beam, and uses all of them for receive beamforming [74]. Although only the receive beam is dynamically focused, imaging under this condition results in a high electronic signal-to-noise ratio (SNR) as well as good spatial and contrast resolution. The main problem of this configuration is that the number of elements becomes enormous for a 2-D array of a 3-D phased array imager.

One strategy to reduce the costs and complexity of a 3-D phased array imager is to use a linear or convex array that is moved mechanically [75]-[77]. In this method the number of elements can be reduced greatly by using a 1-D array. The lateral resolution in the measuring plane is high because a receive beam is focused dynamically. However, in the plane perpendicular to the longitudinal axis of the array, a transmit beam and a receive beam are focused on a fixed distance by acoustic lenses on elements. Thus, the lateral resolution is seriously deteriorated in front and behind the focus. Moreover, this type of 3-D phased array imager does not have satisfactory time resolution.

Another strategy to improve time resolution and decrease the number of elements, at the cost of the loss of some lateral resolution and SNR, is to use a digital beam forming technique with a 2-D sparse array, with an element spacing of more than one-half of a wavelength [78]-[87]. This method uses a wide transmit beam and multiple receive beams formed simultaneously. Although several designs of array have been reported, it is difficult to reduce the number of elements to less than half of the dense array.

Karaman et al. [88] proposed that a single-element spatial response with high acoustic

power can be synthesized by a defocused multi-element transmit subaperture. Lockwood et al. [89] applied this scheme to a 3-D synthetic aperture imager with a 1-D array. Although the SNR is improved, lateral resolution deteriorates in the section perpendicular to the array for the same reason as that of a phased array imager with a 1-D array.

In this study we propose a system based on a hybrid array-reflector configuration that realizes high time and spatial resolutions with modest computational load to resolve these problems. In this system all elements on a small dense array are excited with appropriate time delays to synthesize a spatial response similar to that of a single element. The echoes from targets are first gathered by a concave reflector, and then received by the array. The image of the target is reconstructed by numerical back projection [90] from the de-focused image distributed on the array.

In Materials and methods, we first outline the framework of the proposed 3-D acoustic imaging system. We provide some necessary wave equations and parameters to evaluate the spatial resolution of this method. Then we optimize the reflector shape and the array configuration for a wide measurement area with high spatial resolution. We propose a method to suppress the sidelobe level by employing a proper reflection coefficient of the mirror in the numerical back projection. The proposed method reconstructs images from received signals by numerical back projection, and thus the reflection ratio of the mirror can be set freely in the numerical back projection. We examine the spatial resolution of the proposed imager in Results. In Discussion, we compare the spatial resolution of the proposed imager with current 3-D imagers. Furthermore we evaluate improvements in the SNR with the proposed imager compared to conventional ones, such as digital beam forming and phased array imagers. Finally, we draw conclusions.

#### 4.2 Materials and methods

# 4.2.1 Principle of the hybrid 3-D imaging system with a small dense array and a reflector

A digital beamforming imager transmits a wide beam to the whole measured area and receives echoes by a 2-D array. It then utilizes inverse Fourier transform to make all the images in the measurement area. Since this imager makes a 3-D image from one transmit and receive event, it has high time resolution. However, a large 2-D array with an enormous number of elements is required to obtain high spatial resolution, which thus is very costly. We propose a system to decrease the number of elements but having the same high time and spatial resolutions.

Fig. 4.1 shows a schematic view of the acoustic real-time 3-D imaging system based on a hybrid array-reflector configuration. In this method, all elements on a small dense array are excited with proper time delays so that all transmit pulses are focused at a single point after reflecting at the reflector mirror. Then the transmit pulses are synthesized

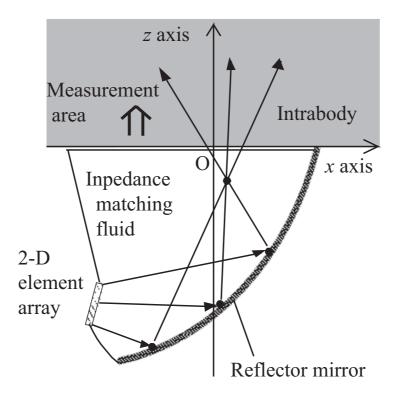


Figure 4.1: Schematic view of the system in the transmit phase.

to a broad beam similar to that of a single transmit element with high acoustic power. A transmit beam is radiated over the entire measuring field from this focal point. The reflected echoes are first gathered by a concave reflector, and then received by the array, as shown in Fig. 4.2. Since the reflector and the array are fixed, it is out of focus and so a de-focused image is distributed on the array. The image of the target is reconstructed from the received signal on the array by numerical back projection.

With this scheme, images of the whole area measured can be reconstructed from a single transmit and receive event, which enables real-time 3-D imaging. Assuming that the propagation velocity of sound is 1600 m/s, in the case that maximum measuring range is 0.16 m, it is theoretically possible to realize a frame rate of 5000 3-D images/s, when the SNR is sufficiently high.

## 4.2.2 Calculation of acoustic propagation

In this section, to evaluate spatial resolution of the proposed 3-D acoustic imager, we explain the wave equations to calculate signals received on the array and the estimated pressure at the measuring points.

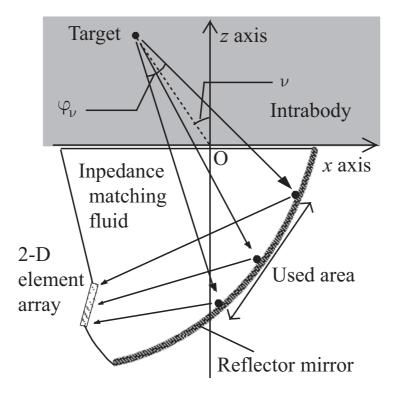


Figure 4.2: Schematic view of the system in the receive phase.

#### Calculation of received signals

The received signal is the scattered pressure field integrated over the element array. We calculate this signal in the frequency domain. Fig. 4.3 shows the coordinate system for the calculation.

All transmit pulses from elements with proper time delays are reflected on the mirror and focused at  $T_r$ . A broad beam is then radiated from this point. The transmit beam is scattered at  $T_a$  by the inhomogeneity of the target. The backscattered echo is reflected on the mirror at M, and received by an element at  $S_1$ .  $U_1$  and  $U_2$  are the intersections of lines  $T_rT_a$  and  $T_aM$ , respectively, in the x-y plane. If the size of the target is sufficiently smaller than the wavelength, the pressure variation in the frequency domain at M is given by

$$p_{\rm M}(\omega) = \left\{ \frac{\Delta c}{c_0} + (1 + \cos \theta_1) \frac{\Delta \rho}{2\rho_0} \right\}$$

$$(jk)^2 \frac{e^{-(\alpha_1 + jk)(r_{1a} + r_{2a}) - (\alpha_2 + jk)(r_{1b} + r_{2b})}}{4\pi^2 (r_{1a} + r_{1b})(r_{2a} + r_{2b})} A(\omega) \Delta V, \tag{4.1}$$

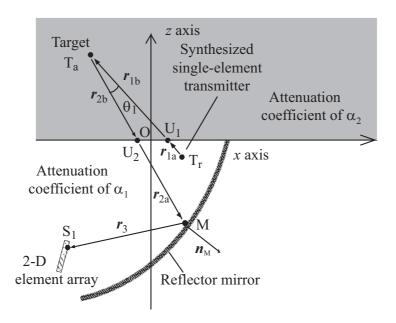


Figure 4.3: Arrangement of a 2-D element array and a mirror in the transmit phase.

where  $\mathbf{r}_{1a} = \overrightarrow{\mathrm{T_r U_1}}, \mathbf{r}_{1b} = \overrightarrow{\mathrm{U_1 T_a}}, \mathbf{r}_{2a} = \overrightarrow{\mathrm{U_2 M}}, \mathbf{r}_{2b} = \overrightarrow{\mathrm{T_a U_2}}, r_{1a} = |\mathbf{r}_{1a}|, r_{1b} = |\mathbf{r}_{1b}|, r_{2a} = |\mathbf{r}_{2a}|, r_{2b} = |\mathbf{r}_{2b}|, \omega$  is the angular frequency,  $k = \omega/c_0$  is the wave number,  $\theta_1 = \angle \mathrm{T_r T_a M}, \rho_0$  is the density of the undisturbed medium,  $c_0$  is the mean propagation velocity,  $\Delta \rho$  is the variation of the density,  $\Delta c$  is the variation of the propagation velocity,  $\Delta V$  is the volume of a target, and  $A(\omega)$  is the frequency spectrum of transmit beam radiated from  $\mathrm{T_r}$  [91].  $\alpha_1$  and  $\alpha_2$  are attenuation coefficients of the impedance matching fluid and the intrabody, respectively.  $|\Delta c|/c_0$  and  $|\Delta \rho|/\rho_0$  should satisfy

$$|\Delta c|/c_0 \ll 1, \tag{4.2}$$

$$|\Delta \rho|/\rho \ll 1. \tag{4.3}$$

We introduce the assumption that  $r_{2a} + r_{2b}$  is much longer than the wavelength, in other words  $k(r_{2a} + r_{2b}) \gg 1$ , and then the particle velocity at M is given by

$$\nu_{\rm M}(\omega) = p_{\rm M}(\omega)/\rho_0 c_0. \tag{4.4}$$

The volume velocity of a small area around M is

$$V_{\rm M} = \nu_{\rm M}(\omega) \Delta S \frac{\mathbf{r}_{\rm 2a} \cdot \mathbf{n}_{\rm M}}{r_{\rm 2a} n_{\rm M}},\tag{4.5}$$

where  $n_{\rm M}$  is a vector perpendicular to the mirror at M,  $n_{\rm M} = |n_{\rm M}|$ , and  $\Delta S$  is the square measure of the small area on the mirror. Then the velocity potential and pressure variation at  $S_1$  are obtained respectively by

$$\Phi_{S_{1}}(\omega) = \int_{S} \frac{V_{M}e^{-(\alpha_{1}+jk)r_{3}}}{2\pi r_{3}}dS, \qquad (4.6)$$

$$p_{S_{1}}(\omega) = j\rho\omega\Phi_{S_{1}}(\omega)$$

$$= \int_{S} -jk^{3} \left\{ \frac{\Delta c}{c_{0}} + (1+\cos\theta_{1})\frac{\Delta\rho}{2\rho_{0}} \right\} \frac{\mathbf{r}_{2a} \cdot \mathbf{n}_{M}}{r_{2a}n_{M}}$$

$$\frac{e^{-(\alpha_{1}+jk)(r_{1a}+r_{2a}+r_{3})-(\alpha_{2}+jk)(r_{1b}+r_{2b})}}{8\pi^{3}(r_{1a}+r_{1b})(r_{2a}+r_{2b})r_{3}} A(\omega)\Delta V dS, \qquad (4.7)$$

where  $\mathbf{r}_3 = \overrightarrow{\mathrm{MS}}_1, r_3 = |\mathbf{r}_3|$ .

The pressure variation in the time domain at  $S_1$  is given by the inverse Fourier transformation of  $p_{S_1}(\omega)$  as

$$P_{S_1}(t) = F^{-1}[p_{S_1}(\omega)].$$
 (4.8)

As it is difficult to calculate  $p_{S_1}(\omega)$  of all angular frequencies, we introduce an assumption

$$e^{-\alpha_1(r_{2a}+r_3)-\alpha_2 r_{2b}} \simeq e^{-\alpha_1(r_{0b}+r_{0c})-\alpha_2 r_{0a}},$$
 (4.9)

where  $r_{0a} = |\overrightarrow{T_aO}|, r_{0b} = |\overrightarrow{OM_0}|, r_{0a} = |\overrightarrow{U_2M}|, S_0$  is the center of the 2-D array, and  $M_0$  is at the center in the visual angle of the mirror from  $S_0$ , as shown in Fig. 4.4.

By introducing this assumption, the following equations are given from Eq. 4.7.

$$p_{S_1}(\omega) \simeq p_{1S_1}(\omega)p_{2S_1}(\omega),$$
 (4.10)

$$p_{1S_1}(\omega) = -jk^3 e^{-\alpha_1(r_{1a} + r_{0b} + r_{0c}) - \alpha_2(r_{1b} + r_{0a})} A(\omega) \Delta V / (8\pi^3), \tag{4.11}$$

$$p_{2S_{1}}(\omega) = \int_{S} \left\{ \frac{\Delta c}{c_{0}} + (1 + \cos \theta_{1}) \frac{\Delta \rho}{2\rho_{0}} \right\} \frac{r_{2a} \cdot n_{M}}{r_{2a} n_{M}}$$

$$\frac{e^{-jk(r_{1a} + r_{1b} + r_{2a} + r_{2b} + r_{3})}}{(r_{1a} + r_{1b})(r_{2a} + r_{2b})r_{3}} dS.$$
(4.12)

 $P_{\mathrm{S}_1}(t)$  is given by the convolution of  $F^{-1}[p_{1\mathrm{S}_1}(\omega)]$  and  $F^{-1}[p_{2\mathrm{S}_1}(\omega)]$ . Since  $p_{1\mathrm{S}_1}(\omega)$  is independent of the position of M, it is enough to calculate  $p_{1\mathrm{S}_1}(\omega)$  only one time. In the value  $p_{2\mathrm{S}_1}(\omega)$  only the term  $e^{-jk(r_{1\mathrm{a}}+r_{1\mathrm{b}}+r_{2\mathrm{a}}+r_{2\mathrm{b}}+r_3)}$  is dependent on  $\omega$ . Therefore  $F^{-1}[p_{2\mathrm{S}_1}(\omega)]$  is an impulse function. Then the following equations are given.

$$P_{S_{1}}(t) \simeq P_{1S_{1}}(t) * F^{-1}[p_{2S_{1}}(\omega)]$$

$$= \sum P_{1S_{1}} \left\{ t - (r_{1a} + r_{1b} + r_{2a} + r_{2b} + r_{3})/c_{0} \right\}$$

$$\left\{ \frac{\Delta c}{c_{0}} + (1 + \cos \theta_{1}) \frac{\Delta \rho}{2\rho_{0}} \right\} \frac{\mathbf{r}_{2a} \cdot \mathbf{n}_{M}}{r_{2a} n_{M}} \frac{\Delta S}{(r_{1a} + r_{1b})(r_{2a} + r_{2b})r_{3}}, \quad (4.13)$$

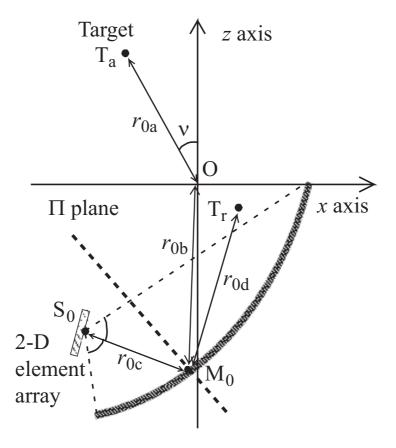


Figure 4.4: Schematic view of the mirror and array configuration for calculating in the time domain.

$$P_{1S_1}(t) = F^{-1}[p_{1S_1}(\omega)].$$
 (4.14)

The received signal on the element at  $S_1$  is proportional to  $P_{S_1}(t)$ .

#### Image reconstruction

We reconstruct images of targets from the distributed images on the array by numerical back projection. Similar to the calculation of the received signal, we define an element and the measuring point existing, respectively, at  $S_{2m}$  and  $T_b$ , as shown in Fig. 4.5. Assuming that the received signal is proportional to the estimated volume velocity at  $S_{2m}$ , the estimated velocity potential at M is given by

$$\Phi_{\rm M}(\omega)' \propto \sum_{m} \frac{p_m(\omega)'^* e^{-(\alpha_1 + jk)r_3'}}{2\pi r_3'},$$
(4.15)

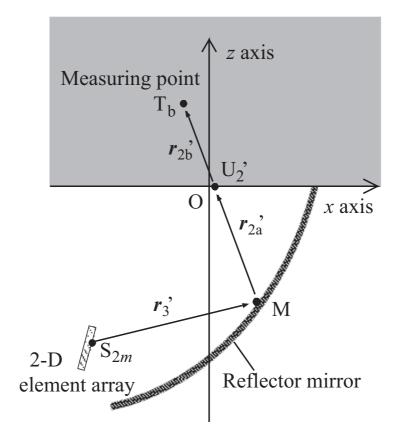


Figure 4.5: Arrangement of a 2-D element array and a mirror in the receive phase.

where  $\mathbf{r}_{3}' = \overrightarrow{S}_{2m}\overrightarrow{M}$ ,  $r_{3}' = |\mathbf{r}_{3}'|$ ,  $p_{m}(\omega)'^{*}$  is a complex conjugate of the received signal on the element. The estimated volume velocity at M is given by

$$V_{\rm M}' = -\frac{\partial \Phi_{\rm M}(\omega)'}{\partial r_{3}'} \frac{\mathbf{r}_{3}' \cdot \mathbf{n}_{\rm M}}{r_{3}' n_{\rm M}} \Delta S. \tag{4.16}$$

The estimated velocity potential and the estimated pressure variation at  $T_{\rm b}$  are given by

$$\Phi_{T_{b}}(\omega)' = \int_{S} \frac{V_{M}' e^{-(\alpha_{1}+jk)r_{2a}'-(\alpha_{2}+jk)r_{2b}'}}{2\pi(r_{2a}'+r_{2b}')} dS,$$

$$p_{T_{b}}(\omega)' = j\rho\omega\Phi_{T_{b}}(\omega)'$$
(4.17)

respectively, where  $\boldsymbol{r}_{2a}' = \overrightarrow{MU_2}', \boldsymbol{r}_{2b}' = \overrightarrow{U_2'T_b}, r_{2a}' = |\boldsymbol{r}_{2a}'|, r_{2b}' = |\boldsymbol{r}_{2b}'|.$ 

The pressure variation in the time domain at T<sub>b</sub> is given by the inverse Fourier transformation of  $p_{\mathrm{T_b}}(\omega)'$  as

$$P_{\rm T_b}(t)' = F^{-1} \left[ p_{\rm T_b}(\omega)' \right].$$
 (4.19)

We also introduce an assumption

$$e^{-\alpha_1(r_{2a}'+r_3')-\alpha_2r_{2b}'} \simeq e^{-\alpha_1(r_{0b}+r_{0c})-\alpha_2r_{0a}}.$$
 (4.20)

By introducing this assumption, the following equations are given from Eq. 4.18.

$$p_{\mathrm{T_b}}(\omega)' \propto p_{\mathrm{1T_b}}(\omega)' p_{\mathrm{2T_b}}(\omega)',$$
 (4.21)

$$p_{T_{b}}(\omega)' \propto p_{1T_{b}}(\omega)'p_{2T_{b}}(\omega)', \qquad (4.21)$$

$$p_{1T_{b}}(\omega)' = -k^{2}e^{-\alpha_{1}(r_{0b}+r_{0c})-\alpha_{2}r_{0a}}p_{m}(\omega)'^{*}/(4\pi^{2}), \qquad (4.22)$$

$$p_{2T_{b}}(\omega)' = \int_{S} \frac{e^{-jk(r_{2a}' + r_{2b}' + r_{3}')}}{(r_{2a}' + r_{2b}')r_{3}'} \frac{\mathbf{r}_{3}' \cdot \mathbf{n}_{M}}{r_{3}'n_{M}} dS.$$
(4.23)

As the equations 4.13, 4.14, and 4.15, the following equations are obtained.

$$P_{T_{b}}(t)' \propto P_{1T_{b}}(t)' * F^{-1} \left[ p_{2T_{b}}(\omega)' \right]$$

$$= \sum_{T_{b}} \left\{ t - (r_{2a}' + r_{2b}' + r_{3}')/c_{0} \right\}' \frac{\boldsymbol{r}_{3}' \cdot \boldsymbol{n}_{M}}{r_{3}' n_{M}} \frac{\Delta S}{(r_{2a}' + r_{2b}')r_{3}'}, \quad (4.24)$$

$$P_{1T_{\rm b}}(t)' = F^{-1} \left[ p_{1T_{\rm b}}(\omega)' \right].$$
 (4.25)

The estimated power at T<sub>b</sub>, the objective function, is given by

$$W_{\rm T_b}(t)' \propto P_{\rm T_b}(t)' P_{\rm T_b}(t)'^*$$
 (4.26)

#### Calculation parameters

To investigate spatial resolution of the proposed method, we set the parameters as follows: mean propagation velocity  $c_0 = 1600$  m/s, density of the undisturbed medium  $\rho_0 =$  $1.08 \times 10^3$  kg/m<sup>3</sup>, the variation of the propagation velocity  $\Delta c = -300$  m/s, and the variation of the density  $\Delta \rho = -1.0 \times 10^2 \text{ kg/m}^3$ . The attenuation coefficients  $\alpha_1$  and  $\alpha_2$ are  $2.0(\omega/2\pi)^2 \times 10^{-14}$  and  $5.0(\omega/2\pi) \times 10^{-6}$  Np/m, respectively. In this method, similar to the digital beamforming method, the element pitch is 0.5  $\lambda$  to prevent grating lobes, where  $\lambda = c/f_0$  is the wavelength at the center frequency. Therefore the radiating high frequency ultrasound needs the miniaturization of the element size. In this paper, we set the element pitch as  $5 \times 10^{-4}$  m. This means that  $\lambda = 0.001$  m; in other words, the center frequency  $f_0 = 1.6$  MHz. Since the number of elements on the array is proportional to the cost, to employ a large array is unrealistic. Many researchers have investigate 2-D arrays

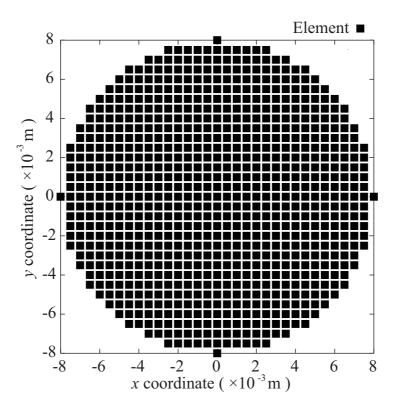


Figure 4.6: Element pattern for a 797-element array.

with 500 to 1000 elements [86] [87]. We employ a circular array of 0.016 m in diameter with 797 elements, as shown in Fig. 4.6.

Fig. 4.7 shows the broad-band pulse transmitted by the elements in this paper, where -6 dB fractional bandwidth is 60 %. The spectrum of the pulse is expressed as

$$S(\omega) = A_{\rm c}\omega^2 e^{-B_{\rm c}(\omega-\mu)^2} \tag{4.27}$$

where  $A_{\rm c}$  and  $B_{\rm c}$  are coefficients and  $\mu$  is the central angular frequency. Since we proposed that a wide transmit beam with high acoustic power can be synthesized using focusing method [92], we assume that the synthesized transmit beam is an omnidirectional spherical wave whose spectrum is proportional to  $S(\omega)e^{-\alpha_1(r_{0\rm c}+r_{0\rm d})}$ , where  $r_{0\rm d}=|\overrightarrow{\rm M}_0\overrightarrow{\rm T}_{\rm r}|$  and  $e^{-\alpha_1(r_{0\rm c}+r_{0\rm d})}$  is caused by the attenuation through the impedance matching fluid.

## 4.2.3 Optimization of the reflector shape and the array configuration

Since we reconstruct the received signal by numerical back projection, there is no need to focus it on the array. This indicates that the reflector shape suitable for this method

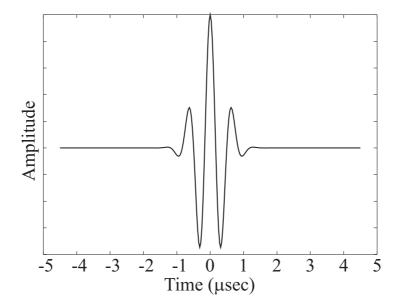


Figure 4.7: Waveform of the pulse used in this paper.

may be different from traditional ones. Utilizing geometric optics we optimize the reflector shape and the array configuration for a wide measurement area with high spatial resolution.

Fig. 4.2 schematically shows the ray trace of an echo in geometric optics. Part of the echo reflected on the mirror is received on the array. We call the reflected region on the mirror the 'used area', and define  $\varphi_{\nu}$  as the visual angle of the used area from the target position as follows.

$$\varphi_{\nu} = \int_{S} \frac{g(\mathbf{r})}{r^{3}} \mathbf{r} \cdot d\mathbf{S}$$

$$= \sum_{\mathbf{r}} g(\mathbf{r}) \frac{\mathbf{r} \cdot \mathbf{n}_{M}}{r^{3} n_{M}} \Delta S, \qquad (4.28)$$

$$g(\mathbf{r}) = \begin{cases} 1 & \text{if the point M is on the used area} \\ 0 & \text{else} \end{cases}$$
 (4.29)

where  $\mathbf{r} = \mathbf{r}_{2a} + \mathbf{r}_{2b}$ ,  $r = |\mathbf{r}|$  and  $\nu$  is the target direction from the z axis, as shown in Fig. 4.4.

First, in the case where the used area consists of plural groups, the sidelobe level is high because the main lobe divides. Below, we investigate an example of such a case. Fig. 4.8 is the used area on the mirror in the x-z section. The x, y and z coordinates of

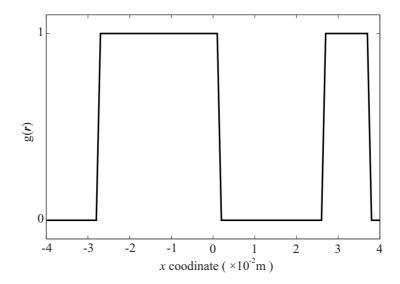


Figure 4.8: The area used on the mirror in the x-z section. The value of used area is 1 and that of non-used area is 0. The x, y and z coordinates of a target are 0.005, 0 and 0.07 m respectively.

a target are 0.005, 0 and 0.07 m, respectively. The function value of 1 means that the region of the mirror is a used area, and 0 means that it is a non-used area. In this case the echo reflected on a region, whose x coordinate is more than 0.002 m and less than 0.026 m, is not received on the array. Thus the used area consists of two groups, one is the region on the mirror whose x coordinate is negative and the other is the right edge. Fig. 4.9 is the lateral resolution of this mirror for a depth of 0.07 m. The first sidelobe level is -5.9 dB, which disturbs the medical diagnoses. Therefore, we discard the mirror with a used area in the x-z plane or  $\Pi$  plane that consists of plural groups. The  $\Pi$  plane is perpendicular to both the x-z plane and the mirror, as shown in Fig. 4.4. The intersection of the  $\Pi$  plane and the mirror in the x-z plane is at the center in the visual angle of the mirror.

Next, we optimize the mirror shape under the above conditions. To realize sufficient lateral resolution and SNR using a small array, the echo should be gathered on the array. This means that the visual angle should be maximized. We set the evaluation function

$$E = E_{\mathbf{X}} + E_{\mathbf{Y}}, \tag{4.30}$$

$$E = E_{X} + E_{Y}, \qquad (4.30)$$

$$E_{X} = \int_{\nu_{X_{\min}}}^{\nu_{X_{\max}}} \varphi_{\nu} d\nu = \sum_{x} \varphi_{\nu} \Delta \nu, \qquad (4.31)$$

$$E_{\rm Y} = \int_{\nu_{\rm Ymin}}^{\nu_{\rm Ymax}} \varphi_{\nu} d\nu = \sum_{y} \varphi_{\nu} \Delta \nu,$$
 (4.32)

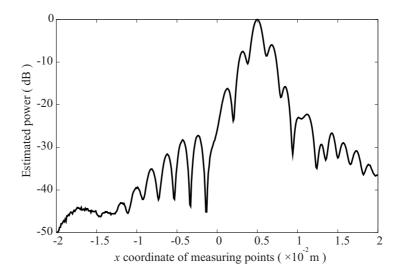


Figure 4.9: Lateral resolution where the used area consists of plural groups. The main lobe divides, and thus the sidelobe level becomes high.

where  $E_{\rm X}$  and  $E_{\rm Y}$  are in cases where targets are in the x-z and y-z planes, respectively. As shown in Eq. 4.28,  $\varphi_{\nu}$  is determined indirectly by the shape of the reflection mirror. Thus the maximization of E becomes a problem of finding the optimum shape function of a mirror that gives the highest value of E.

We call the shape functions of the optimized reflector in the x-z and  $\Pi$  planes  $f_x$  and  $f_y$ , respectively. These functions are given by

$$f_{x} = l_{1x} \left[ \left\{ 1 - \cos(l_{3x}x + l_{3x}x_{\max} + l_{4x}) \right\}^{l_{2x}} - \left\{ 1 - \cos(l_{4x}) \right\}^{l_{2x}} \right]$$

$$/ \left[ \left\{ 1 - \cos(2l_{3x}x_{\max} + l_{4x}) \right\}^{l_{2x}} - \left\{ 1 - \cos(l_{4x}) \right\}^{l_{2x}} \right]$$

$$f_{y} = l_{1y} \left\{ 1 - \cos(l_{3y}y) \right\}^{l_{2y}} / \left\{ 1 - \cos(l_{3y}y_{\max}) \right\}^{l_{2y}},$$

$$(4.34)$$

where  $x_{\text{max}}$  and  $y_{\text{max}}$  are half of the mirror width in the x-z and  $\Pi$  planes, respectively. They are in fact the heights from the bottom points of the reflector in each section.

Since we determine the visual angle of the measuring area as  $\pi/3$ , we set  $\nu_{\text{Xmax}} = \nu_{\text{Ymax}} = \pi/6$ ,  $\nu_{\text{Xmin}} = \nu_{\text{Ymin}} = -\pi/6$ . Then we optimize  $l_{1x}, l_{2x}, l_{3x}, l_{4x}, l_{1y}, l_{2y}, l_{3y}, x_{\text{max}}, y_{\text{max}}$  by maximizing the evaluation function E. The range of each variable is as follows:  $0.025 \text{ m} \leq x_{\text{max}} \leq 0.04 \text{ m}, 0.025 \text{ m} \leq y_{\text{max}} \leq 0.04 \text{ m}, 0.01 \text{ m} \leq l_{1x} \leq 0.1 \text{ m}, 0.5 \leq l_{2x} \leq 3, \pi/40 \leq l_{3x}x_{\text{max}}, 0 \leq l_{4x}, 2l_{3x}x_{\text{max}} + l_{4x} \leq \pi/2, 0.01 \text{ m} \leq l_{1y} \leq 0.1 \text{ m}, 0.5 \leq l_{2y} \leq 3, \pi/20 \leq l_{3y}y_{\text{max}} \leq \pi/2.$ 

It is thought that many local maximums of E exist. We first optimize  $f_x$  and  $f_y$  by maximizing  $E_X$  and  $E_Y$ , respectively. At this optimization we deal with a 2-D problem.

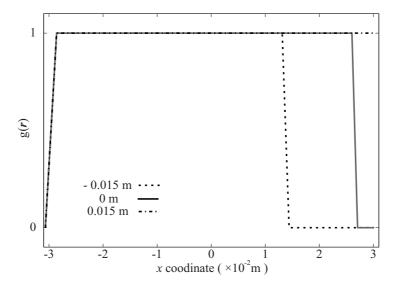


Figure 4.10: The used area on the optimized mirror in the x-z section. The value of the used area is 1 and that of the non-used area is 0. The x coordinates of targets are -0.015, 0 and 0.015 m. The target range is 0.07 m in the x-z section.

We set this as the initial value of the mirror shape, and optimize by maximizing E. We deal with a 3-D problem with this optimization.

The variables of the optimized reflector mirror are:  $x_{\text{max}} = 0.031 \text{ m}, y_{\text{max}} = 0.04 \text{ m}, l_{1x} = 0.06 \text{ m}, l_{2x} = 2.3, l_{3x} = \pi/124, l_{4x} = \pi/20, l_{1y} = 0.015 \text{ m}, l_{2y} = 1.4, l_{3y} = 3\pi/160.$ 

Fig. 4.10 shows the used area on the optimized mirror in the x-z plane. X coordinates of the targets are -0.015, 0 and 0.015 m. The target range is 0.07 m. Fig. 4.11 shows the used area projected onto the x-y plane in the case where a target exists at the center for a 0.07 m depth.

Since a large part of the echo reflected by the mirror returns to the array, the visual angle of the used area from the target,  $A_{\rm H}$ , is larger than that of a same size array put at the center of the x-y plane,  $A_{\rm DBF}$ . We call the ratio of  $A_{\rm H}$  to  $A_{\rm DBF}$  as the receive efficiency,  $R_{\rm H}$ .

$$R_{\rm H} = A_{\rm H}/A_{\rm DBF}.\tag{4.35}$$

The echo reflected by the used area is received on the array, and thus  $R_{\rm H}$  is close to the SNR improvement of the proposed method from that of a digital beamforming method with the same size array [93]. For example, where a target exists at the center for a depth of 0.07 m,  $R_{\rm H}$  is 6.2. In this case the SNR improvement of the proposed method compared with a digital beamforming method is 7.8 dB, as shown in 'Considerations on signal-to-noise ratio', a subsection in Discussion. Henceforth, we normalize the estimated power at each measuring point to make the peak of it  $R_{\rm H}$  when we calculate the lateral

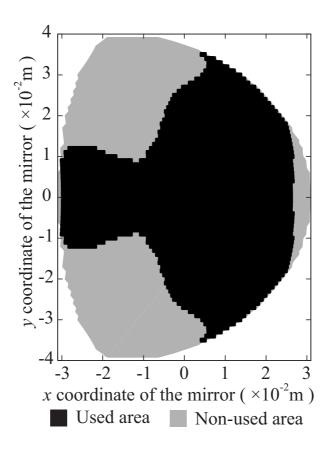


Figure 4.11: The used area on a mirror projected onto the x-y plane where a target exists at the center for a 0.07 m depth.

resolution of the proposed imager.

#### 4.2.4 Sidelobe suppression in image reconstruction

For medical diagnoses, we should decrease the sidelobe levels of the proposed imager. In the proposed method only reflected echoes on the mirror are received on the array. Breaks of the received signal occur at the edge of the mirror and make for a high sidelobe level. While the reflection ratio of the mirror should taper off toward the edge, it is difficult to make such a mirror. Therefore, we employ a tapered reflection ratio for the mirror in image reconstruction from the received signal on the array. Since images are reconstructed from received signals by numerical back projection, the reflection ratio of the mirror can be set freely in image reconstruction. We now investigate the effect of tapering the reflection ratio of the mirror.

The used area on the reflector is distinctive for the target position. Therefore, weight-

ing the reflection ratio of the mirror is useful to reduce the sidelobe level at the cost of some loss of SNR and lateral resolution. Because of the reflection ratio tapering off, the functions 4.17 and 4.24 are changed as follows.

$$\Phi_{T_{b}}(\omega)' = \int_{S} \frac{a_{M} V_{M}' e^{-(\alpha_{1}+jk)r_{2a}' - (\alpha_{2}+jk)r_{2b}'}}{2\pi (r_{2a}' + r_{2b}')} dS, \qquad (4.36)$$

$$P_{\mathrm{T_b}}(t)' = \sum P_{\mathrm{1T_b}} \left\{ t - (r_{2a}' + r_{2b}' + r_{3}')/c_0 \right\}' \frac{r_{3}' \cdot n_{\mathrm{M}}}{r_{3}' n_{\mathrm{M}}} \frac{a_{\mathrm{M}} \Delta S}{(r_{2a}' + r_{2b}')r_{3}'}, \quad (4.37)$$

where  $a_{\rm M}^{2}$  is the reflection ratio of the mirror at the point M in the numerical back projection.

The first sidelobe level of a digital beamforming imager with a dense circular 2-D array is -18.3 dB. Therefore, we set the threshold as -18.3 dB. If the sidelobe level of a measuring direction is higher than the threshold, we use this method to decrease the sidelobe level to less than it.

For a depth of 0.07 m in the x-z section, the first sidelobe level is highest in the case that the x coordinate of a target is 0.015 m. Fig. 4.12 shows the used area on an optimized reflector in such a case. A break occurs in the received signal at the right edge of the mirror, and thus we set the reflection ratio of the mirror to taper off at the right edge, as shown in Fig. 4.13. The visual angle decrease of the used area from the target is -0.18 dB. This means that tapering makes for a slight decrease in the estimated power. Fig. 4.14 shows the lateral resolution of the proposed method with and without tapering. The sidelobe level is suppressed to less than -21 dB at the cost of some slight deterioration of the SNR and lateral resolution.

#### 4.3 Results

In this section, we examine the spatial resolution of the proposed image. First, we compare the spatial resolution of a phased array imager with a liner array to that of the proposed one. When using a linear or convex array for 3-D imaging, the receive beams can be dynamically focused in the section parallel to the longitudinal axis of the array. On the other hand, in the perpendicular section, transmit and receive beams are focused by acoustic lenses. This means that the focal distance is fixed. Fig. 4.15 shows the spatial resolution of a phased array imager in a perpendicular section when the array width is 0.016 m and the focal length is 0.07 m. A target exists at the center for depths of (a) 0.02 m and (b) 0.07 m. If targets exist near the focal zone, spatial resolution is high but spurious images of high amplitude appear in a wide area when the distance between the focal zone and the targets is large, as shown in this figure. This significantly disrupts medical diagnoses.

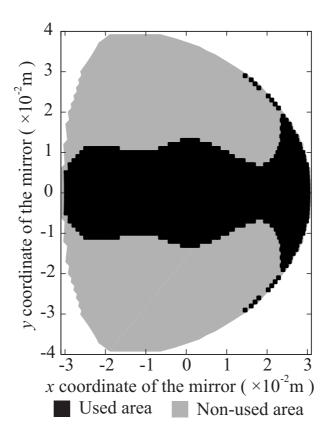


Figure 4.12: The used area on a mirror projected onto the x-y plane where the x coordinate of a target is 0.015 m in the x-z section for a 0.07 m depth.

Fig. 4.16 shows the spatial resolution of the proposed method where the optimized reflector mirror is used. The target ranges are (a) 0.02 m and (b) 0.07 m. In this method, receive beams are dynamically focused to all measuring points and good spatial resolution can be acquired.

Fig. 4.17 shows lateral resolution of the proposed imager with a 0.016 m width array at the range of 0.07 m in the (a) x-z and (b) y-z sections. The x coordinates of targets in the x-z section are -0.03, -0.015, 0, 0.015 and 0.03 m, and the y coordinates in the y-z section are 0, 0.015 and 0.03 m. Sidelobe levels in all these situations are less than -21 dB.

The lateral resolution of y = 0.015 m in the y-z section has swells at y = 0.013 and 0.017 m. This is made by the small used area separated from the main used area, as shown in Fig. 4.18. In the case where images are reconstructed using a taper function to remove the small used area, -3 dB lateral resolution deteriorates slightly and the swells vanish.

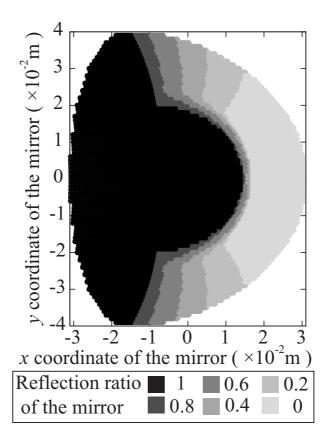


Figure 4.13: The taper function for the reflection ratio on the mirror in numerical back projection.

#### 4.4 Discussion

#### 4.4.1 Evaluation of the radiation pattern

In this session, we compare the spatial resolution of the proposed imaging scheme from that of the digital beamforming method. The x-z and y-z section -3 dB lateral resolutions at the center for a 0.07 m depth are about 1.70  $\lambda$  and 1.41  $\lambda$ , respectively, which is the same as that of a digital beamforming imager with an elliptic array sized 0.041 m long and 0.051 m wide, as shown in Fig. 4.19. Because the elements are spaced at intervals of one-half of a wavelength on the array, the area of the array is proportional to the number of elements. Therefore, the number of elements can be reduced to about 1/8.2 of a dense 2-D array having the same spatial resolution.

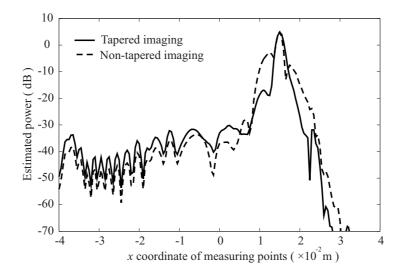


Figure 4.14: Lateral resolution of a tapered and non-tapered proposed imager with a 0.016 m width array in a 3-D problem. The x coordinate of a target is 0.015 m, and those of the measuring points are -0.04 to 0.04 m.

#### 4.4.2 Considerations on signal-to-noise ratio

A common problem for a digital beamforming imager is the low signal-to-noise ratio due to the wide transmit beam. Since this proposed method also uses wide transmit beams, we need to investigate the SNR with this method. In this section we compare the SNR of phased array, digital beamforming and proposed methods.

Noise in an acoustic image is primary determined by uncorrelated electronic noise in the receiver. For this discussion we follow the investigation of Karaman *et al.* [88].

For a phased array imager all transmit pulses are focused and the signal power is proportional to  $N_{\rm t}^2$  at the focal region, where  $N_{\rm t}$  is the number of transmit elements. Assuming uncorrelated noise, a multi-element receiver causes a SNR improvement of  $10 \log(N_{\rm r})$  dB, where  $N_{\rm r}$  is the number of receive elements. Consequently the SNR of a phased array imager, SNR<sub>PA</sub>, satisfies the following equation.

$$SNR_{PA}/SNR_0 = 10 \log(N_t^2 N_r),$$
 (4.38)

where  $SNR_0$  is the SNR of a single-element imager.

For a digital beamforming imager, a defocused multi-element transmitter synthesizes single-element spatial resolution, and the signal power is  $N_{\rm t}$  times that of a single-element transmitter. Consequently the SNR of a synthetic aperture imager, SNR<sub>DBF</sub>, satisfies the following equation.

$$SNR_{DBF}/SNR_0 = 10\log(N_t N_r N_c), \tag{4.39}$$

where  $N_{\rm c}$  is the number of coherently integrated pulses.

For the proposed imager a multi-element transmitter with proper time delay synthesizes a single-element spatial response, similar to a digital beamforming imager with defocusing, and it is expected that the signal power is  $N_{\rm t}$  times as intensive as that of a single element transmitter.  $R_{\rm H}$  is the SNR improvement of the proposed method compared with the digital beam forming method. Because a large part of the echo reflected by the mirror returns to the array, usually  $R_{\rm H}$  is larger than 1. We further define  $P_{\rm H}$ ,  $P_{\rm l}$ , and  $b_{\rm l}$ , satisfying the following expression.

$$P_{\rm H}l = \sqrt{R_{\rm H}b_l}P_lD_{\rm t}D_{\rm r},\tag{4.40}$$

where  $P_{\mathrm{H}l}$  is the received signal amplitude in the proposed method,  $P_l$  is that in the digital beamforming method, and  $b_l$  is a coefficient.  $D_{\mathrm{t}}$  and  $D_{\mathrm{r}}$  are caused by the attenuation through the impedance matching fluid at the transmit and receive phase. Since the power summation of received signals is proportional to the power of returned echoes, the following expressions are given.

$$W_{\rm H} \propto \sum_{l} P_{\rm H}l^2 = R_{\rm H} \sum_{l} (b_l P_l^2) D_{\rm t}^2 D_{\rm r}^2,$$
 (4.41)

$$W_{\rm DBF} \propto \sum_{l} P_l^2.$$
 (4.42)

The coefficient  $b_l$  satisfies the following equation.

$$\sum_{l} (b_l P_l^2) = \sum_{l} P_l^2. \tag{4.43}$$

Because of reconstruction based on numerical back projection, the estimated signal amplitude,  $S_{\rm HA}$ , is given by

$$S_{\rm HA} \propto \sum_{l} (\sqrt{R_{\rm H} b_l} P_{\rm H} l) e^{-2\alpha_1(r_{\rm 0a} + r_{\rm 0b})},$$
 (4.44)

where we introduce the approximation that  $D_{\rm t} = D_{\rm r} = e^{-\alpha_1(r_{0a} + r_{0b})}$ .

The estimated signal power,  $S_{\rm HP}$ , satisfies the following equation.

$$S_{\rm HA} \propto R_{\rm H}^2 (\sum_l P_l)^2 e^{-4\alpha_1(r_{\rm 0a} + r_{\rm 0b})}.$$
 (4.45)

Assuming uncorrelated noise, the SNR of the proposed imager, SNR<sub>H</sub>, is given by the relation

$$SNR_{H}/SNR_{0} = 10 \log(N_{t}N_{r}R_{H}N_{c}e^{-4\alpha_{1}(r_{0a}+r_{0b})}). \tag{4.46}$$

For example, with an 800-element array ( $N_{\rm t}=N_{\rm r}=800$ ), the impedance matching fluid is water ( $\alpha_1=2.0(\omega/2\pi)^2\times 10^{-14}~{\rm Np/m}$ ),  $r_{\rm 0a}+r_{\rm 0b}=0.085$  m, if the receive

efficiency  $R_{\rm H}$  is 6.2, and the number of coherently integrated pulses  $N_{\rm c}$  is 260, a proposed imager realizes the following SNR.

$$SNR_{H}/SNR_{SA} = 7.8 [dB], \qquad (4.47)$$

$$SNR_{H}/SNR_{PA} = 3.0 [dB]. \tag{4.48}$$

In this case 3-D images can be acquired at the rate of 19 3-D images/s. In the case of the impedance matching fluid being ultrasound jelly, the SNR improvements are 6.7 and 1.9 dB, respectively.

For cardiology, higher time resolution is needed. Assuming a heart rate of 80 beats/min and a moving distance in a beat cycle of 0.02 m, the maximum speed is about 0.04 m/s. To improve the SNR we can use coherent integration when the target moves 1/4 of a wavelength. Where that wavelength is 0.001 m, the maximum coherent integration time is 1/160 second; in other words,  $N_{\rm c}=30$ . This means that more than 160 images/s are needed to measure the heart when the wavelength is less than 0.001 m. The proposed scheme is suited for such purposes.

#### 4.5 Conclusion

For a high resolution acoustic real-time 3-D imaging system, we proposed a system based on a hybrid method with a reflector mirror and a small dense array. Utilizing this scheme, images of the whole measuring area can be reconstructed from a single transmit and receive event; so enabling real-time 3-D imaging. Receiving a large part of the echo focused by the mirror has the same effect as using a large array. This method realizes lateral resolutions of 1.70  $\lambda$  in the x-z and 1.41  $\lambda$  in the y-z sections for a depth of 0.07 m, where the center frequency is 1.6 MHz, the width of the reflector is 0.062 m long and 0.08 m wide, and the array is a circle 0.016 m in diameter. This shows that the number of elements can be reduced to about 1/8.2 of a dense 2-D array having the same spatial resolution but using a digital beamforming method. Because we make the reflection ratio of the mirror taper off in the numerical back projection, the sidelobe level is suppressed to less than -21 dB. The maximum theoretical frame rate is 5000 frames/s, when the SNR is sufficiently high. Since the transmit beam is synthesized by all elements on the array, a sufficiently high SNR is achieved. In cases where the frame rate is 19 images/s, the SNR improvements compared to a conventional phased array method and a digital beamforming method with defocusing are 3.0 dB and 7.8 dB, respectively.

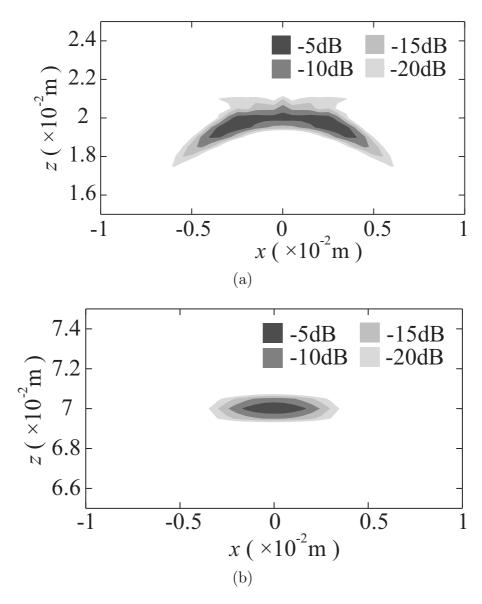


Figure 4.15: Spatial resolution of a phased array imager with a 1-D array. The focal length of the acoustic lenses is 0.07 m, and the targets exist at the center for depths of (a) 0.02 m and (b) 0.07 m. This section is perpendicular to the longitudinal axis of the linear array.

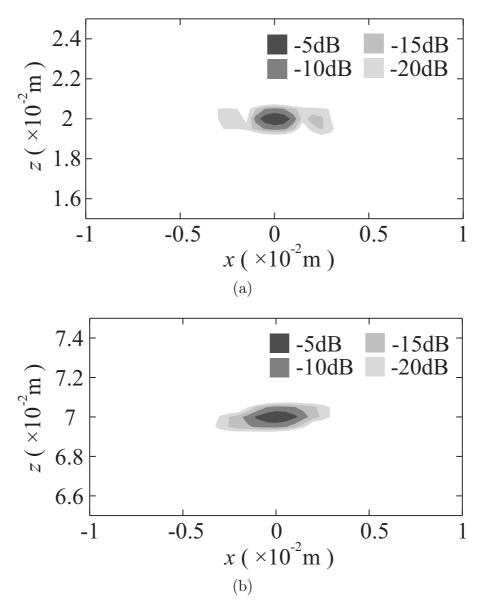


Figure 4.16: Spatial resolution of the proposed imager in the x-z section. Targets exist at the center for depths of (a) 0.02 m and (b) 0.07 m.

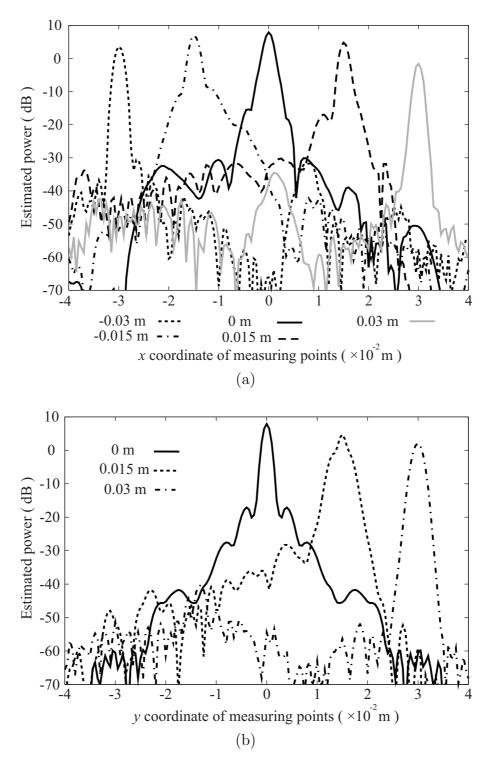


Figure 4.17: Lateral resolution of the proposed imager with a 0.016 m width array in the (a) x-z and (b) y-z sections for a 0.07 m depth. (a) X coordinates of targets are -0.03, -0.015, 0, 0.015 and 0.03 m. (b) Y coordinates of targets are 0, 0.015 and 0.03 m.

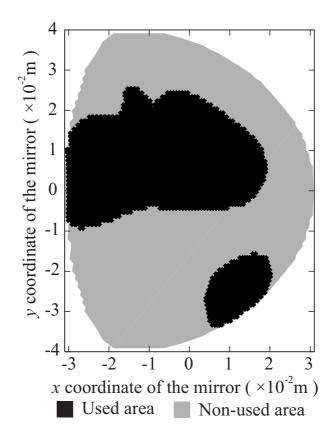


Figure 4.18: The used area on a mirror projected onto the x-y plane where the y coordinate of a target is 0.015 m in the y-z section for a 0.07 m depth.

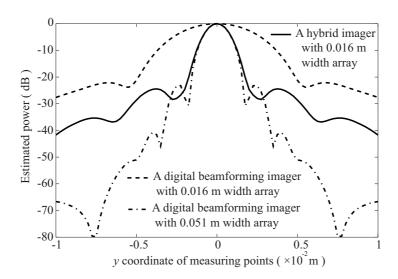


Figure 4.19: Lateral resolution of the proposed imager with a 0.016 m width array and digital beamforming imagers with 0.016 m and 0.051 m width arrays. A target exists at the center for a 0.07 m depth.

### Chapter 5

# Transfer Information Enhancement with a 2-D Tactile Stimulator Array for an Acoustic Vision Substitute System

#### 5.1 Introduction

Many researchers have investigated human machine information transfer methods through tactile excitation. Often, a 2-D stimulator array is used in a vision substitute system [94]-[98]. Previous research has been directed to converting visual images to vibrotactile or electrotactile excitation, and thus excitation intensity does not correspond to the range of the target in these methods. For target range detection, a user needs to memorize the shape of the target. Then the user identifies the target and compares the presented information with the memorized shape. Therefore, it is difficult to recognize the location of plural targets with different ranges, because of the difficulty for memory of the plural target shapes and identification of them.

It is expected that early blind have a quite different recognition way of spatial information from late blind, and thus it is difficult to design a vision substitute system for both early and late blind. In recent years Japan rapidly turns into aging society and the occurrence of diabetes increases. Therefore the number of late blind will increase because of senile macular degeneration and diabetic retinopathy. Hence, we direct to a vision substitute system for late totally blind. For acquiring information from visual environments with plural targets, existing vision substitute systems need to improve their angular and range resolutions. The goal of this study is to develop an efficient system for presenting environmental information. To provide environmental information with a portable instrument, we have proposed an acoustic vision substitute system based on a hybrid array-reflector configuration that realizes high time and spatial resolutions with

just a modest computational load [99]. Fig. 5.1 shows the schematic view of our vision substitute system in which a broad transmit beam is radiated over the entire measurement area. The reflected echo is first focused by a concave reflector, and then received by the 2-D sensor array. Images are reconstructed from the widely distributed signals received on the array by numerical back projection. With this method, one transmit and receive event can make a 3-D image of the whole measurement area. This system realizes 34 images/s in the case that the measurement range is 5 m.

We propose that spatial information, measured by the acoustic sensor, is presented by a 2-D tactile display placed on the forehead. Auditory sense is one of the most important information for the blind. Mounting a stimulating device on a hand or an arm prevents a user from moving freely. Of all body regions on which we could mount a stimulating instrument without an obstruction, the forehead has a low two-point discrimination threshold and wide stimulating area. Thus we determined the stimulation region should be the forehead. As well, the forward direction of the face corresponds to the center direction of the measurement area. Therefore, for late totally blind, recognizing target directions is relatively easy.

This paper has two purposes. The first is the angular resolution improvement of transfer information to provide sufficient environmental information. The second is to transfer the target ranges exactly for the distinction of plural targets at different ranges. So that each stimulator individually transfers different information, the stimulators in the array are spaced at intervals of the two-point discrimination threshold [100]-[102]. This restricts the number of stimulators that transfer information through a certain area. In this paper we propose two methods to improve angular resolution and transfer target range. The methods employ a 2-D stimulator array having stimulators spaced at intervals of less than the length of the simultaneous two-point discrimination threshold to increase the number of stimulators. Since two stimulators adjoined to each other work with a certain stimulus onset asynchrony (SOA), they can separately transfer different information. Furthermore a user selects the measurement range and the system proposes targets within the range to the user. By selecting from a short range to a long range, the user can acquire spatial information of the entire target area. Since the user knows the measurement range, the range of the targets can be accurately recognized. Here, we investigate these methods experimentally, and confirm their effectiveness.

In section 2, we propose two methods, an alternating stimulation method and a voluntary range selection method. We then explain the instrument used in the experiment and the content of the experiment. In section 3, we evaluate the experimental results. Finally, conclusions are drawn in section 4.

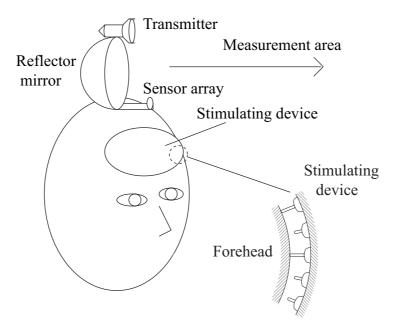


Figure 5.1: Schematic view of the acoustic vision substitute system.

#### 5.2 Methods

#### 5.2.1 Alternating stimulation method

This system uses a 2-D stimulator array as a stimulating device. The stimulator spacing should be more than the two-point discrimination threshold so that each stimulator transfers different information to the user. Since this restricts the number of stimulators constituting a 2-D stimulator array, it is difficult to transfer enough information to a user for the vision substitute system. We propose an alternating stimulation method to gain transfer information by increasing the number of stimulators. In this method stimulators in a 2-D array are divided into several groups. Fig. 5.2 shows examples of the stimulators divided into two and four groups. Stimulators that belong to a group move synchronously and each stimulator group is activated alternately. Stimulators within a group are spaced at intervals of the two-point discrimination threshold. However, the interval of two stimulators that adjoin each other is less than the interval of the two-point discrimination threshold. Since they belong to different groups, there is a SOA between two stimulations. In this case, the two stimulations are perceived individually under the condition that the stimulator spacing is about 1/3 of the two-point discrimination threshold [101]. In the case of the two examples shown in Fig. 5.2, the intervals of the stimulators adjoining each other are respectively 0.71 and 0.5 of the two-point discrimination threshold. Therefore, if the stimulator spacing of the same group is set to the two-point discrimination

threshold, stimulations can individually transfer different information. This means that the number of stimulators can be increased to 2 or 4 times that in a 2-D array spaced at an interval of the two-point discrimination threshold. Thus the spatial information presented in this method is improved to 2 or 4 times that in the simultaneous stimulation one.

#### 5.2.2 Voluntary range selection

To distinguish multiple targets, we need to present the direction and range of targets. The proposed system presents the direction of a target by stimulating the location on the forehead. The subject can then recognize the range of targets as follows.

Fig. 5.3 shows a schematic view of targets in the measurement area. Fig. 5.4 is the projection image of targets to the measurement area. The range of targets A, B is less than  $d_1$ , and that of C, D is between  $d_1$  and  $d_2$ . Since a target with a shorter range is more important, the target of the shortest range is displayed in the case where plural targets exist in the same direction.

First, a user determines the measurement range of  $d_1$  and gives instructions to the vision substitute system. We suppose the instruction is given by a brain switch [103], a biting force switch, a voice switch, or a kind of contact switch. In future we will examine these various switch types and select the best. The system presents directions of targets A, B by vibrotactile excitation on the forehead. Fig. 5.5 shows stimulating points matched with targets in the case of the measurement range of  $d_1$ . From the stimulating position presented by this system, the user can recognize the size and direction of the targets.

Second, the user gives the instruction regarding the measurement range of  $d_2$  to the system, and it presents the directions of targets A, B, C, D. Fig. 5.6 shows stimulating points matched with targets when the measurement range is  $d_2$ . From the changes in the information displayed the user recognizes that the range of targets C, D is between  $d_1$  and  $d_2$ . By measuring from a short to a long range, the user acquires spatial information of the entire target area.

For identifying objects on a table, there is no need to measure targets with a long range; therefore, a user fixes the measurement range as a short one. Then the interval of each radiation time becomes shorter in the case that a transmitter radiates after the echo from the longest range is received. This allows an improvement in the time resolution. For long range detection, the user can memorize the range of targets from a single detection of the whole measurement area. Then the user can fix the measurement range as a long one, after measuring from the short range to a long one. When the measurement range is 5 m, the time resolution of the system is about 0.03 second, which means that it can deal with pedestrian movement.

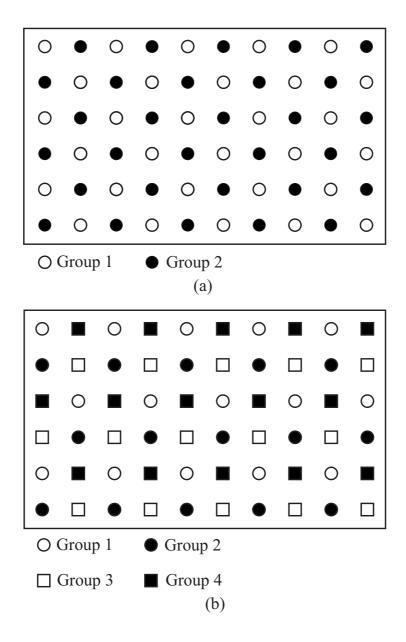


Figure 5.2: Division of stimulators that are components of a 2-D array stimulating device placed on the forehead. Stimulators are divided into (a) two and (b) four groups. Stimulators that belong to a group move synchronously and stimulator groups are activated alternately.

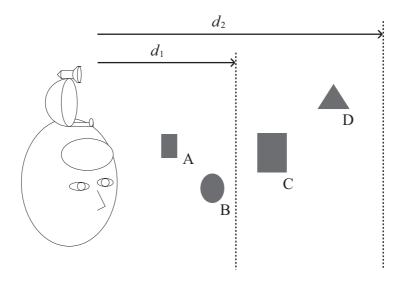


Figure 5.3: Schematic view of targets in the measurement area.

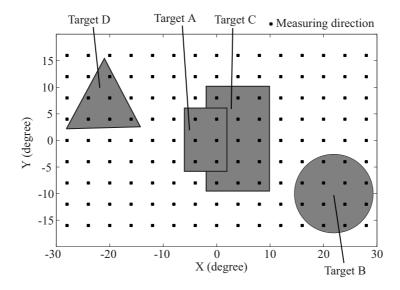


Figure 5.4: Directions of targets in the measurement area.

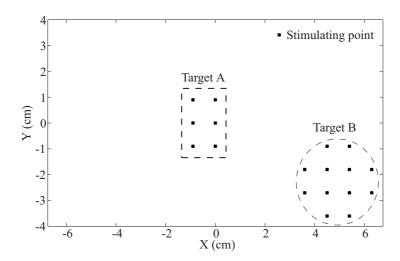


Figure 5.5: Stimulating points matched with targets when the measuring range is  $d_1$ .

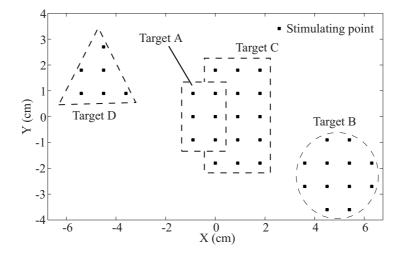


Figure 5.6: Stimulating points matched with targets when the measurement range is  $d_2$ .

#### 5.2.3 Overview of the experiment

We examine the alternating stimulation and the voluntary range selection methods experimentally using a 2-D solenoid array consisting of a 2 x 4 arrangement with two dummy solenoids placed at the left and right side of the array, as shown in Fig. 5.7. The two solenoids placed at both sides always generate sound and vibration, to prevent participants distinguishing tactile patterns by sound. The protuberances, placed at both edges of the array, restrain the stimulation rods from pushing hard against the forehead. When employing the simultaneous stimulation method, the active stimulators work synchronously. When employing the alternating stimulation method, the stimulators in the 2-D array are divided into two groups, as shown in Fig. 5.8. Each stimulation group is activated alternately. With this proposed stimulation method, a couple of stimulation sets present single spatial information. To correspond the power consumption of the dummy solenoids between the two stimulation methods, the left side dummy solenoid belongs to group 1 and the right side to group 2. We first compare the perceived stimulus quality of the alternating stimulation to that of simultaneous stimulation. We then investigate the exactitude of transferring range information of targets using a voluntary range selection method. We suppose that the user gives instructions to the system for a short to a long range. Since the target with a longer range is presented later, the stimulation points increase within a stimulation set.

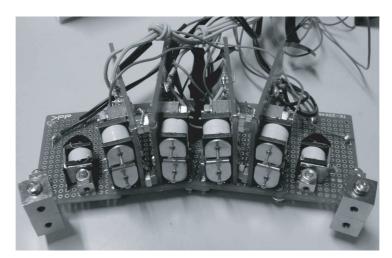


Figure 5.7: Solenoid array placed on participants 'foreheads. The 2  $\times$  4 solenoids placed at the center of the array are the stimulators. The two solenoids placed at the sides always generate sound and vibration to prevent participants from distinguishing tactile patterns by sound.

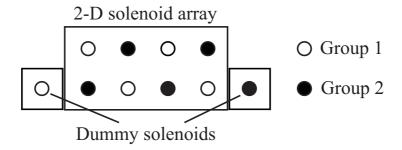


Figure 5.8: An arrangement of stimulators divided into two groups when employing the alternating stimulation method.

#### 5.2.4 Vibrotactile stimuli

In this study, we use a solenoid array as the stimulating device. Each solenoid has a round-topped vibrating rod, as shown in Fig. 5.9. As shown in [102], the two-point discrimination threshold at the forehead is 0.9 cm to 1.5 cm. It is assumed from the Loomis 's study [104], that the localization error at the forehead is about 1/4 of the two-point discrimination threshold. Since we assume that the stimulator spacing is about two-point discrimination threshold for transferring information accurately, the tops of the vibrating rods are spaced at intervals of 1.3 cm vertically and 1.5 cm horizontally. A participant places the array on his forehead and responds to the tactile pattern presented by the array. Rectangular pulses are delivered to activate solenoids, which contain two dummy solenoids. The voltage delivered to a solenoid is 3 V. Its pressure, dependent on the stroke of the stimulation rod, is 1 to 2.5 gf.

To provide fine spatial information, it is necessary to stimulate the skin tactile receptors with high spatial resolution. The skin deform threshold of the receptor should be low for the stimulators to have a low power consumption. Since a Meissner 's corpuscle has both high spatial resolution and low skin deform threshold [96], we decided to activate Meissner 's corpuscles. Their most sensitive frequency is 20 to 40 Hz; so we set the stimulating frequency at 30 Hz. Fig. 5.10 shows the waveforms used in this experiment. The interval of pulse onsets is 33.3 ms (pulse repetition rate is 30 Hz) and pulse width is half of the interval. We follow Y. Shimizu [105], and set the duration of the stimulation and SOA at 200 and 800 ms, respectively; that is, the burst onset is separated by 800 ms and each burst contains 6 pulses.

A phantom sensation occurs under certain conditions of SOA, stimulator spacing and stimulation pressure. Such as when two stimulators that adjoin each other can not individually transfer different information. To prevent a phantom sensation, in the alternating stimulation trials we set the SOA and the duration of stimulation as 400 ms and 200 ms, respectively. We also set both types of trials to have the same power consumption as follows.

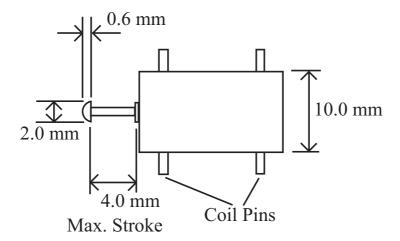


Figure 5.9: Schema of a solenoid component in the 2-D stimulator array placed on the forehead.

In the simultaneous stimulation trials, the waveform in Fig. 5.10 is delivered to all active solenoids. The tactile patterns used in these trials are 1-point stimulations and 4-point square stimulations, as shown in Fig. 5.11. The 1-point stimulations are presented at one of the 8 positions. The 4-point stimulations are presented simultaneously at one of three positions; left, middle, and right. In the alternating stimulation trials, the waveforms in Fig. 5.12 -(1) and 5.12 -(2) are delivered to the active solenoids of groups 1 and 2, respectively. The tactile patterns used in these trials are the same as those in the simultaneous trials. Each 4-point square stimulation is presented by two pairs of stimulators that are activated alternately, as shown in Fig. 5.13. A 1-point stimulation is presented in the same way as that in the simultaneous stimulation trials, except for the activation of the dummy solenoids.

In the alternating stimulation method experiment, the presentation time of each pattern is 5 s, which contains 6 bursts of voltage delivered to the solenoids. Since the receptive field of a Meissner 's corpuscle is 12.6 mm² [96], the influence of an individual stimulation over an adjacent stimulation point is neglectable. Both trials in this experiment have the same SOA, and therefore there is no difference between any influences from the adaptation in the two trials. This indicates that in the comparison between the simultaneous and alternating stimulation trials it is not necessary to evaluate the influence of the adaptation. The interval between two presentation times is 5 s, and at that time a participant responds to the presented pattern.

In the voluntary range selection method experiment, we assume that the measurement range has 5 phases. Two targets represented as 4-point square stimulations exist at the right and left in different ranges, and a user measures from a short to a long range. Here, these targets are presented one after the other, as shown in Fig. 5.14. The presentation

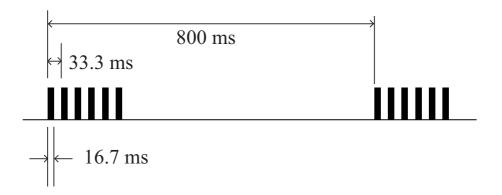


Figure 5.10: Stimulus waveform in the simultaneous stimulation trials. Pulse repetition rate is 30 Hz and pulse width is half of the pulse onset interval. Each burst has 6 pulses and burst onset interval is 800 ms.

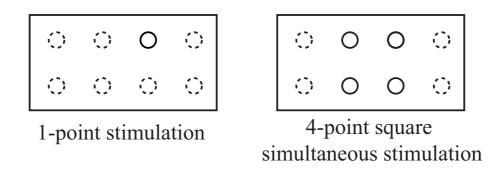


Figure 5.11: Tactile patterns in the simultaneous stimulation trials. The 1-point stimulations are presented at one of the 8 positions. The 4-point stimulations are presented simultaneously at one of the three positions; left, middle, and right.

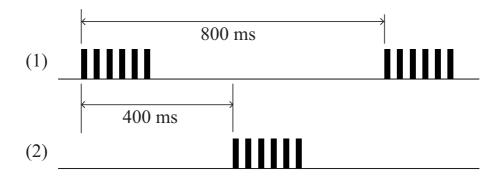


Figure 5.12: Stimulus waveform in the alternating stimulation trials. Waveforms (1) and (2) are delivered to the active solenoids of groups 1 and 2, respectively. Stimulus onset asynchrony between the two groups is 400ms.

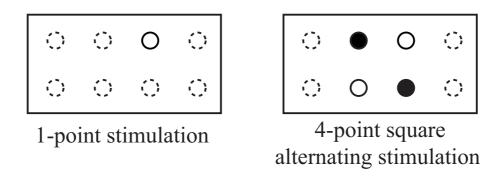


Figure 5.13: Tactile patterns in the alternating stimulation trials. The 4-point stimulations consist of two stimulation groups.

time for each stimulation set is  $25 \, \mathrm{s}$ , and contains  $5 \, \mathrm{stimulation}$  patterns. In this experiment, we use the alternating stimulation method and set the interval between the two presentation times as  $5 \, \mathrm{s}$ .

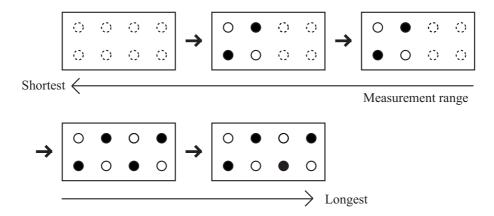


Figure 5.14: Tactile patterns in the voluntary range selection trials. Two targets, represented as 4-point square stimulations, are presented one after the other.

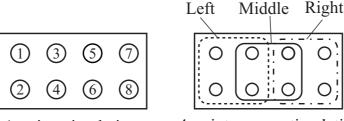
#### 5.2.5 Participants

Six healthy males (21-28 years old) participated in this experiment. Participants provided informed consent and wiped their forehead before the start of the experiment. In the experiments, participants opened their eyes and inserted earplugs. We checked the contact between stimulation rods and the forehead before and after each experiment. All participants underwent the experimental procedures.

#### 5.2.6 Main experiment

We number the solenoids from 1 to 8, as shown in Fig. 5.15. A 1-point stimulation is presented by activating one of the eight solenoids. A 4-point stimulation is presented at left, middle, or right position by four activated solenoids, as shown in Fig. 5.15. We call these stimulations as 1-8, left, middle, and right. A participant responds to the stimulations with the names, as shown in Table 5.1. If a participant perceives a 1-point pattern, he responds one of the 8 number; 1-8. If he perceives a 4-point pattern, he selects one of the three choices; left, middle, or right.

The alternating stimulation method experiment consists of two practical trials followed by two experimental ones. The first practical trial employs simultaneous stimulations, and the second alternating ones. In the practical trial, the stimulations of 1 to 8, left, middle and right are presented in that order. Participants are informed about the names



1-point stimulation 4-point square stimulation

Figure 5.15: Solenoid numbers and activated solenoid groups of the 4-point stimulation. A 1-point stimulation is presented by activating one of the eight solenoids. A 4-point stimulation is presented at left, middle, or right position by four activated solenoids. Thus these stimulations are named 1-8, left, middle, and right.

Table 5.1: Variety of responses in the alternating stimulation method experiment. If a participant perceives a 1-point pattern, he responds with one of the 8 numbers; 1-8. If he perceives a 4-point pattern, he selects one of the three choices; left, middle, or right.

Perception	Response
1-point pattern	1 to 8
4-point pattern	Left, Middle, Right

of the stimulations presented and practice to become accustomed to the stimulations. This practice cycle is presented twice, and then each practical trial consists of 16 1-point stimulations and 6 4-point stimulations. Each experimental trial consists of 12 1-point stimulations and 12 4-point stimulations. The arrangement on the array and the order of these tactile patterns are random. In the experimental trials, participants respond to the stimulations with the names, as shown in Table 5.1. The first experimental trial employs simultaneous stimulations and the second alternating stimulations, similar to in the practical trials.

The voluntary range selection method experiment consists of one practical trial followed by an experimental one. The practical trial and the experimental one have 8 and 12 stimulation sets, respectively. The two 4-point stimulations of these 20 stimulation sets are presented randomly. Similarly to the alternating stimulation method experiment, in the practical trial participants are informed about the presented patterns and practice to become accustomed to these stimulation patterns. In the experimental trial they respond with the directions and the starting times of two 4-point stimulations. In this experiment we employ the alternating stimulation method.

#### 5.3 Results

In the alternating stimulation method experiment, a participant responds with the pattern and position of the stimulation. There is a distance between the position of the stimulation and that of the response when the response to the stimulation pattern is correct. We evaluate the possibility that the distance, between the position of the stimulation and that of the response, is a certain distance when a 1-point stimulation is presented and the response being 1-point pattern. We define the possibility as the number of each distance over the total number of the responses being a 1-point pattern. The distance variation is 8 as follows; 0, 1.3, 1.5, 2.0, 2.6, 3.0, 3.9, and 4.2 cm. Therefore we define  $L_0$  as the interval of the stimulation rods, and then classify the 8 distances to 4 grades; 0,  $L_0$ ,  $\sqrt{2}L_0$ , and  $2L_0$  or over. Table 5.2 shows the average and the standard deviation of the possibility. The possibility of the distance being 0 or  $L_0$  is almost 1, and the possibility of the distance being  $2L_0$  or over is almost nil. This indicates that we can neglect the probability of false positives.

Table 5.2: The average and the standard deviation of the possibility that the distance between the position of the stimulation and that of the response is each value when a 1-point stimulation is presented and the pattern of the response is correct. The average is written in the upper line of each cell, and the standard deviation with vinculum in the lower line.

Distance	0	$L_0$	$\sqrt{2}L_0$	$2 L_0 \leq$
Simultaneous	0.437	0.469	0.0787	0.0152
stimulation	(0.117)	(0.173)	(0.091)	(0.034)
Alternating	0.518	0.408	0.0602	0.0139
stimulation	(0.305)	(0.278)	(0.065)	( 0.031 )

Table 5.3 shows the definitions of the variables used in the evaluation of the alternating stimulation method. Their values are the numbers of the responses in the experiment. Table 5.4 shows the average and the standard deviation of the possibilities that the response is correct or not correct when the response is a 4-point pattern. The possibilities for 4-point and 1-point stimulations are defined simply as  $a_{22}/(a_{21} + a_{22} + a_{23})$  and  $a_{12}/(a_{11} + a_{12} + a_{13})$ , respectively. This result shows the effectiveness of the proposed alternating stimulation method for enhancing transfer of information with p < 0.01. We introduce the assumption that the possibility follows a normal distribution and use a t-examination.

Furthermore, the interpretation of a no signal response is as follows. Since the false positive probability can be neglected, a bad contact between a stimulator and the forehead causes a no signal response. For future work we need to improve the stimulation

Table 5.3: Definition of the variables used in the evaluation of the alternating stimulation method. Their values are the numbers of the sensation responded to in the experiment.

	Response		
	1-point	4-point pattern	No
	pattern	pattern	pattern
1-point stimulation	$a_{11}$	$a_{12}$	$a_{13}$
4-point stimulation	$a_{21}$	$a_{22}$	$a_{23}$

Table 5.4: The average and the standard deviation of the possibilities that the response is correct or not correct when the response is a 4-point pattern, The possibilities for 4-point and 1-point stimulations are defined simply as  $a_{22}/(a_{21}+a_{22}+a_{23})$  and  $a_{12}/(a_{11}+a_{12}+a_{13})$ , respectively.

	The possibility of a 4-point pattern response		
	4-point stimulation	1-point stimulation	
Simultaneous	0.556	0.0278	
stimulation	(0.190)	(0.0393)	
Alternating	0.861	0.0417	
stimulation	(0.150)	(0.0636)	

instrument to prevent any bad contacts. The probability of a bad contact between a stimulator and the forehead,  $p_{BC}$ , satisfies

$$p_{\rm BC} = a_{13}/(a_{11} + a_{12} + a_{13}). (5.1)$$

To revise the possibility that the response is correct when a tactile pattern is a 4-point square stimulation, we treat the result statistically. The number of 4-point square stimulations becoming 1-point stimulations because of a bad contact between stimulators and the forehead,  $b_1$ , satisfies

$$b_1 = 4(a_{21} + a_{22} + a_{23})p_{BC}^3(1 - p_{BC}). (5.2)$$

In this interpretation, the possibility that a 4-point square stimulation becomes a no stimulation,  $p_{\rm BC}^4$ , is less than 0.2 %. This is consistent with the result that in all experimental trials  $a_{23}=0$ . In this interpretation we define the correct response as a 4-point pattern response when a multiple-point stimulation is presented for a 4-point stimulation. The number of multiple-point stimulations presented is given by  $a_{21}+a_{22}-b_1$ . We remove the superficially correct occasion that the a participant mistakes and responds

with a 4-point pattern when a 1-point stimulation is presented because of a bad contact in the case of a 4-point stimulation. The number of occasions that this happens is given by

$$b_2 = b_1 a_{12} / (a_{11} + a_{12}). (5.3)$$

Therefore the possibilities of a 4-point response when a 4-point stimulation and a 1-point stimulation are presented,  $p_{44}$  and  $p_{14}$ , satisfy

$$p_{44} = (a_{22} - b_2)/(a_{21} + a_{22} - b_1), (5.4)$$

$$p_{14} = a_{12}/(a_{11} + a_{12}). (5.5)$$

Fig. 5.16 shows the average of the possibilities,  $p_{44}$  and  $p_{14}$ , including the 2 standard deviation error bar. The result shows the effectiveness of the proposed alternating stimulation method for enhancing transfer of information with p < 0.025. We also introduce the assumption that the possibility follows a normal distribution and use a t-examination.

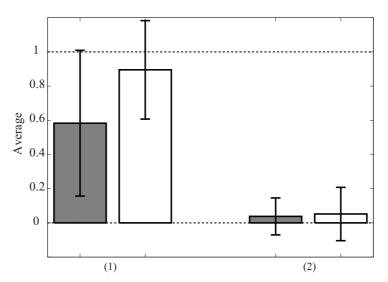


Figure 5.16: The average of the possibilities that (1) the response is correct or (2) not correct when the response is a 4-point pattern for the interpretation of the perception of no signal, including the 2 standard deviation error bar. Colored bars are those of the simultaneous stimulation; white bars are of the proposed alternating stimulation.

In this experiment we can reject cases in which a participant used auditory information caused by bone conduction, as follows. First, SOAs of the vibration sound are fixed at 800 and 400 ms in the simultaneous and alternating trials, respectively. It is then necessary

for a participant to distinguish the intensity of the vibration sound to make the correct response. In the simultaneous trials, 3 or 6 solenoids generate the vibration sound, and then the intensity variation of the sound is generated by 3 solenoids. In the alternating trials, 1, 2 or 3 solenoids generate the vibration sound, and then the maximum variation of the sound is generated by 2 solenoids. This indicates that if a participant utilizes auditory information, the participant distinguishes the two stimulation patterns in the simultaneous stimulation trials more easily than in the alternating stimulation trials. This is contradictory to the results of this experiment. Therefore, we reject the possibility that a participant used auditory information in this experiment.

Table 5.5 shows the average and the standard deviation of the possibilities that the response is correct in the voluntary range selection method experiment. The possibilities for direction and range are defined respectively as the numbers of the responses where target direction and range are correct over that of all responses. This result shows that range information is almost exactly transferred using the proposed method.

Table 5.5: The average and the standard deviation of the possibility that the response is correct when a tactile pattern is a 4-point square stimulation.

	Average	Standard deviation
Direction	0.958	$4.05 \times 10^{-3}$
Range	0.979	$1.01 \times 10^{-3}$

#### 5.4 Conclusion

For the stimulating device to be utilized in our acoustic vision substitute system, we propose two information transfer methods that use a 2-D stimulator array. In the alternating stimulation method, stimulators are divided into several groups, and each stimulator group is activated alternately. Since two stimulators that adjoin each other belong to different groups, there is a certain SOA between two stimulations. In this case the two stimulations are perceived individually under the condition that the stimulator spacing is about 1/3 of the two-point discrimination threshold. When the stimulators are divided into two and four groups, the intervals of the stimulators adjoining each other are 0.71 and 0.5, respectively, of the two-point discrimination threshold. Therefore if the stimulator spacing of the same group is the two-point discrimination threshold, stimulations can individually transfer different information. This means that the number of stimulators can be increased to 2 or 4 times that in a 2-D array spaced at intervals of the two-point discrimination threshold. Then the spatial information presented in this method is improved to 2 or 4 times that of the simultaneous stimulation method. With the voluntary

range selection method, a user selects the measurement range and targets within the range are presented to the user. By selecting from a short to a long range the user acquires spatial information of the entire measurement area. Since the user knows the measurement range, the target ranges can be accurately recognized. We experimentally compare the alternate stimulation and the simultaneous stimulation methods and confirm that the former method is more useful to transfer information to a user. We also experimentally investigate the voluntary range selection method and show that a user can accurately recognize target ranges.

In future work we need to miniaturize this system to make a portable instrument. It will be necessary to reduce power consumption and select proper stimulation devices. To reduce power consumption we need to optimize the duration of the stimulation, SOA, the intensity of the stimulation, and the stimulation waveform. Here, we did not utilize intensity modulation of the stimulation for information presentation. The intensity modulation of stimulation can present other spatial information, such as the echo power from the target. This indicates that this method has the potential to clearly present environmental information.

### Chapter 6

# Improvement of the Spatial Resolution of a 3-D Acoustic Medical Imaging System Based on Hybrid Method Using Synthetic Aperture Technique

#### 6.1 Introduction

A volumetric 3-D real-time high-resolution acoustic imaging system is needed for medical diagnosis. A 3-D imager that employs a linear array measures one target plane at a time, and then moves mechanically for 3-D imaging [106][107]. However, this method has insufficient time resolution for the medical examination of a fast-moving organ such as the heart. The use of acoustic lenses on the elements to focus the transmit and receive beams to a target plane results in serious deterioration in spatial resolution both in front of and behind the focus. A digital beamforming imager that incorporates a 2-D array enables measurement of the entire target field as a single transmit and receive event. This system, therefore, has high time resolution; however, the number of elements on the 2-D array is enormous and the signal-to-noise ratio (SNR) is low [108]-[110]. Though a myocardial motion imager is useful for medical diagnoses [111], it has insufficient lateral resolution.

We proposed a system based on a hybrid array-refrector configuration, shown in Fig. 6.1 [112]-[114]. This system employs a wide transmit beam that is radiated over the entire measurement field. The angular resolution and SNR of the proposed method are improvements over those of a digital beamforming imager with a similarly-sized 2-D array. This is because in the current method most of the echo reflected by the mirror is gathered to the array.

In this paper, we propose a method for the improvement of the spatial resolution of

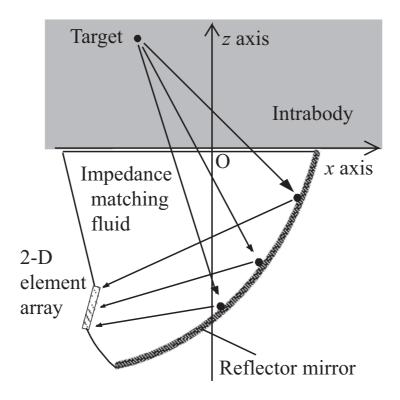


Figure 6.1: Schematic view of the system in the receive phase.

a 3-D acoustic medical imaging system based on a hybrid method that uses a synthetic aperture technique. Since a 3-D imager based on a hybrid method aquires a 3-D image as single transmit and receive event, the image reconstruction from multiple transmit and receive events realizes sufficient time resolution to measure a fast moving organ such as a heart.

In section 2, we outline the framework of the 3-D acoustic imaging system based on the hybrid method. The parameters for calculating spatial resolution are set out in section 3. In the proposed imager all elements on the 2-D array radiate ultrasound pulses at proper time delays for synthesizing a wide transmit beam. In section 4, we propose a method to employ proper time delays. The radiation pattern of the transmit beam is calculated in section 5. In section 6, we evaluate the effect of the coherent integration of multiple transmit and receive events on the improvements in spatial resolution of the proposed method. In section 7, we examine the spatial resolution of the proposed imager in the case that the time resolution is 300 3-D images/s. Finally, we draw conclusions.

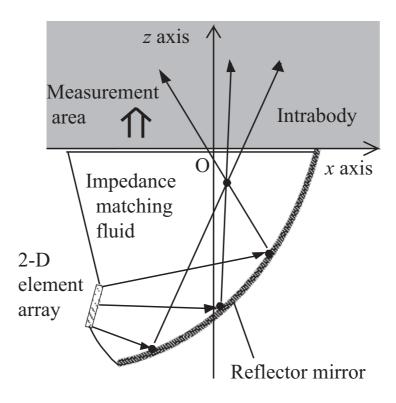


Figure 6.2: Schematic view of the system in the transmit phase.

# 6.2 Formation of the transmit beam using a focusing method

With this method, a transmit beam is radiated over the entire measurement field before any echoes from the targets are received on the 2-D array. The image of the target is reconstructed from the received signals using numerical back-projection. The image reconstruction based on numerical back-projection is processed as follows: the phase of the received signal is reversed before being projected backward from the receive point. The waves projected backward are focused at the target points.

To measure the entire target field as a single transmit and receive event, the transmit beam must be radiated sufficiently widely over the target field. As well, high transmit power is desirable to improve the SNR. A method to form a wide transmit beam is shown in [114]. Fig. 6.2 is a schematic view of the proposed imager in the transmit phase. All elements on the array radiate ultrasound pulses at appropriate time delays to enable the pulses to be focused by the reflector. As a single element response placed at the focus is synthesized, a wide transmit beam with high acoustic power is radiated over the entire target field.

#### 6.3 Calculation parameters

A set of parameters for investigating spatial resolution of a 3-D acoustic imager based on a hybrid method is shown in [114]. We follow this set in this paper: mean propagation velocity  $c_0 = 1600$  m/s, density of the undisturbed medium  $\rho_0 = 1.08 \times 10^3$  kg/m³, the variation of the propagation velocity  $\Delta c = -300$  m/s, and the variation of the density  $\Delta \rho = -1.0 \times 10^2$  kg/m³. The attenuation coefficients of the intrabody and the impedance matching fluid are  $2.0(\omega/2\pi)^2 \times 10^{-14}$  and  $5.0(\omega/2\pi) \times 10^{-6}$  Np/m, respectively. The element pitch is half the wavelength  $\lambda$  at the center frequency, where the center frequency is 1.6 MHz and -6 dB fractional band width is 60 %. A circular 2-D array of 0.016 m in diameter is employed, where the element pitch is 0.0005 m. The number of elements is 797. The reflector size is 0.062 m long and 0.08 m wide.

# 6.4 Transmit time delays for focusing the transmit beam

In this section, we first propose a method that utilizes numerical back-projection to calculate the transmit waveform for focusing the transmit pulses at a point. In this case, we assume that a spherical wave is radiated backward from the focus; we then calculate the received signal at each element on the array. The phase of the transmit pulse is the reverse of the received signal.

The waveform of the received signal is particular to each element because the transmission pass from the focus is unique to the element position. As radiating different individual waveforms from all elements is impractical because the number of elements is 797, all elements radiate ultrasound pulses of the same waveform with different time delays. We introduce the assumption that the waveform radiated backward from the focus is the same as that radiated from all elements. We calculate the time delay by maximizing

$$E(\tau) = \int p(t - \tau)q(t)dt, \tag{6.1}$$

where p(t) is the waveform radiated backward from the focus, q(t) is the waveform received at an element, and t is the transmit time delay of the element. The transmit waveform radiated from the element is  $p(t + \tau)$ .

#### 6.5 The Region with a guaranteed focus

In this section we evaluate the region in which the focus is guaranteed for radiating an ultrasound beam in a direction. In the geometric optics shown in Fig. 6.3, a transmit pulse from an element is reflected by the mirror and then radiated to the measurement point  $(T_a)$  after passing through the focus  $(T_r)$ . In the same way, the inverse pass  $T_aT_r$ 

arrives at the array after being reflected by the mirror. For radiating a transmit beam to  $T_a$ , it is therefore necessary that the focus exists in the region between  $T_a$  and the used area. The used area is the region on the mirror where the echo from  $T_a$  is reflected and arrives at the array. We call this as the region with a guaranteed focus (RGF), as shown in Fig. 6.4.

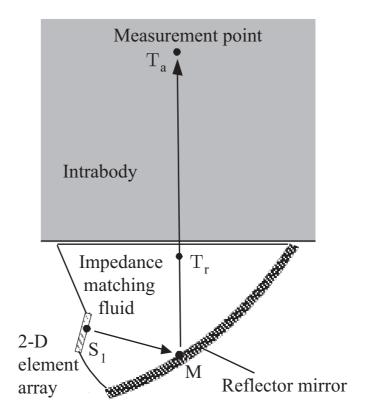


Figure 6.3: A transmit pass in geometric optics. In geometric optics a transmit pulse from an element is reflected by the mirror, and then radiated to the measurement point  $T_a$  after passing through the focus  $T_r$ .

Fig. 6.5 shows the radiation pattern of the proposed imager. In this calculation we set the focus at the origin. The -6 dB transmit beam width is  $1.8\lambda$ in the x-y section. This indicates that the transmit power is gathered at the focus; that is, the time delays employed to the elements are proper. At a 0.07 m depth in a region with an x coordinate of more than -0.013 m and less than 0.03 m, the transmit power is greater than -6 dB compared with the peak power: the amplitude half-width is 33.7 degrees. Therefore, the proposed imager measures a target field of 33.7 degrees of visual angle as a single transmit and receive event.

Fig. 6.6 shows the RGFs on the x axis. The regions, whose x coordinates of measure-

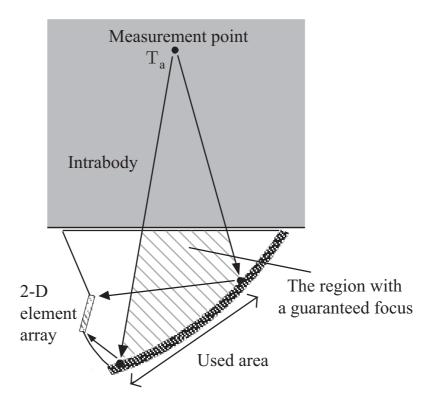


Figure 6.4: The Region with a guaranteed focus. When the focus is contained within the region, the transmit wave is radiated to the measurement point  $T_a$ .

ment points are -0.015 m to 0.03 m, contain the origin and that whose x coordinate is -0.03 m does not contain the origin. This corresponds to the radiation pattern shown in Fig. 6.5. Therefore to radiate a certain measurement point, the focus should be arranged in the RGF of the point.

#### 6.6 Improvement of the spatial resolution by multiple transmit and receive events

Since a single transmit and receive event can make a 3-D image in the proposed method, the time resolution is 5000 images/s when the measurement range is 0.16 m. For medical diagnoses a lower time resolution is sufficient, and so the spatial resolution and SNR can be improved from multiple transmit and receive events. Utilizing a synthetic aperture technique, the coherent integration of multiple receive signals of different transmit points equivalently enlarges the aperture size, and thus the spatial resolution is improved. With this method we can change the focal position by employing proper time delays.

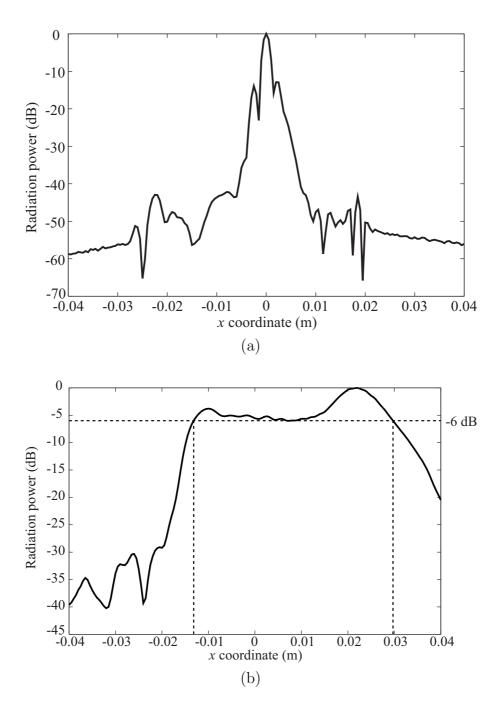


Figure 6.5: Radiation pattern of the proposed imager in the x-z section for (a) 0 m and (b) 0.07 m depths.

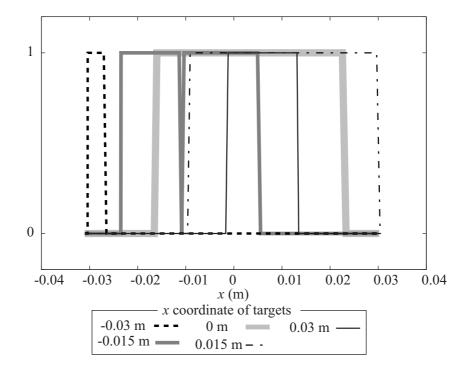


Figure 6.6: The regions with a guaranteed focus on the x axis. The regions, whose x coordinates of measurement points are -0.015 m to 0.03 m, contain the origin and that whose x coordinate is -0.03 m does not contain the origin. This corresponds to the radiation pattern shown in Fig. 6.5(b).

When measuring a fast moving organ, such as the heart of a fetus, a time resolution of 300 3-D images/s is needed. In this case, the spatial resolution can be improved from 16 transmit and receive events by using a synthetic aperture technique. As shown in Fig. 6.7, we arrange the 16 focuses for a -0.01 m depth. The transmit wave is radiated in the direction where the RGF contains the focus. Therefore, the spatial resolutions for point targets at the x coordinates of -0.015, 0, 0.015 m are improved respectively from 10, 14, 8 transmit and receive events. Receiving a large part of the echo reflected on the mirror has the same effect as using a large array. As shown in [113], the echo passing through a section of the RGF are received on the array; thus the spatial resolution of the proposed imager is equivalent to that of a digital beamforming imager with an array of the same size as the section of the RGF. Then we call the section of the RGF as the effective aperture. Fig. 6.8 shows the synthesized aperture from 14 events when measuring the center for a 0.07 m depth; where we introduce the approximation that a spherical wave is radiated from the focus. The coherent integration utilizing the synthetic aperture technique realizes a spatial resolution equivalent to that of an aperture given by the convolution of the focuses and the effective aperture.

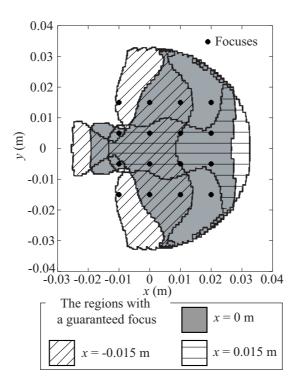


Figure 6.7: Arrangement of the focuses and the regions with a guaranteed focus for a -0.01 m depth.

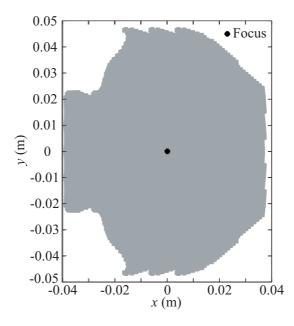


Figure 6.8: The synthesized aperture from 14 transmit and receive events when measuring the center for a 0.07 m depth.

#### 6.7 Results and Discussion

Fig. 6.9 shows the spatial resolution of the proposed imager acquired from single and 16 transmit and receive events. As noted above, the spatial resolutions of the x coordinates of -0.015, 0, 0.015 m are improved, respectively, from 10, 14, 8 transmit and receive events by utilizing a synthetic aperture technique.

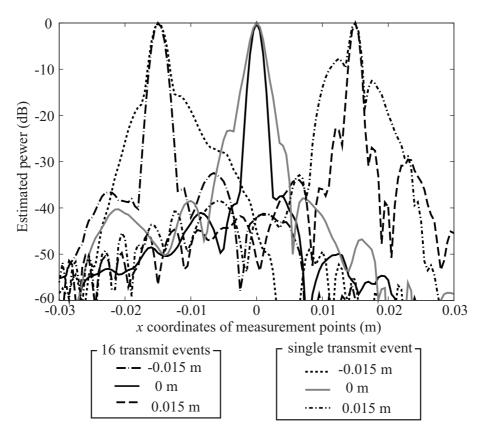


Figure 6.9: Lateral resolution of the proposed imager acquired from single and 16 transmit and receive events in the x-z section for a 0.07 m depth. The x coordinates of point targets are -0.015, 0 and 0.015 m.

We compare the spatial resolution of the proposed imaging method with that using the digital beamforming method. The spatial resolution of digital beamforming imagers is improved from 16 transmit and receive events. As shown in Fig. 6.10, the x-z and y-z section -3 dB lateral resolutions are about  $1.30\lambda$  and  $1.17\lambda$ , respectively. A target exists at the center for a 0.07 m depth. They are the same as those of a digital beamforming imager with an elliptic array of 0.041 m long and 0.047 m wide. Because the elements are spaced at intervals of one-half of a wavelength on the array, the area of the array is proportional to the number of elements. Therefore, the number of elements can be

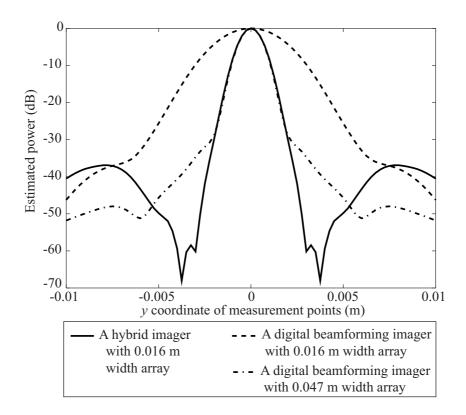


Figure 6.10: Lateral resolution of the proposed imager with a 0.016 m width array and digital beamforming imagers with 0.016 and 0.047 m width arrays. A point target exists at the center for a 0.07 m depth. The spatial resolutions of the proposed imager and digital beamforming imagers are improved, respectively, from 14 and 16 transmit and receive events.

reduced to about 1/7.5 of a dense 2-D array having the same spatial resolution.

#### 6.8 Conclusion

To realize a high resolution acoustic real-time 3-D imaging system, we proposed one based on a hybrid method utilizing a synthetic aperture technique. Since images of the entire measurement field are reconstructed as single transmit and receive event, we can reconstruct a 3-D image from multiple transmit and receive events with sufficient time resolution. When the time resolution is 300 3-D images/s, by utilizing the synthetic aperture technique the coherent integration of 16 transmit and receive events improves the spatial resolution. Image reconstruction from 16 events realizes a lateral resolution of  $1.30\lambda$  in the x-z and  $1.17\lambda$  in the y-z sections for a 0.07 m depth, where the center frequency is 1.6 MHz, the width of the reflector is 0.062 m long and 0.08 m wide, and

the array is a circle 0.016 m in diameter. This shows that the number of elements can be reduced to about 1/7.5 of a dense 2-D array having the same spatial and time resolution but using a digital beamforming method with a synthetic aperture technique.

# Appendix A

# Production of the coefficient used in Eq. 2.1.

The particle velocity  $v_{\rm T_10}$  is given by

$$v_{\rm T_{10}} = b_{\rm v} \frac{1 + jkr}{r^2} e^{-(\alpha + jk)r},$$
 (A.1)

where we assume the transmit element as a point source and  $b_{\rm v}$  is a constant value. In the far field, that is, in the condition that the particle velocity  $kr \gg 1$  and the pressure variety  $v_{\rm T_{10}}$  have the same phase, and the following equation is satisfied.

$$p_{\rm T_{10}} = \frac{\rho \omega}{k} p_{\rm T_{10}}.$$
 (A.2)

Therefore, the acoustic power I is given by

$$I = \frac{1}{2} p_{\text{T}_1 0} v_{\text{T}_1 0}^* = \frac{k \rho \omega b_{\text{v}}^2}{2r^2} e^{-2\alpha r}.$$
 (A.3)

When the attenuation coefficient  $\alpha = 0$ , the transmit power is given by  $W = 4\pi r^2 I$ , and thus the following equations are obtained.

$$W = 2\pi b_{\rm v}^2 k \rho \omega, \tag{A.4}$$

$$b_{\rm v} = \sqrt{\frac{W}{2\pi k \rho \omega}}. \tag{A.5}$$

Therefore, the particle velocity is obtained by

$$v_{\mathrm{T}_{10}} = \sqrt{\frac{W}{2\pi k \rho \omega}} G_{\mathrm{r}} R_{\mathrm{r}}(x, y, z) \frac{1 + jkr}{r^{2}} \cdot e^{-(\alpha + jk)r}. \tag{A.6}$$

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# **Major Publications**

#### Refereed Papers

- 1. H. Taki, H. Yashima, and T. Sato, "Study of the Hybrid Method and the Sensor for a High-Resolution Ultrasound Vision Substitute System for Visually Handicapped," (in Japanese) IEICE Trans. Electron., vol. J88-A, No.5, pp. 568-576, 2005.
- 2. H. Taki, and T. Sato, "Transfer Information Enhancement with a 2-D Tactile Stimulator Array for an Acoustic Vision Substitute System," IEICE Trans. Electron., Accepted.

#### Refereed Conference Proceedings

- 1. H. Taki, and T. Sato, "High-Resolution Real-Time 3-D Acoustic Imaging System with a Reflector," Proc. 2nd IASTED international conference on Biomedical Engineering, Feb., 2005.
- 2. H. Taki, and T. Sato, "Human Interface and Transmit Frequency Control for the Through-Air Acoustic Real-Time High Resolution Vision Substitute System," Proc. 27th IEEE Annual International Conference of the Engineering in Medicine and Biology Society, 2005.
- 3. H. Taki, and T. Sato, "Transfer Information Enhancement with a 2-D Tactile Stimulator Array for Acoustic Vision Substitute System," Proc. 28th IEEE Annual International Conference of the Engineering in Medicine and Biology Society, 2006.